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# Unemployment Facts

704 Macroeconomic Theory II  
Topic 1

Masao Fukui

2024 Spring

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# Course Logistics

- Lecture:
  - Tuesdays, Thursdays, 11-12:15, in CDS 463
- Instructor:
  - Masao Fukui ([mfukui@bu.edu](mailto:mfukui@bu.edu))
  - Office hours: Mon 2:45-5:45pm in Room 400
- TA:
  - Shraddha Mandi ([mandis@bu.edu](mailto:mandis@bu.edu))
  - Office hours: 12:30-2:30 in room 413
- Sections: Tu 3:30-4:45 in CAS 116

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# Grades

- Grades:
  - 40% problem sets
  - 60% final exam
- There will be 4 problem sets
  - Strongly encouraged to work in a group
  - But each student must hand in their own write-up.
  - Strongly encouraged to write in LaTeX
  - Write as if you were writing a paper and submitting it to a journal. Don't paste the screenshot of Stata output window!
- The first problem set is already posted. Due March 29th.

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# Course Overview

**Frictionless models**  
(Neoclassical growth, RBC)

**1. Goods market friction:**  
Price stickiness (NK)

**2. Labor market friction:**  
Search & matching

**3. Financial market friction**

- First half: labor market frictions
- Second half: financial market frictions

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# What is Unemployment?

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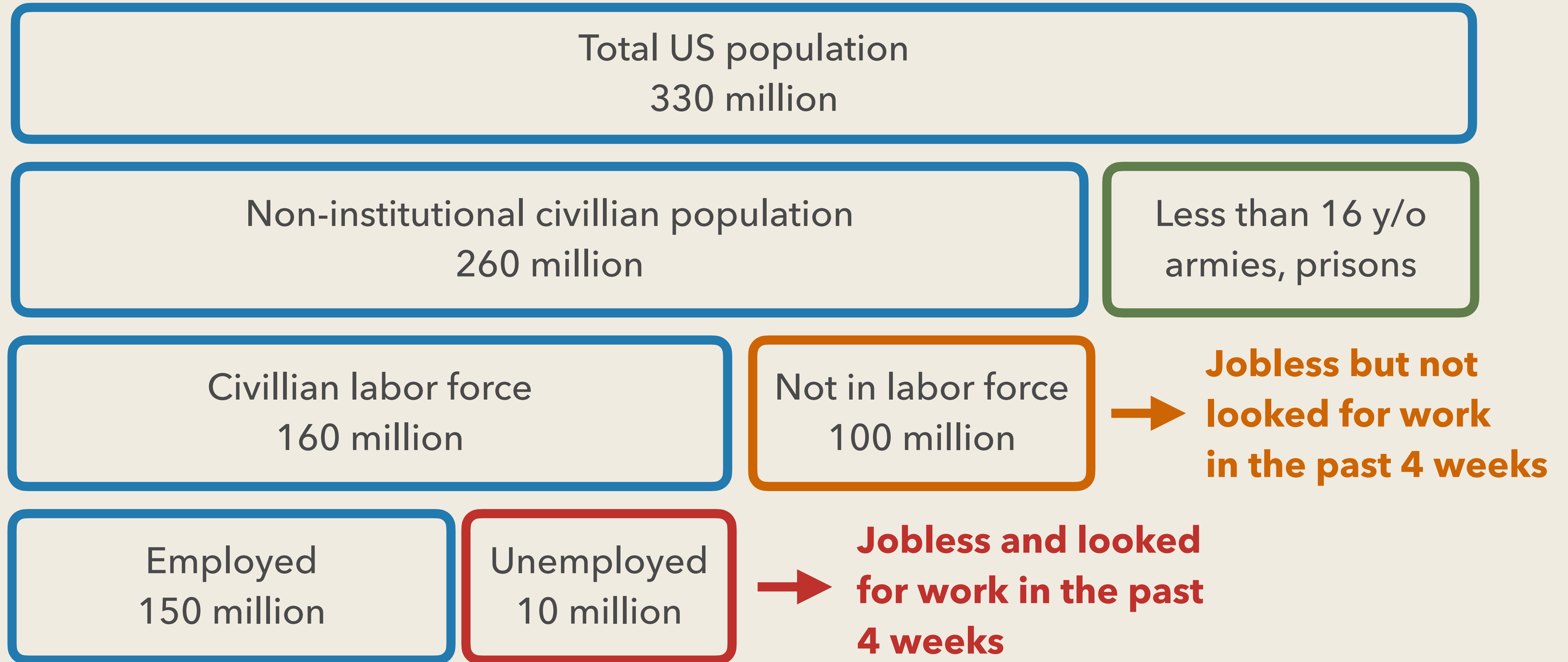
# Why Study Unemployment?

- Unemployment is often a central focus in business cycles
- Why care about unemployment?
  - Individual: lower income, consumption, and emotional well-being
  - Aggregate: Potentially under-utilization of resources
- Questions:
  1. Why is there unemployment? Why does it fluctuate?
  2. Is unemployment inefficient?
  3. What policies should we implement?
- But before theorizing, we need to define and measure unemployment

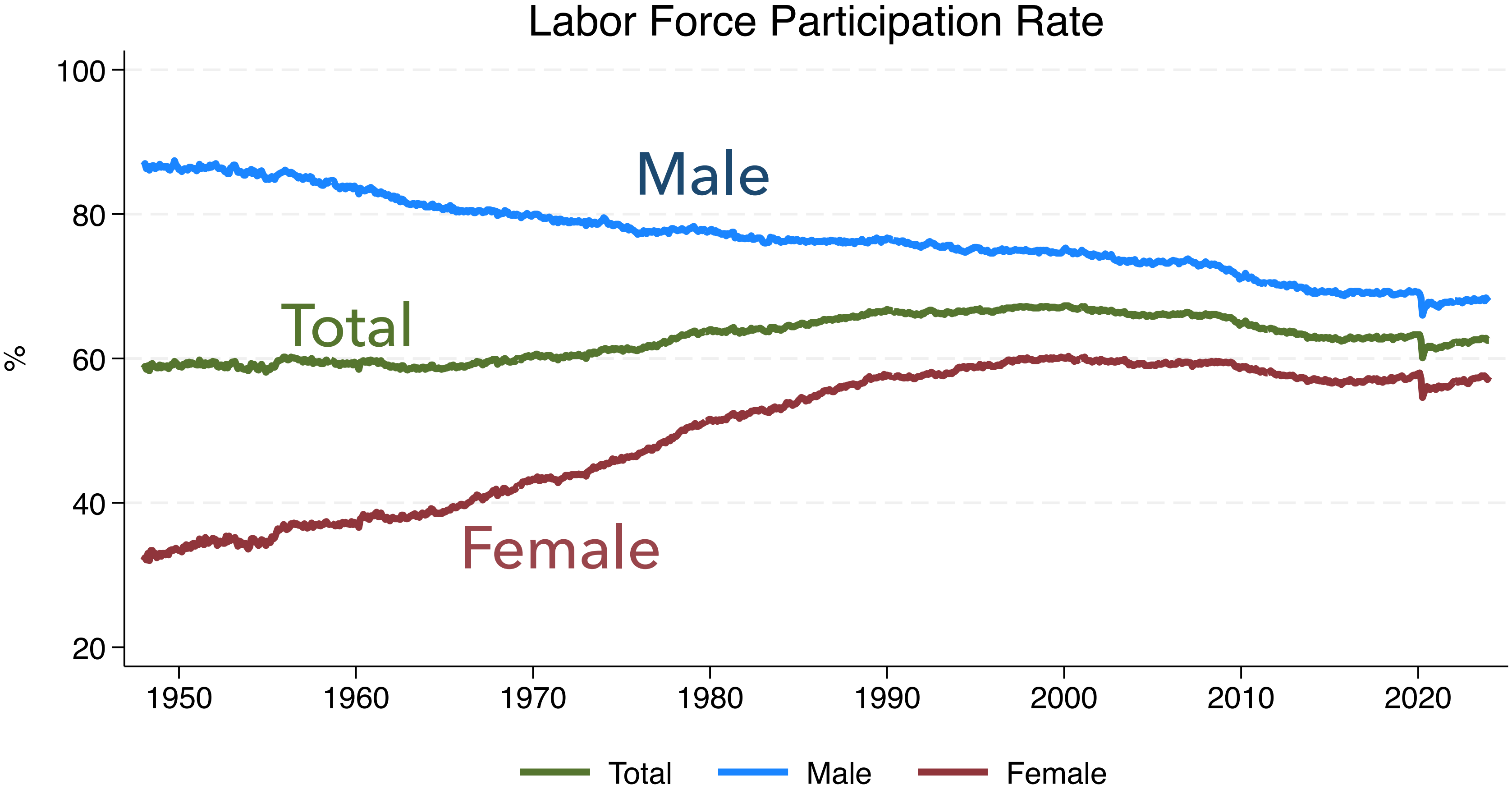
→ Ganong-Noel (2018)

→ Krueger-Meuller (2012)

# Defining Unemployment



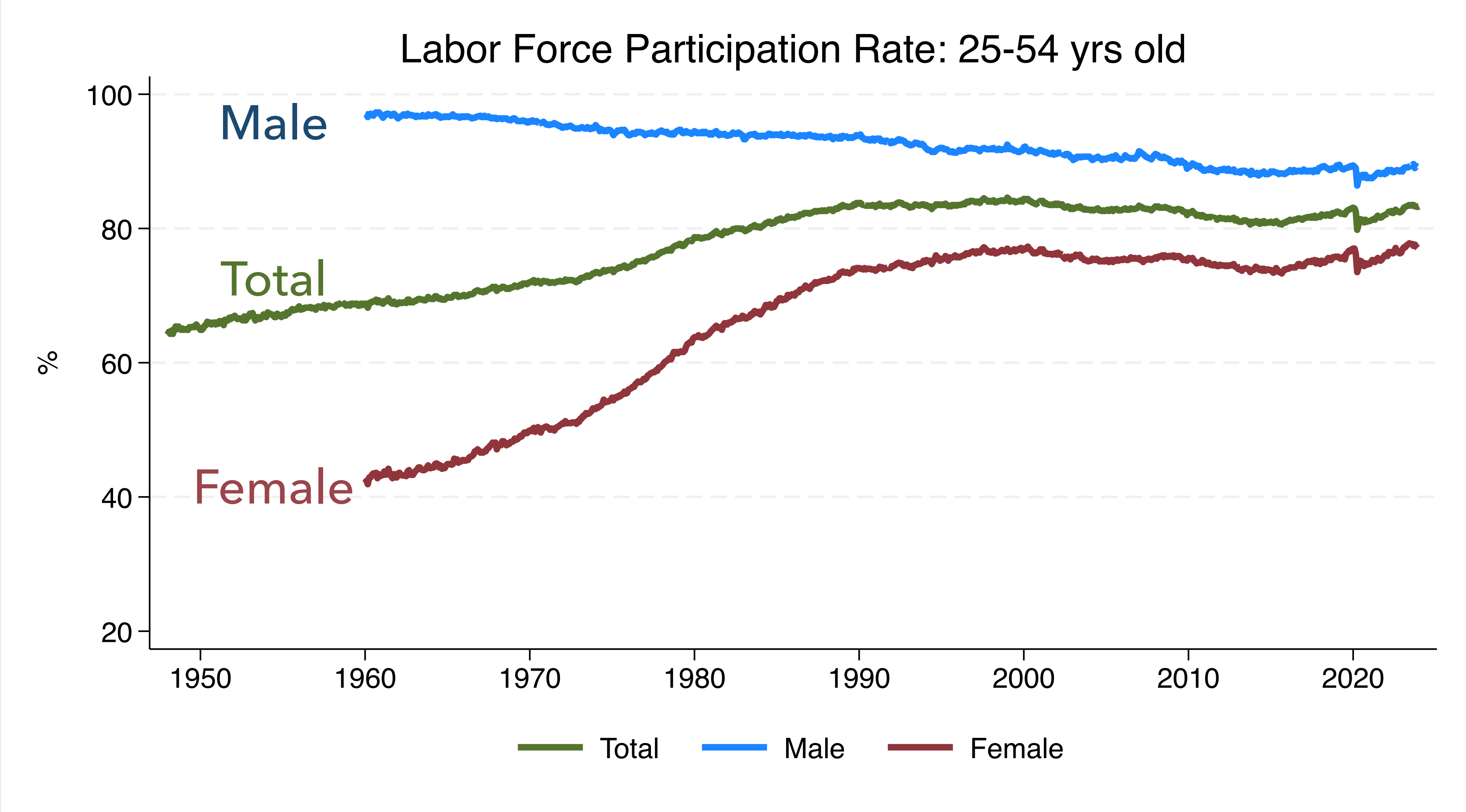
# Labor Force Participation Rate



- Male: declining trend
  - aging
  - longer education
  - wealth effect
  - leisure tech
- Female: rising trend
  - social norm
  - home production technology
  - service sector



