
Supply-Side View of Financial Frictions:

Borrowing Constraints and Misallocation

704 Macroeconomics II
Topic 6

Masao Fukui

Do Financial Frictions Matter in the Short-Run?

How the Great Depression Started

Complete and Closing N. Y. Stock Exchange Prices On Pages 37-40

Complete Wire Reports of UNITED PRESS, the Greatest World-Wide News Service



The Pittsburgh Press

STOCKS EXTRA
Complete Markets

FORTY-EIGHT PAGES WEATHER—RAIN. PITTSBURGH, PA., TUESDAY, OCTOBER 29, 1929 IN TWO SECTIONS—SECTION ONE THREE CENTS

HUGE LOSSES IN WALL STREET; SALES SET ALL-TIME RECORD

200 Escape Seventh Ave. Hotel Fire

RACING TODAY'S RESULTS

BIG DECLINE SLOWED UP BY LATE RALLY

Playful Monk Makes Good Escape From Fraternity Boys.