# Prime Age Labor Force Participation Rate

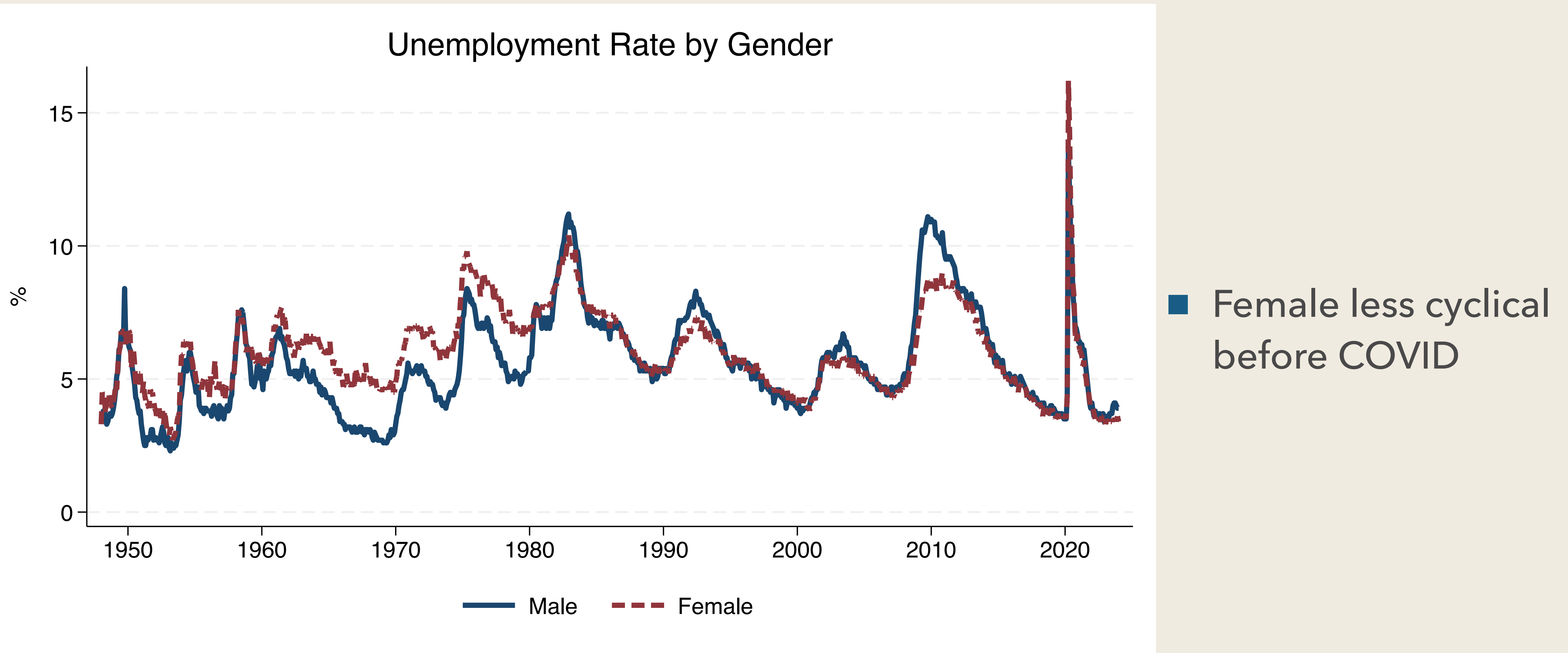


# Unemployment Rate



Data: NBER Macro History Database and CPS

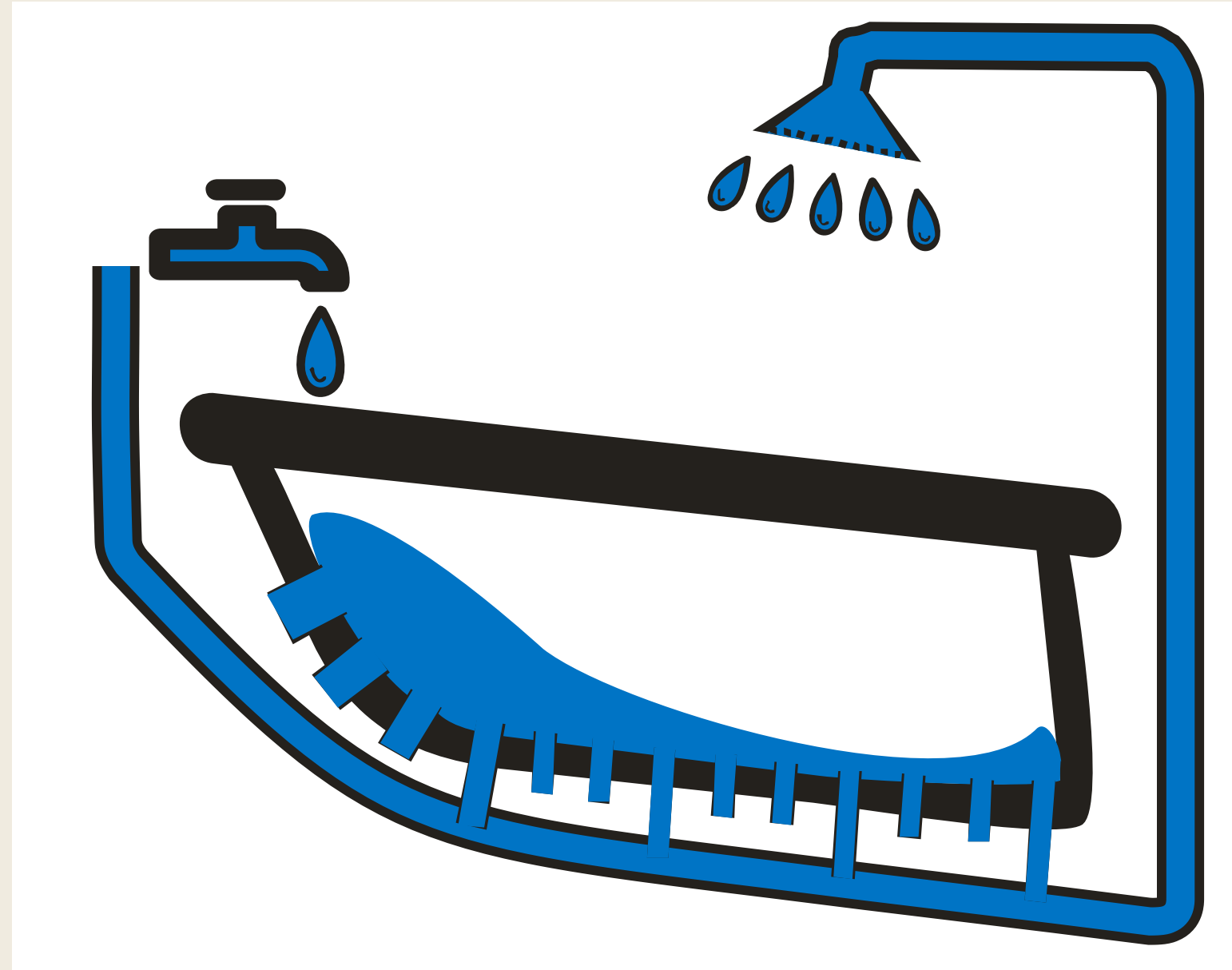
# Unemployment Rate by Gender



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# Flows Into and Out of Unemployment

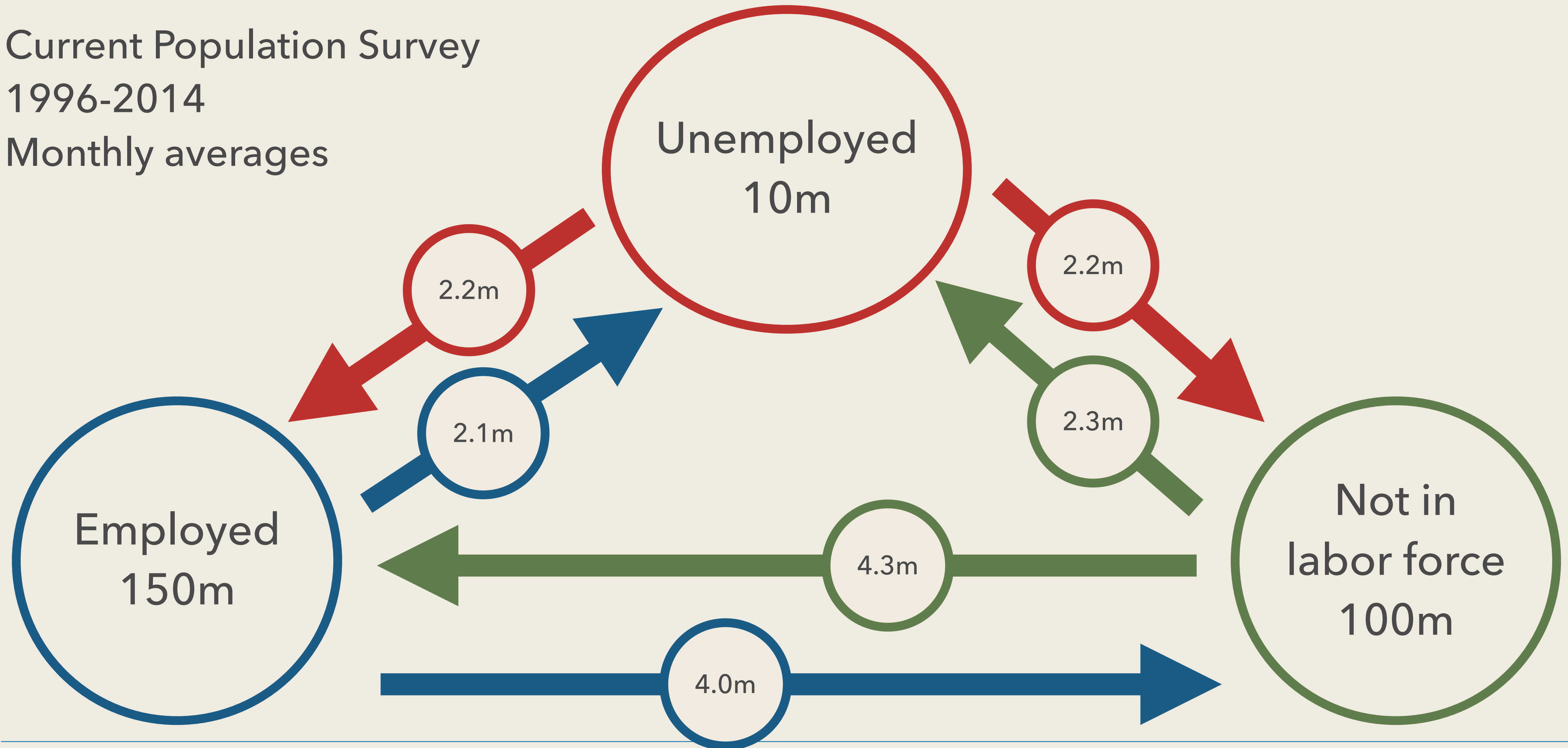
# Stock-Flow Accounting Model



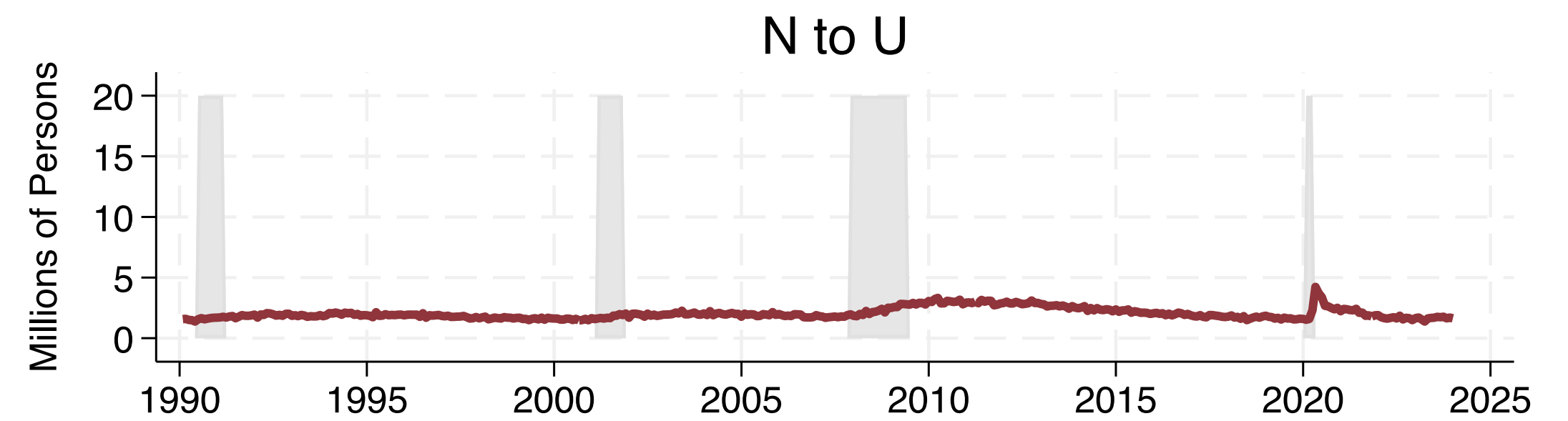
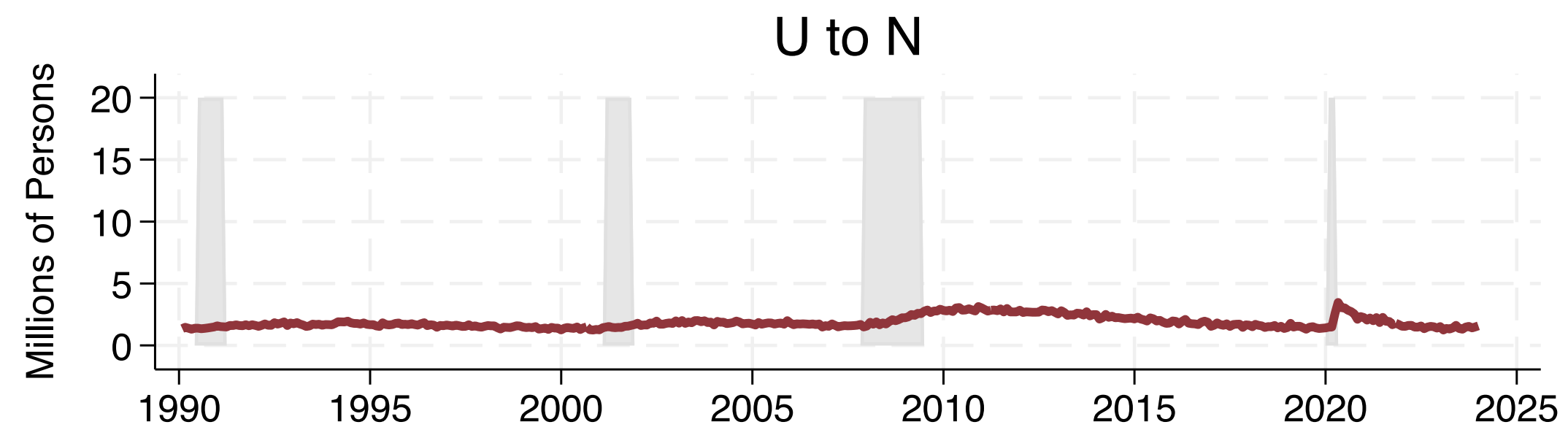
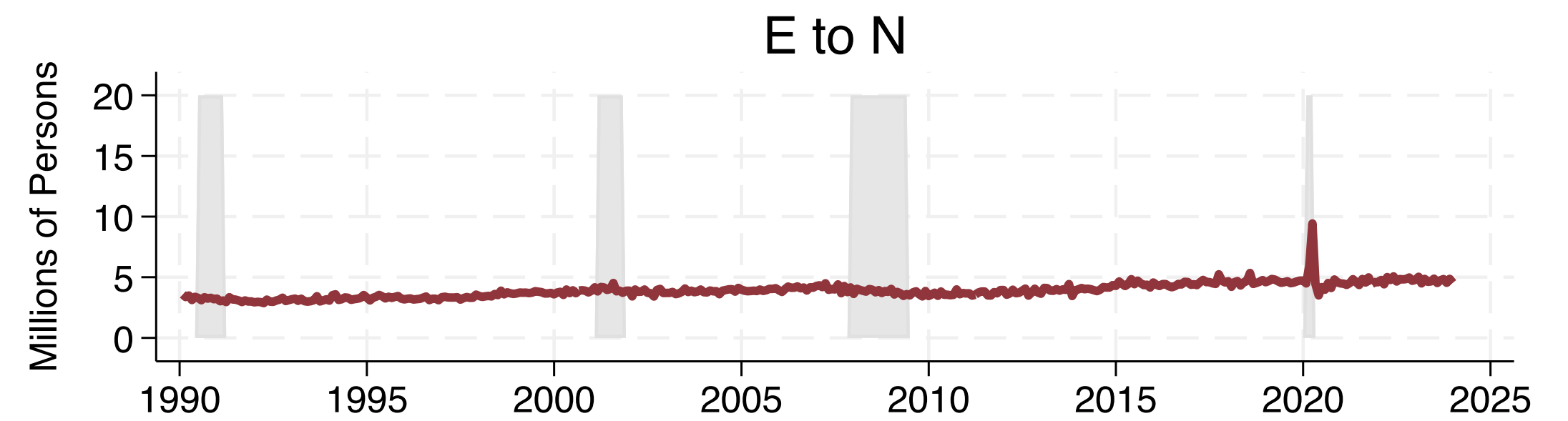
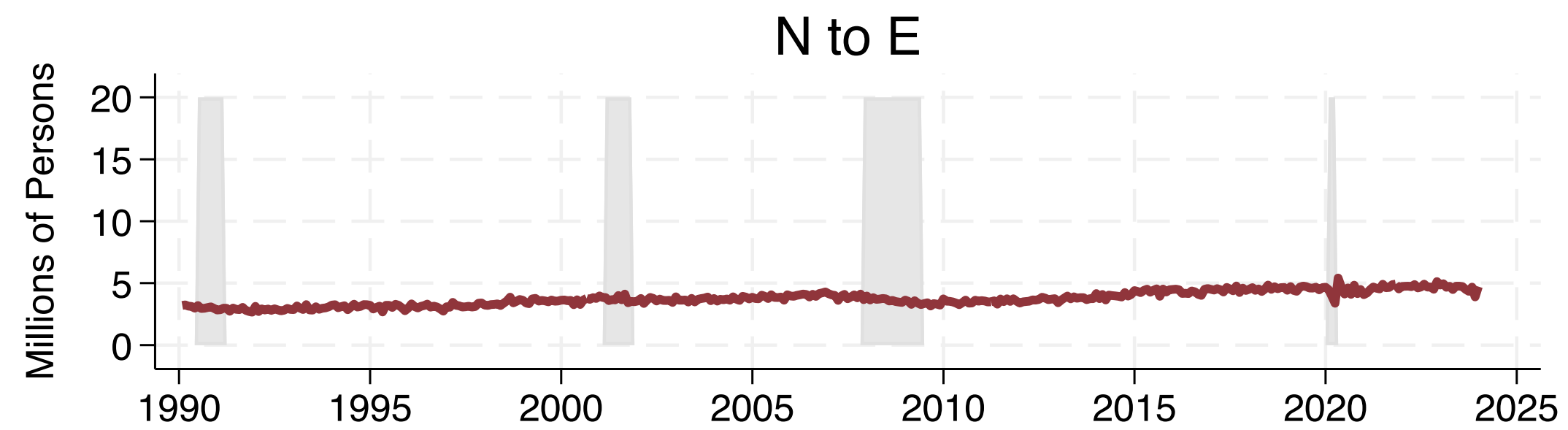
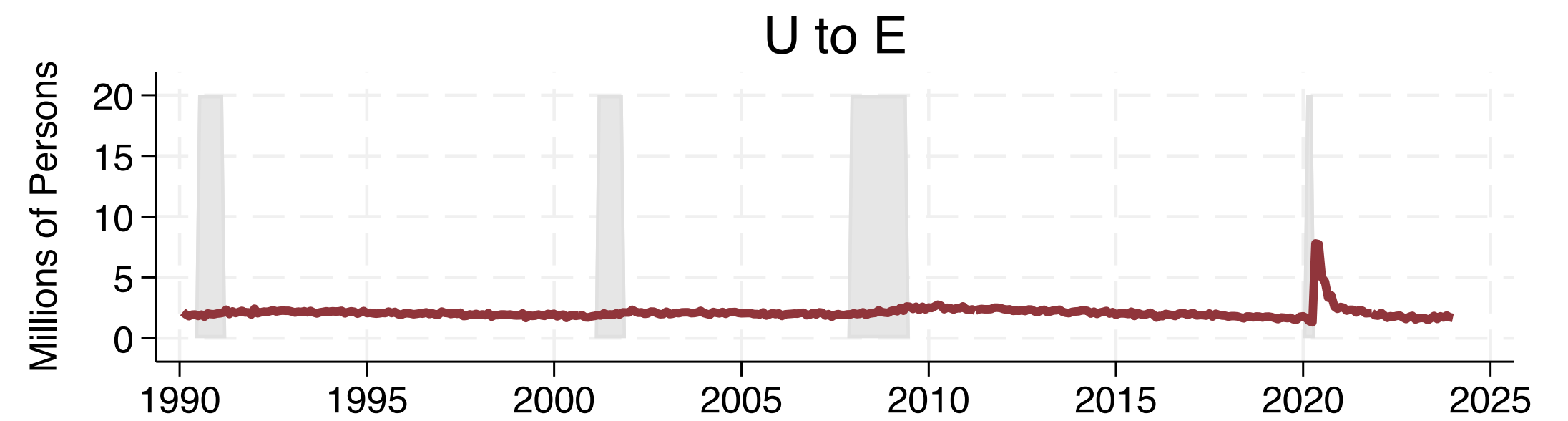
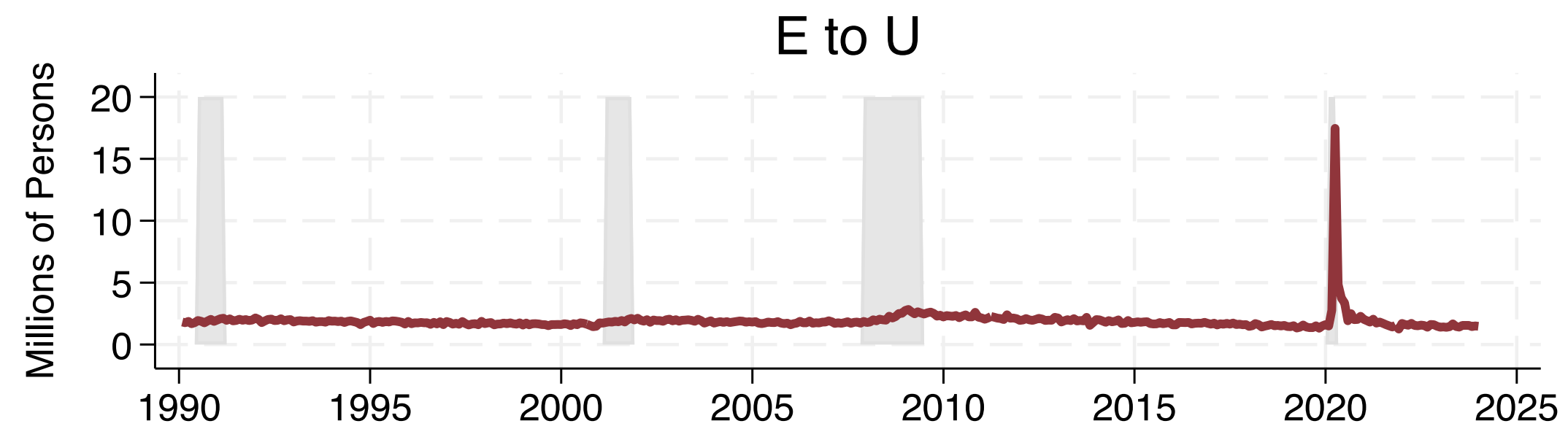
- Unemployment represents a stock of workers
  - Determined through a balance between inflows and outflows
- Useful to break down the role of inflows vs. outflows
  - Disciplines the model we should be writing down

# Flows are Large on Average

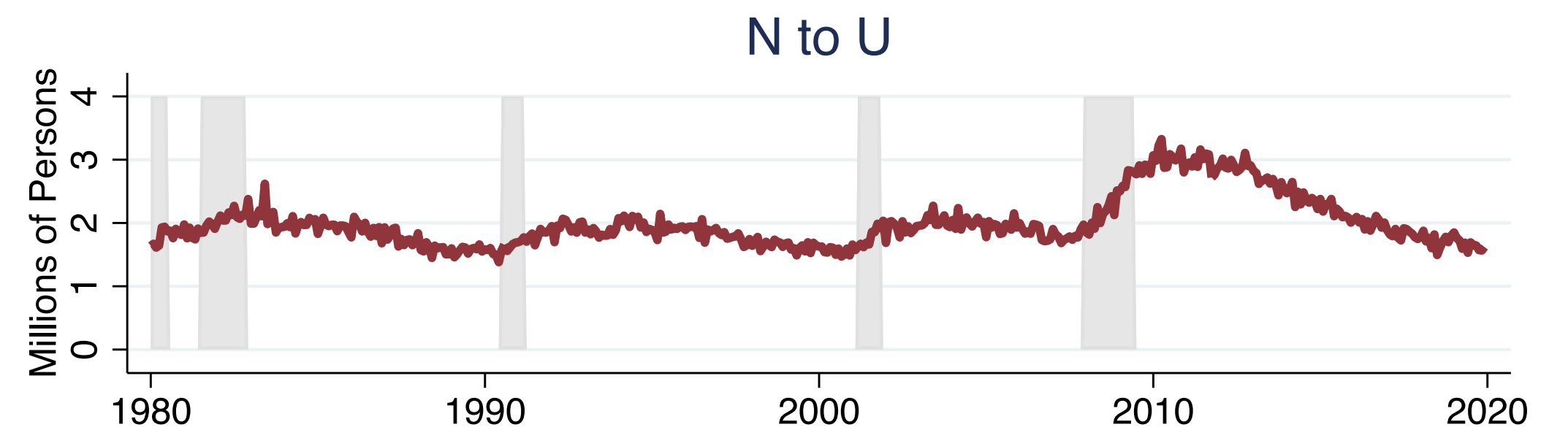
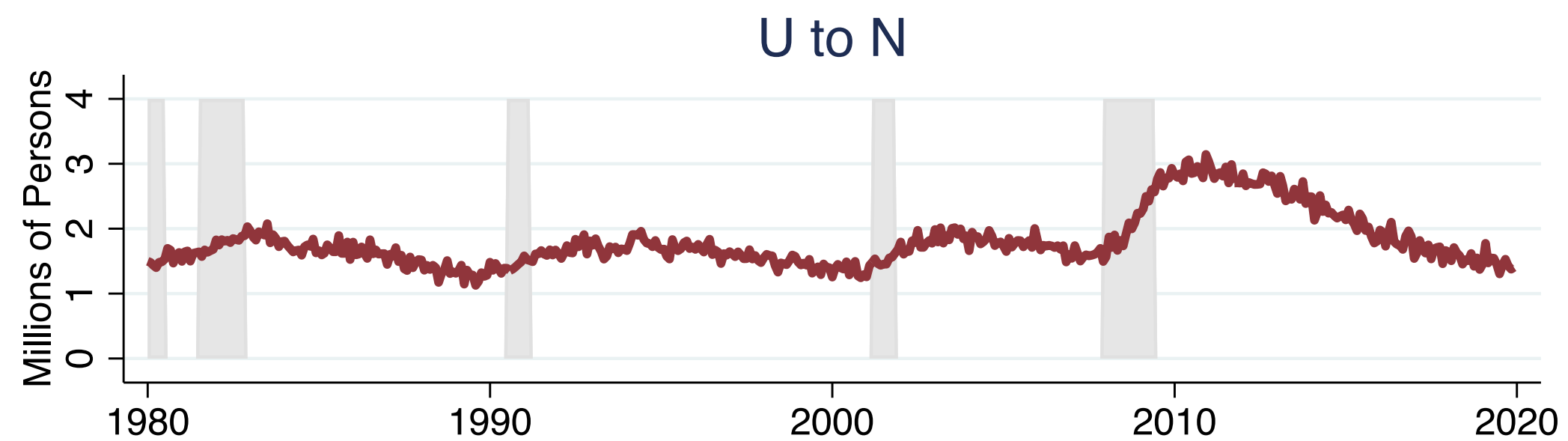
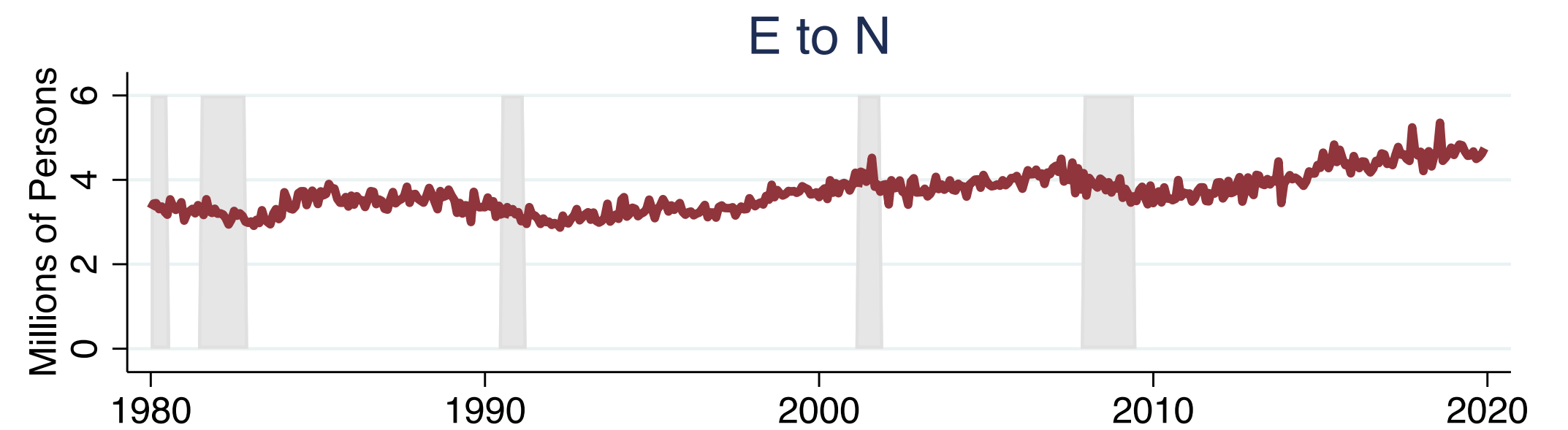
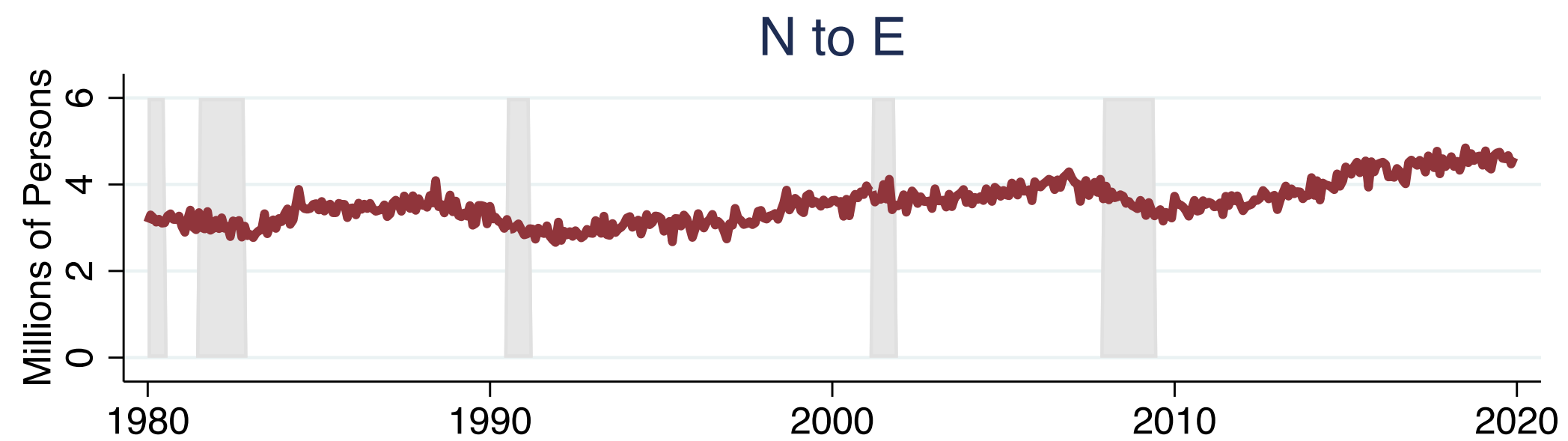
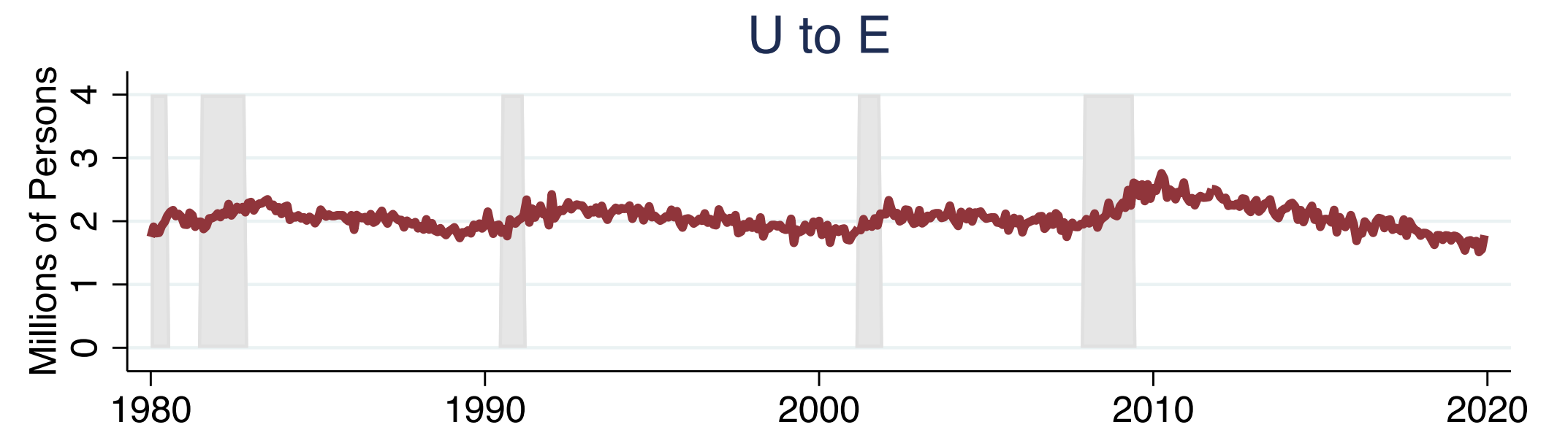
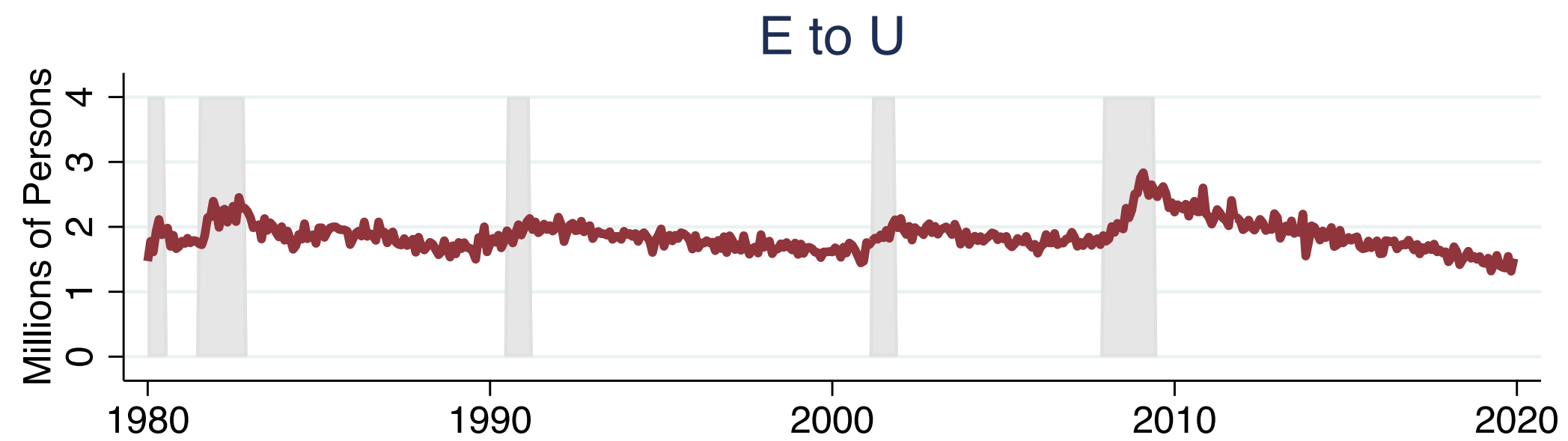
Current Population Survey  
1996-2014  
Monthly averages



# Labor Market Flows over Time



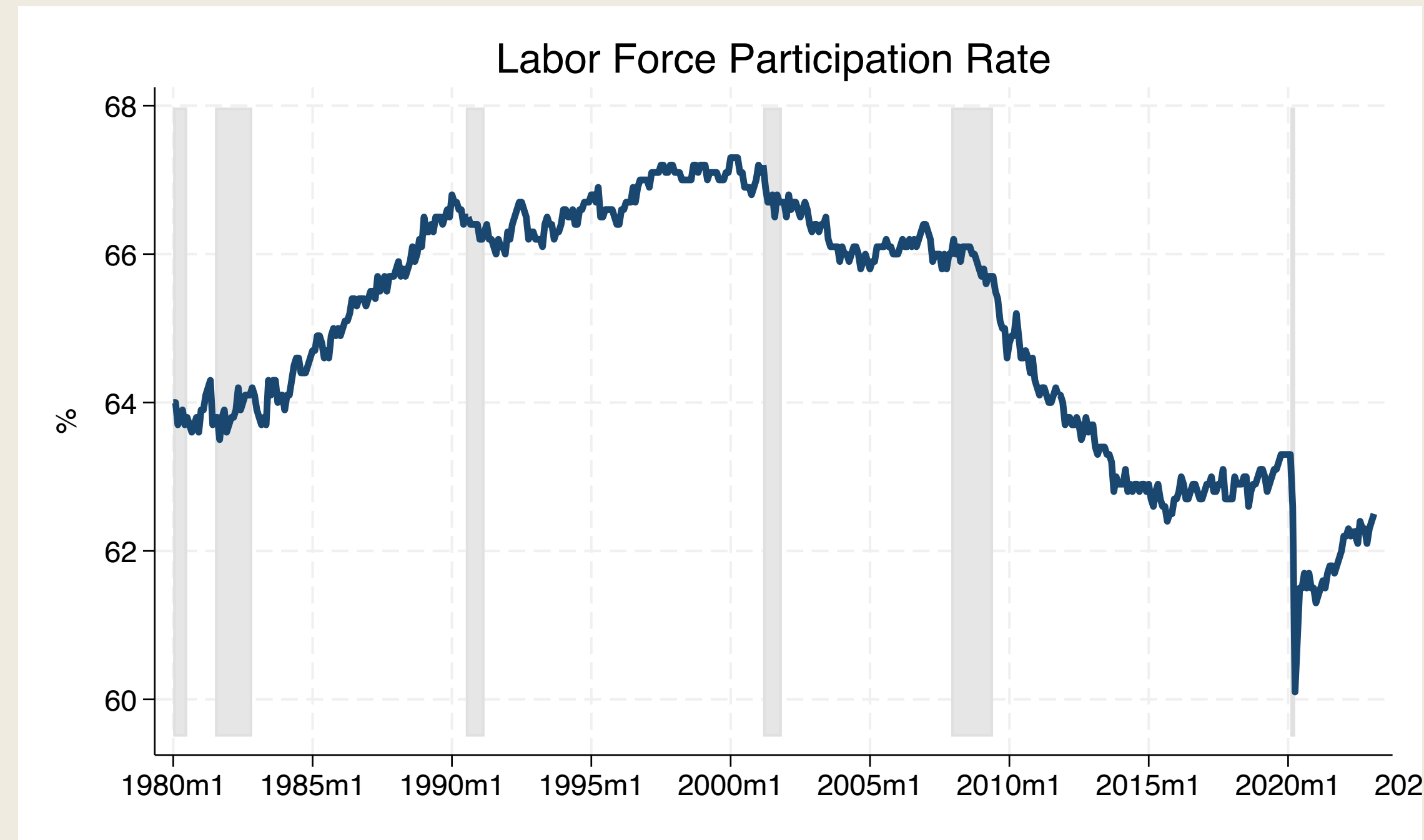
# Labor Market Flows before COVID





# Not in the Labor Force

- We will abstract from individuals not in the labor force
  - One justification is that the labor force participation is not very cyclical
  - Active research on how flows in to and out of N matters.

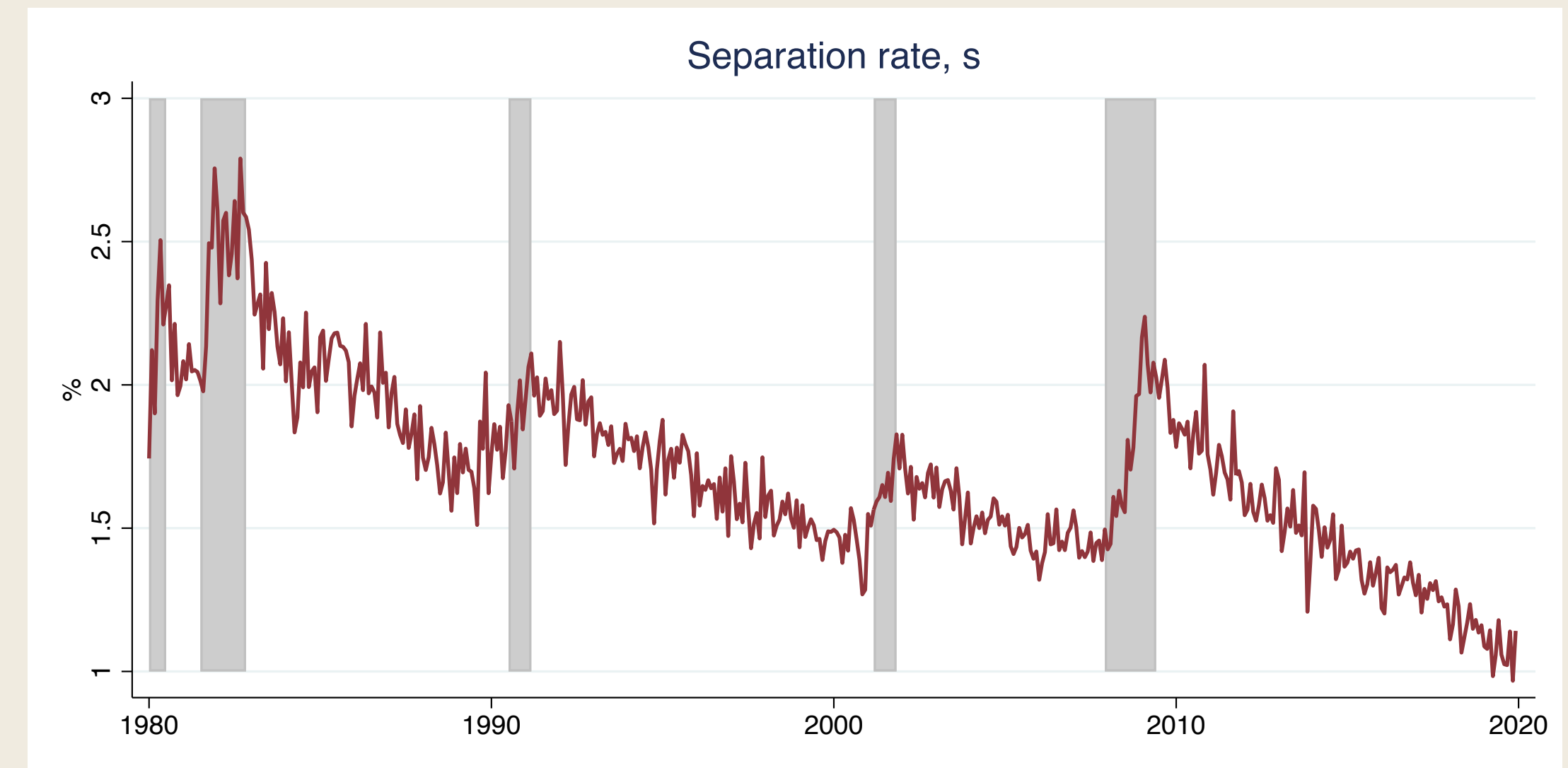
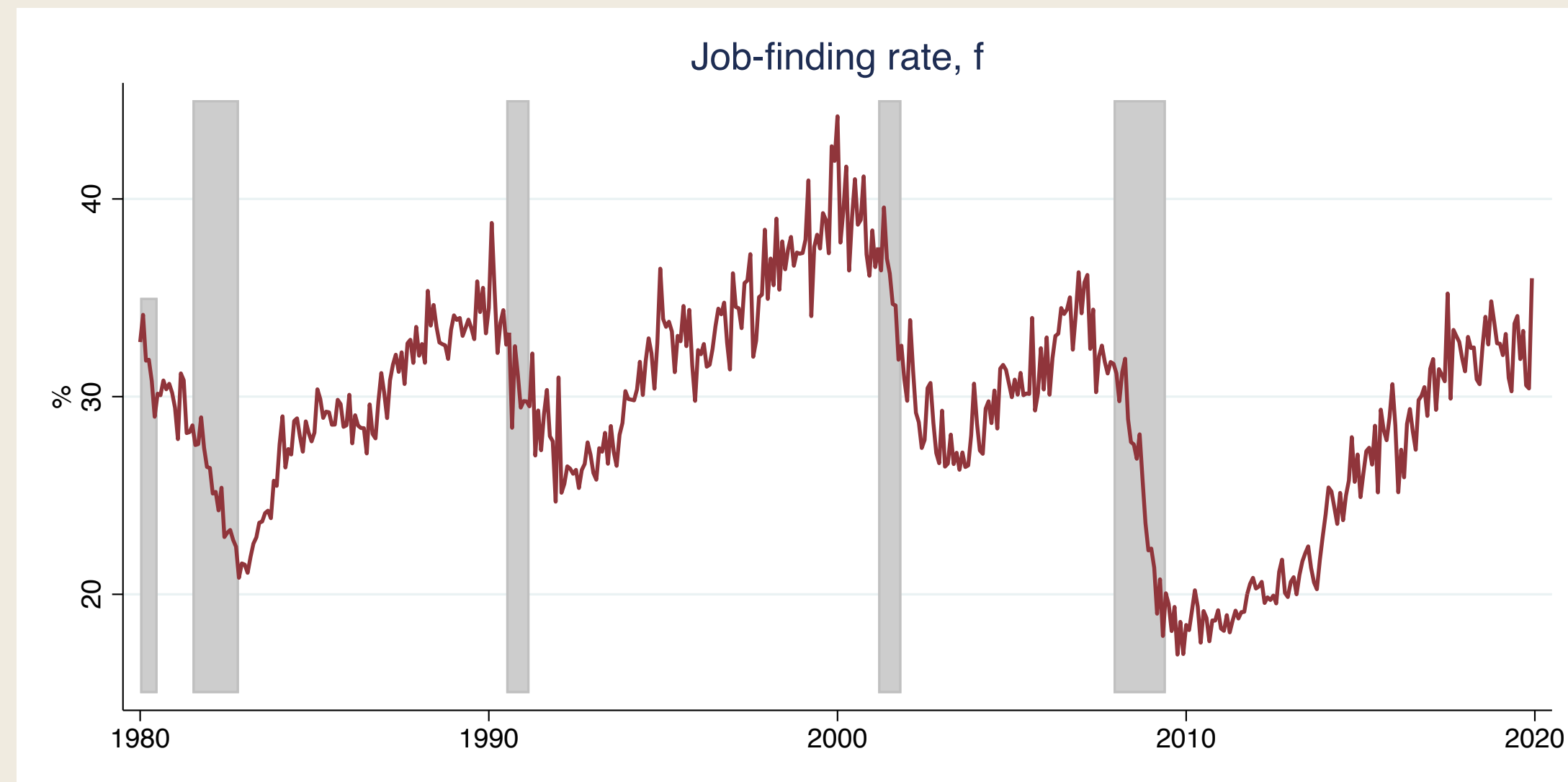


- Normalize:  $U + E = 1$

# Stock-Flow Model

- Basic stock-flow accounting equation:

$$\underbrace{u_{t+1} - u_t}_{\text{changes in unemployment}} = \underbrace{s_t(1 - u_t)}_{\text{separation (inflow into U)}} - \underbrace{f_t u_t}_{\text{job-finding (outflow from U)}}$$



- Is unemployment fluctuations due to fluctuations in  $f_t$  or  $s_t$ ?

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# Approximate Unemployment Rate

- In the steady state,

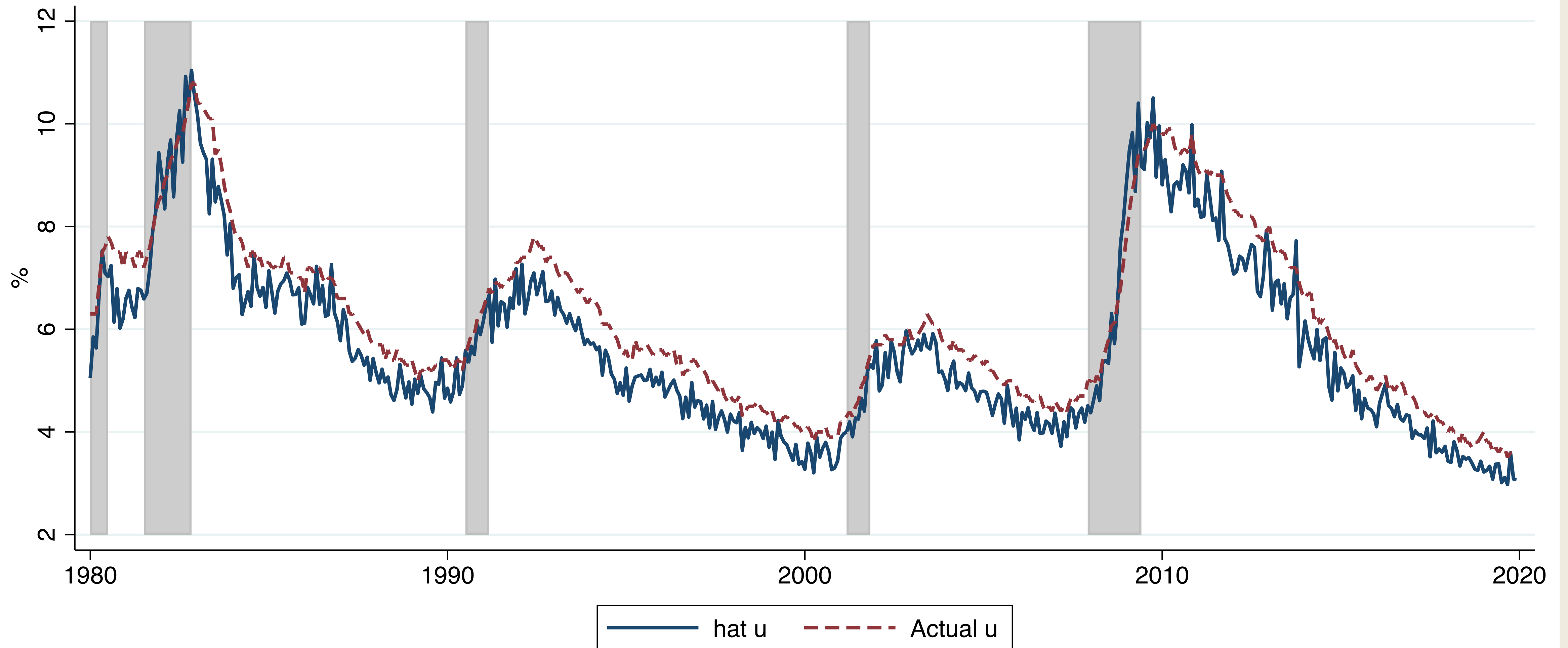
$$\bar{u} = \frac{\bar{s}}{\bar{s} + \bar{f}}$$

- Out of steady state, no such simple formula
- But if transitions are “fast enough”, we can approximate

$$u_t \approx \frac{s_t}{s_t + f_t} \equiv \hat{u}_t$$

- Unemployment is “as if” steady-state with contemporaneous flow
- Can use this approximate formula to unpack the role of inflows vs. outflows

# Approximation is Excellent



# How Much Fluctuations in $u$ due to $s$ or $f$ ?

- Rewrite  $\hat{u}_t = s_t/(s_t + f_t)$  as

$$\frac{\hat{u}_t}{1 - \hat{u}_t} = \frac{s_t}{f_t}$$

- Taking log of both sides, the variance of  $\log(\hat{u}_t/(1 - \hat{u}_t))$  can be decomposed into

$$\text{Var} \left[ \log \frac{\hat{u}_t}{1 - \hat{u}_t} \right] = \underbrace{\text{Cov} \left[ \log \frac{\hat{u}_t}{1 - \hat{u}_t}, \log s_t \right]}_{\text{flutuations due to } s} + \underbrace{\text{Cov} \left[ \log \frac{\hat{u}_t}{1 - \hat{u}_t}, -\log f_t \right]}_{\text{flutuations due to } f}$$

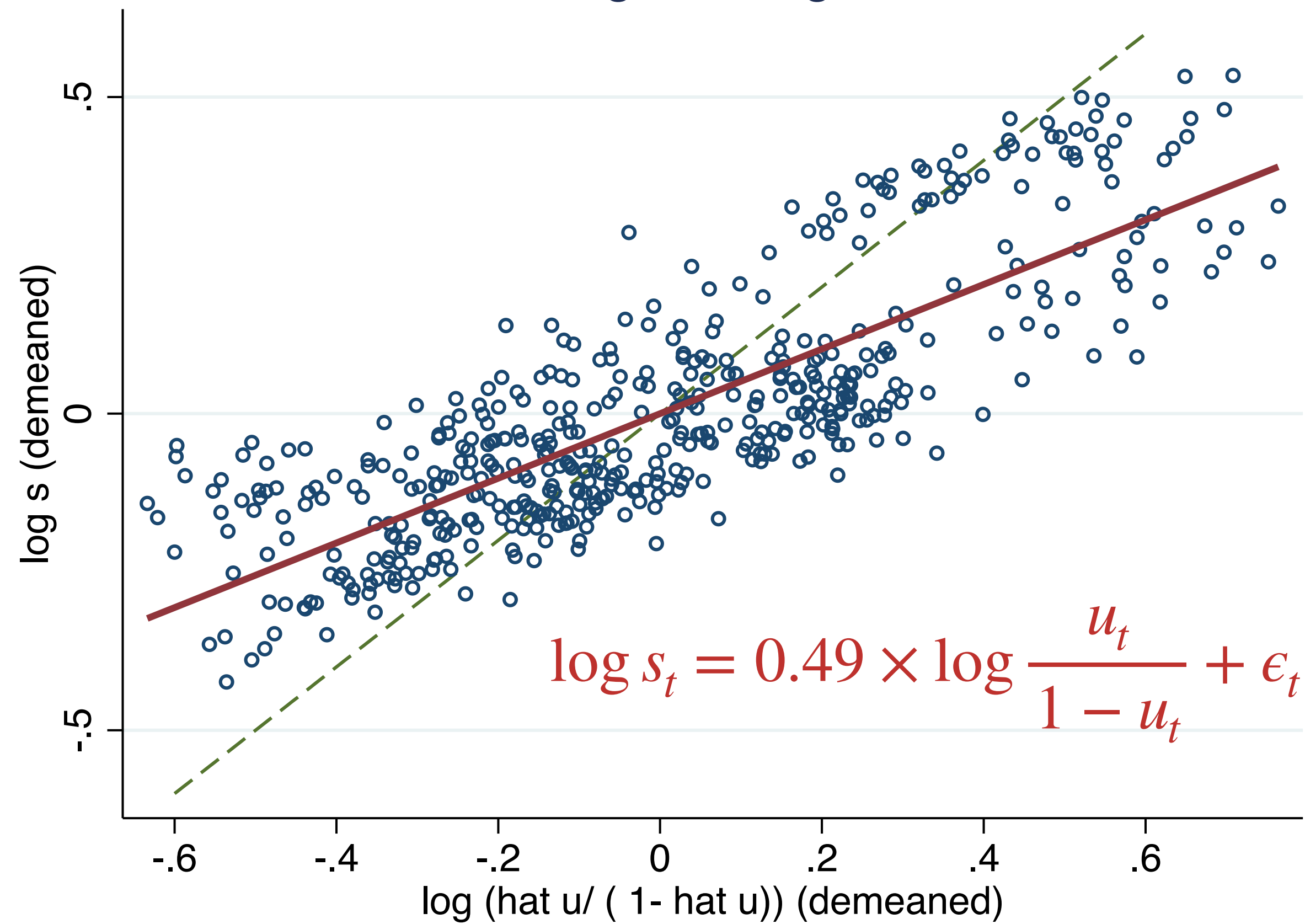
- Consider the following OLS regression

$$\log s_t = \alpha + \beta \log(\hat{u}_t/(1 - \hat{u}_t)) + \epsilon_t$$

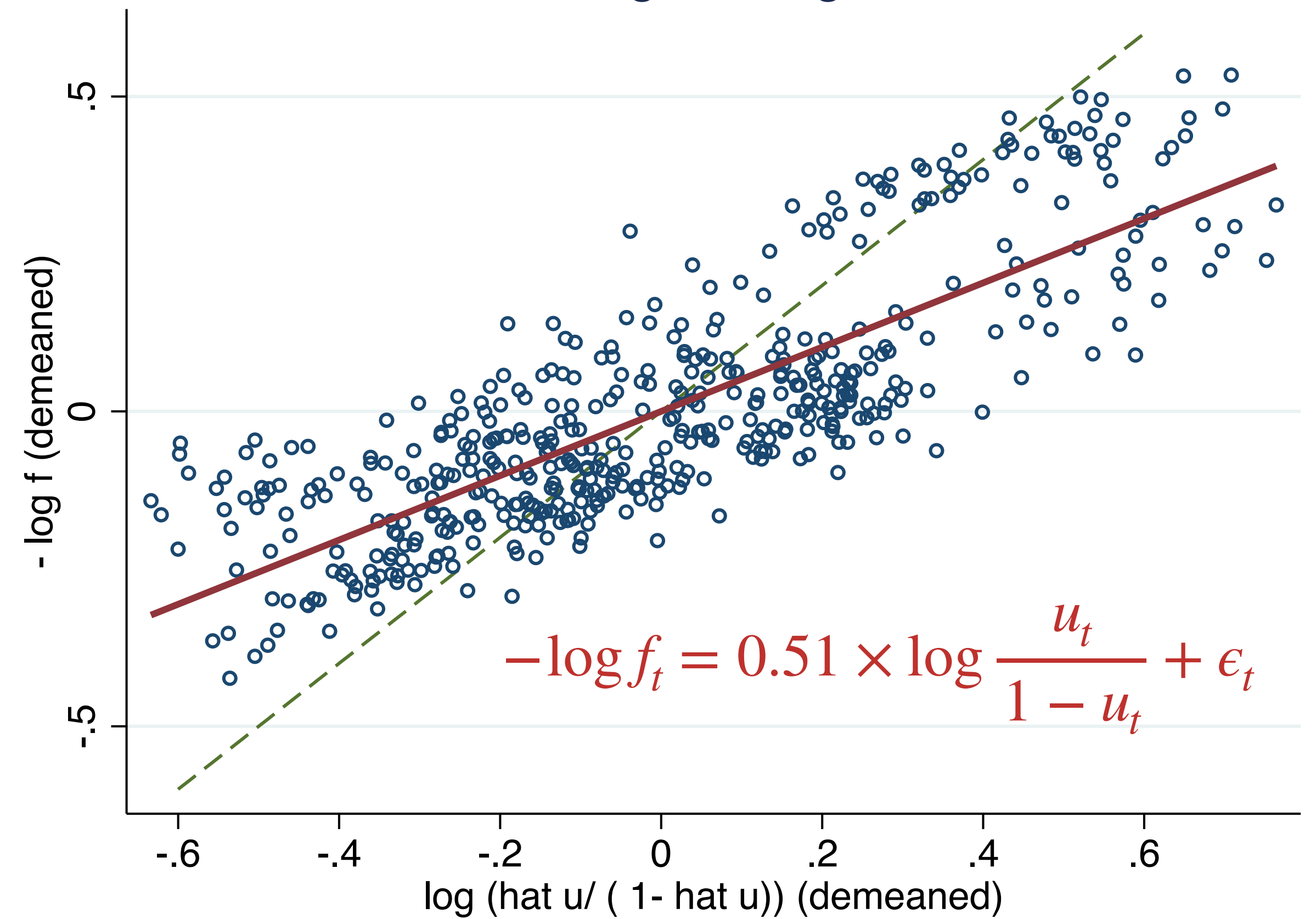
$$\text{Then } \beta = \frac{\text{Cov}(\log s_t, \log \hat{u}_t/(1 - \hat{u}_t))}{\text{Var}(\log \hat{u}_t/(1 - \hat{u}_t))} \Rightarrow \text{Variance share!}$$

# Variance Decomposition through Regression

log s vs log u



- log f vs log u



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# Variance Decomposition

- Decomposition:
  - Job-finding: 51%
  - Job-separation: 49%
- This is in line with Fujita-Ramey (2009)
- In contrast, using different data/methodology, Shimer (2012) argued
  - Job-finding: 90%
  - Job-separation: 10%
- Consensus nowadays is 50:50
  - Literature has been mostly focusing on job-finding due to hysteresis from Shimer

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# Unpacking Job-finding Rate



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# Matching Friction

- Why can't workers find a job immediately? Why does job-finding rate fluctuate?
- Dominant views until 1970s:
  - wage rigidity  $\Rightarrow$  labor supply  $>$  labor demand
- Diamond-Mortensen-Pissarides (DMP) paradigm:
  - Workers look for a job. Firms look for workers.
  - But it takes time to find a match
- Assume that the number of matches in each period is given by
$$m_t = M(u_t, v_t)$$
  - $M$ : matching function,  $u_t$ : unemployment,  $v_t$ : vacancies
  - $M$  is nonnegative, increasing, and concave in both arguments
  - Reduced form way to capture various frictions (e.g., physical and informational)

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# Deriving Beveridge Curve

- It is convenient to assume  $M$  is constant returns to scale (e.g.,  $M(u, v) = \bar{m}u^{1-\alpha}v^\alpha$ )
  - Not empirically settled. Interesting area to explore.

- The job-finding probability can be written as

$$f_t = \frac{M(u_t, v_t)}{u_t} = M(1, v_t/u_t) \equiv \hat{f}(\theta_t)$$

- $\theta_t \equiv v_t/u_t$  is labor market tightness
- Plug the above expression into the approx. unemp. rate formula ( $s_t = f_t u_t / (1 - u_t)$ ):

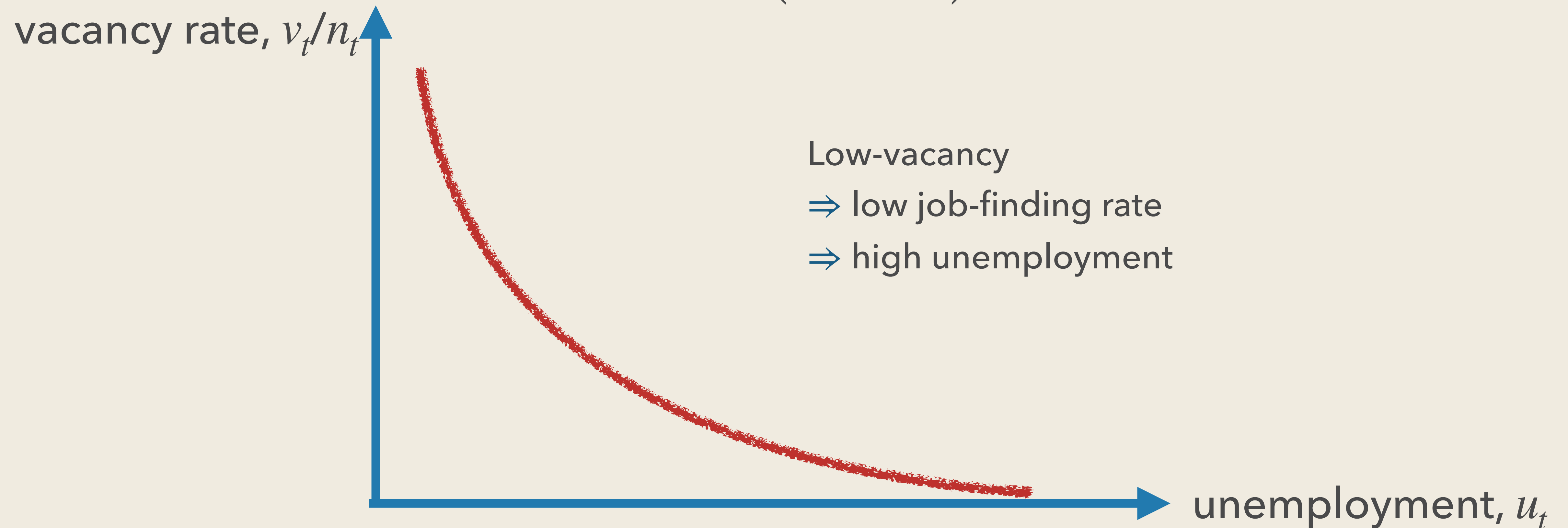
$$s_t = M\left(\frac{v_t}{n_t}, \frac{u_t}{1 - u_t}\right), \quad n_t \equiv 1 - u_t$$

- A relationship between vacancy rate,  $v_t/n_t$ , and unemp. rate,  $u_t$  (for given  $s_t$ )
- Popularly referred to as "**Beveridge curve**"

# Beveridge Curve

- Assuming  $s$  is a constant

$$s = M \left( \frac{v_t}{n_t}, \frac{u_t}{1 - u_t} \right)$$



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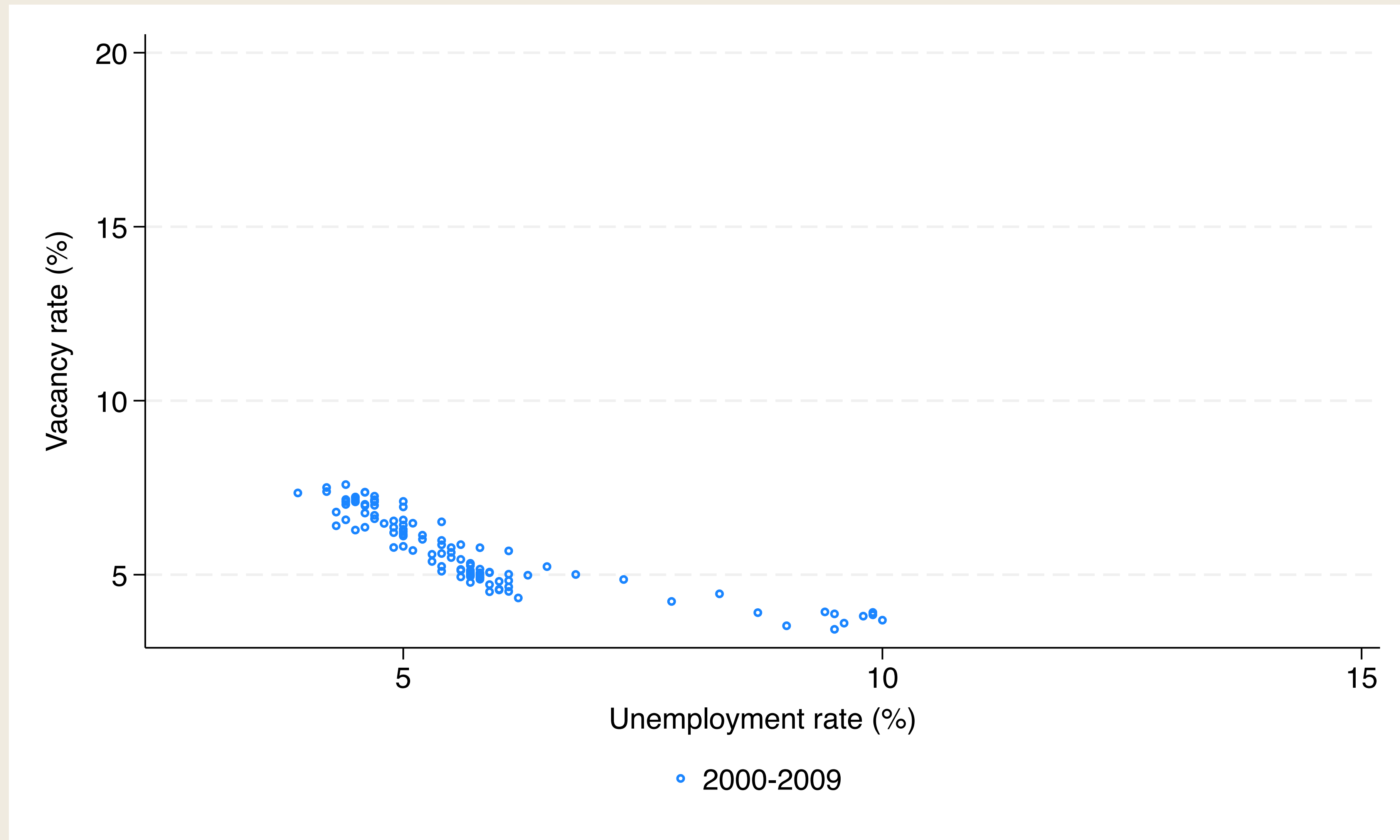
# What is Vacancy?

- How does Beveridge curve look in the data?
  - Before that, what is “vacancy” in the data?
- BLS Job Openings and Labor Turnover Survey (JOLTS) definition:
  1. A specific position exists and there is work available for that position
  2. The job could start within 30 days
  3. There is **active recruiting** for workers from outside the establishment location

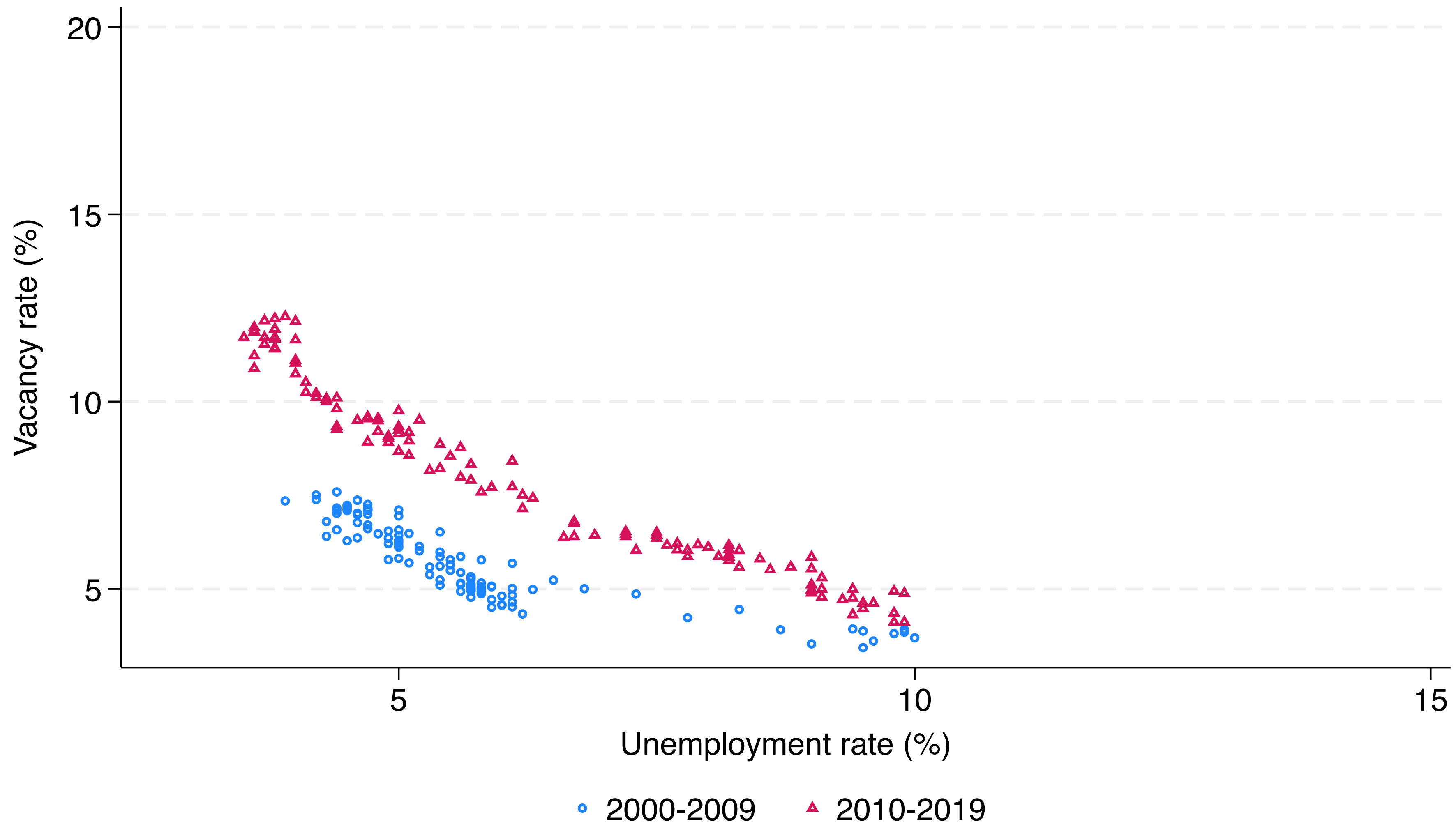
# Vacancy in the Data



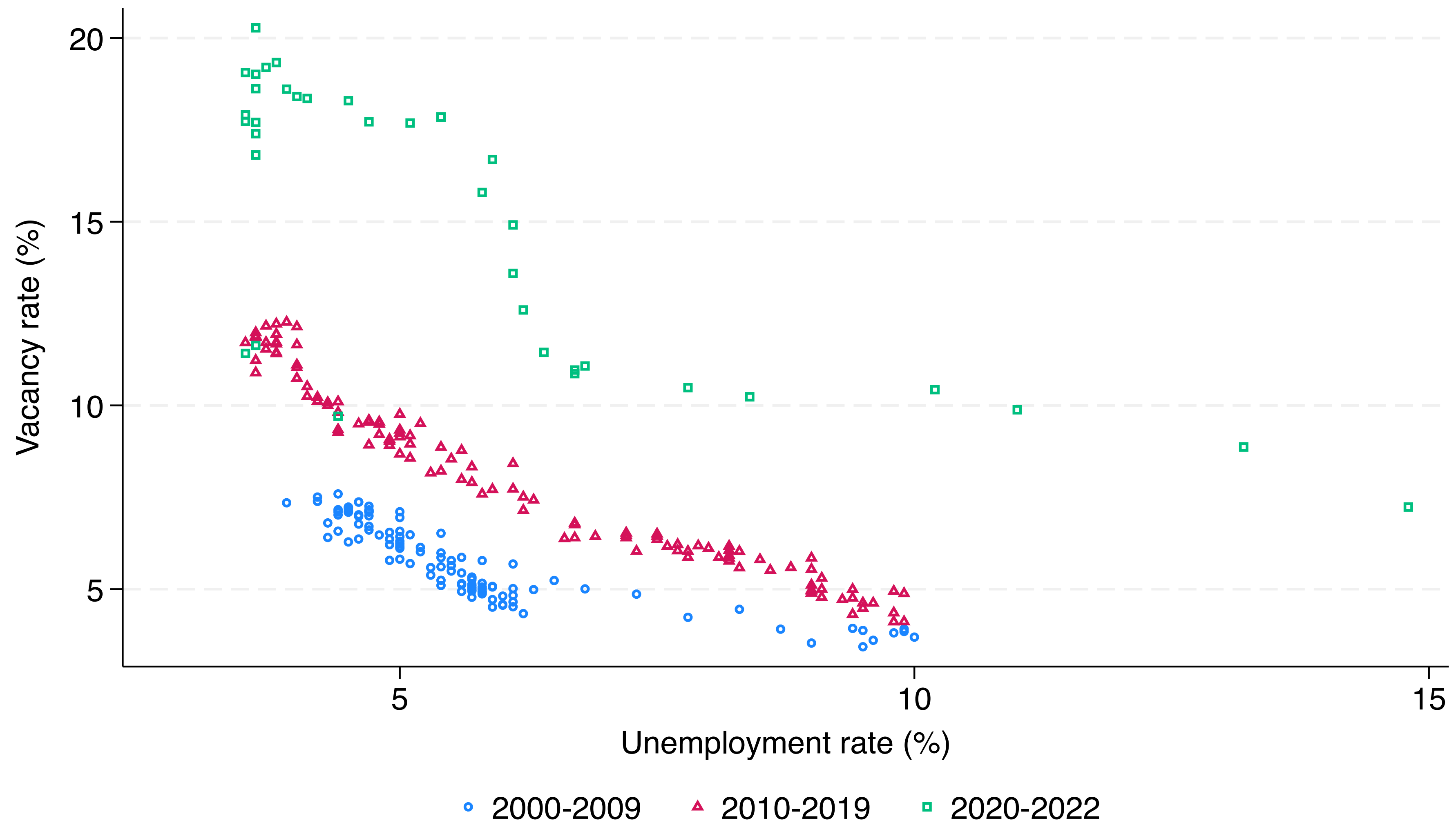
# Empirical Beveridge Curve



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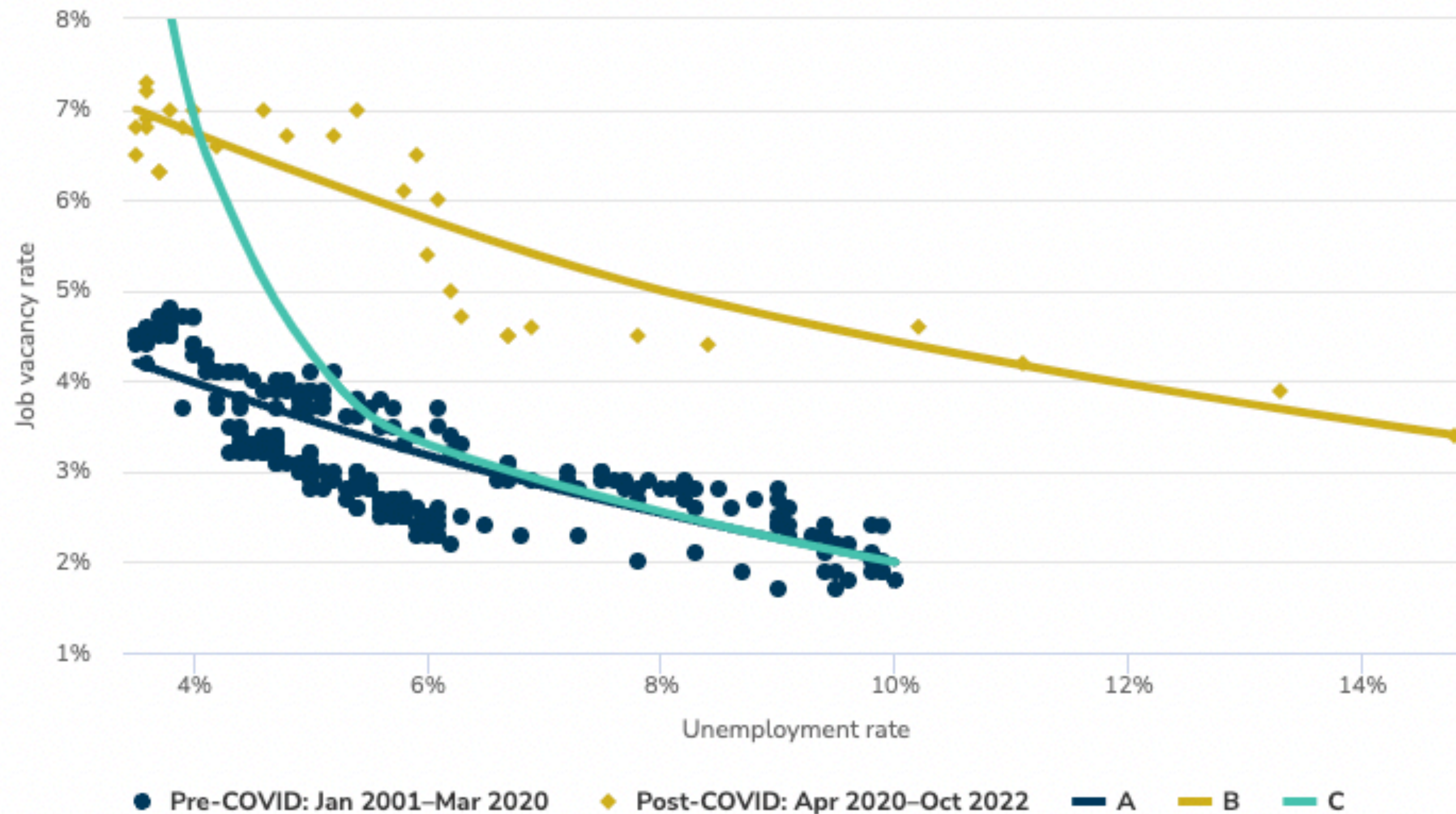
# Empirical Beveridge Curve





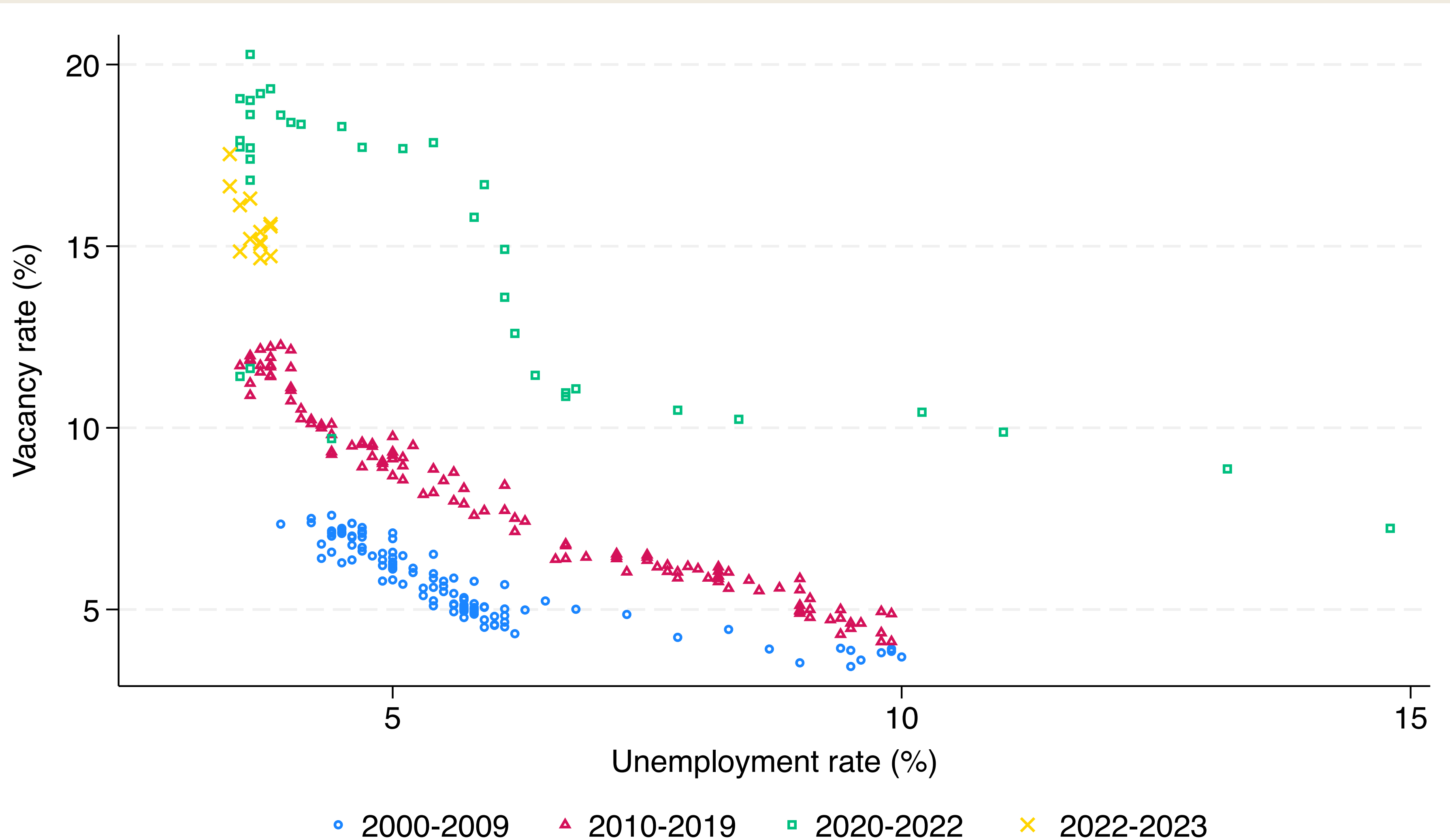
# Soft-Landing or Hard-Landing?

Which Beveridge curve are we on?



- **Blanchard & Summers:**  
We are on B. If the Fed brings down  $v$  to pre-COVID level, we will see a massive increase in  $u$ .  
⇒ hard-landing
- **Mongey:**  
We are on C. Reducing  $v$  doesn't increase  $u$  much.  
⇒ soft-landing

# Who was Right?



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# What Can Beveridge Curve Tell?

- As predicted by DMP paradigm, there appears to be a negative correlation ... with ongoing outward shifts in the relationship
  - For any given  $u_t$ , we have more vacancies now than before
- Suppose the matching function is time-varying and now given by

$$M_t(v_t, u_t) = \bar{m}_t(v_t)^\alpha (u_t)^{1-\alpha}$$

$\bar{m}_t$ : match efficiency shock

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# Beveridge Curve

- Taking log, the Beveridge curve (expressed in logs) is now

$$\log(v_t/n_t) = \tilde{m}_t - \frac{1-\alpha}{\alpha} \log \frac{u_t}{1-u_t}$$

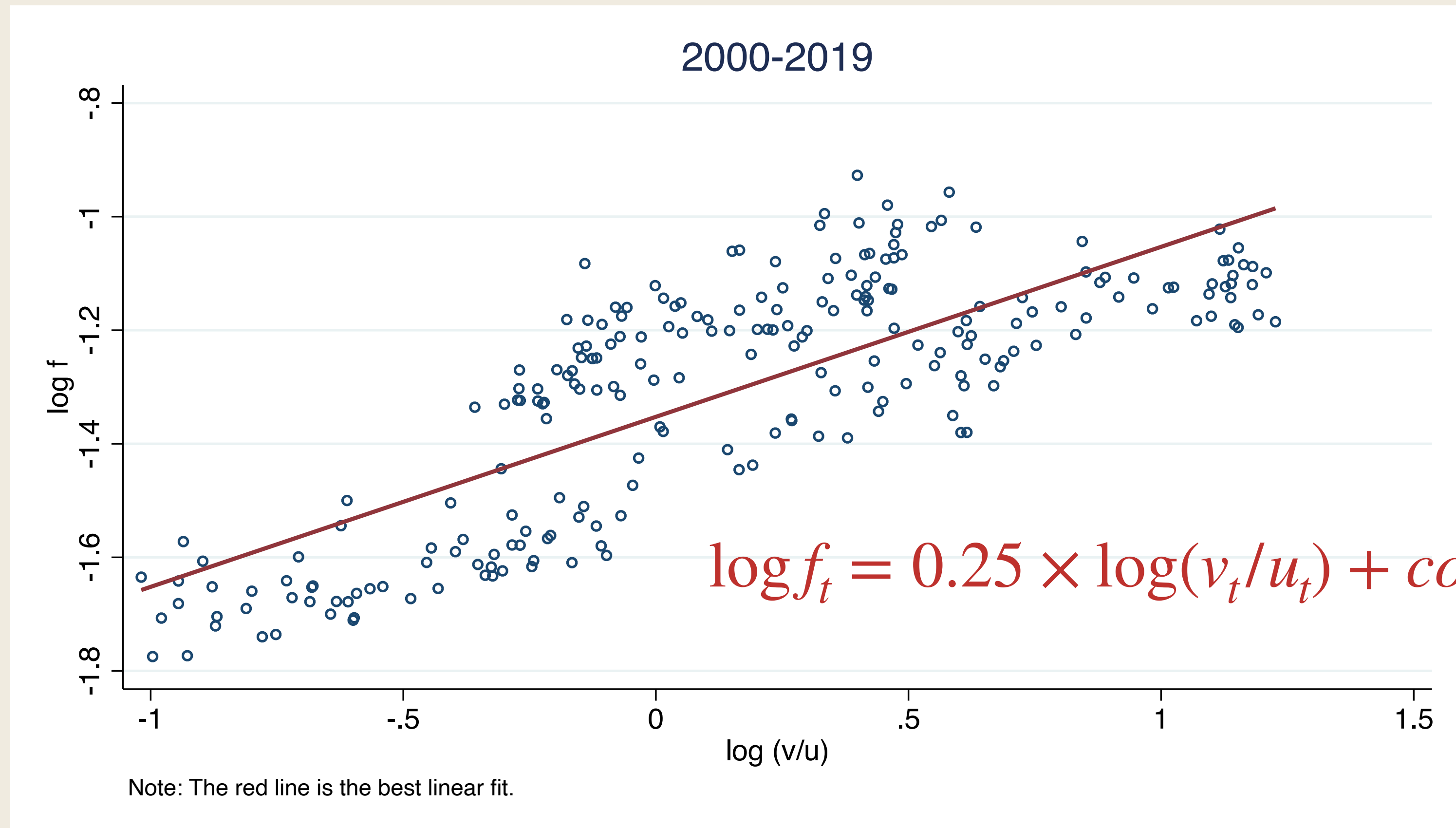
where  $\tilde{m}_t \equiv (1/\alpha) [\log s_t - \log \bar{m}_t]$

- Any shock to  $s_t$  or  $\bar{m}_t$  will show up as the shifts in the empirical Beveridge curve
- If  $\tilde{m}_t$  is correlated with  $u_t$ , the empirical Beveridge curve lacks structural interpretation
  - Just as in  $\text{corr}(q, p)$  tells us neither supply nor demand curve
  - In my view, this is an important open question
- Still,  $\text{corr}(v, u) < 0$  is suggestive that  $v$  is an important determinant of  $u$

# Job-Finding and Market Tightness

- Another way to see the prediction of DMP paradigm is (under Cobb-Douglas)

$$\log f_t = \log \hat{f}(\theta_t) = \log \bar{m} + (1 - \alpha) \log(v_t/u_t)$$



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# Taking Stock

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# Taking Stock

- Unemployment rate fluctuates between 5-10p.p.
- On average, 30% of workers find a job every month; 2% of workers loose their job
- Job-finding and separation play roughly equally important role in fluctuations in  $u$
- DMP paradigm views unemployment as the outcome of matching frictions
- Next lecture: understand the determinants of  $v_t$

# Appendix: Cross-Country Perspective

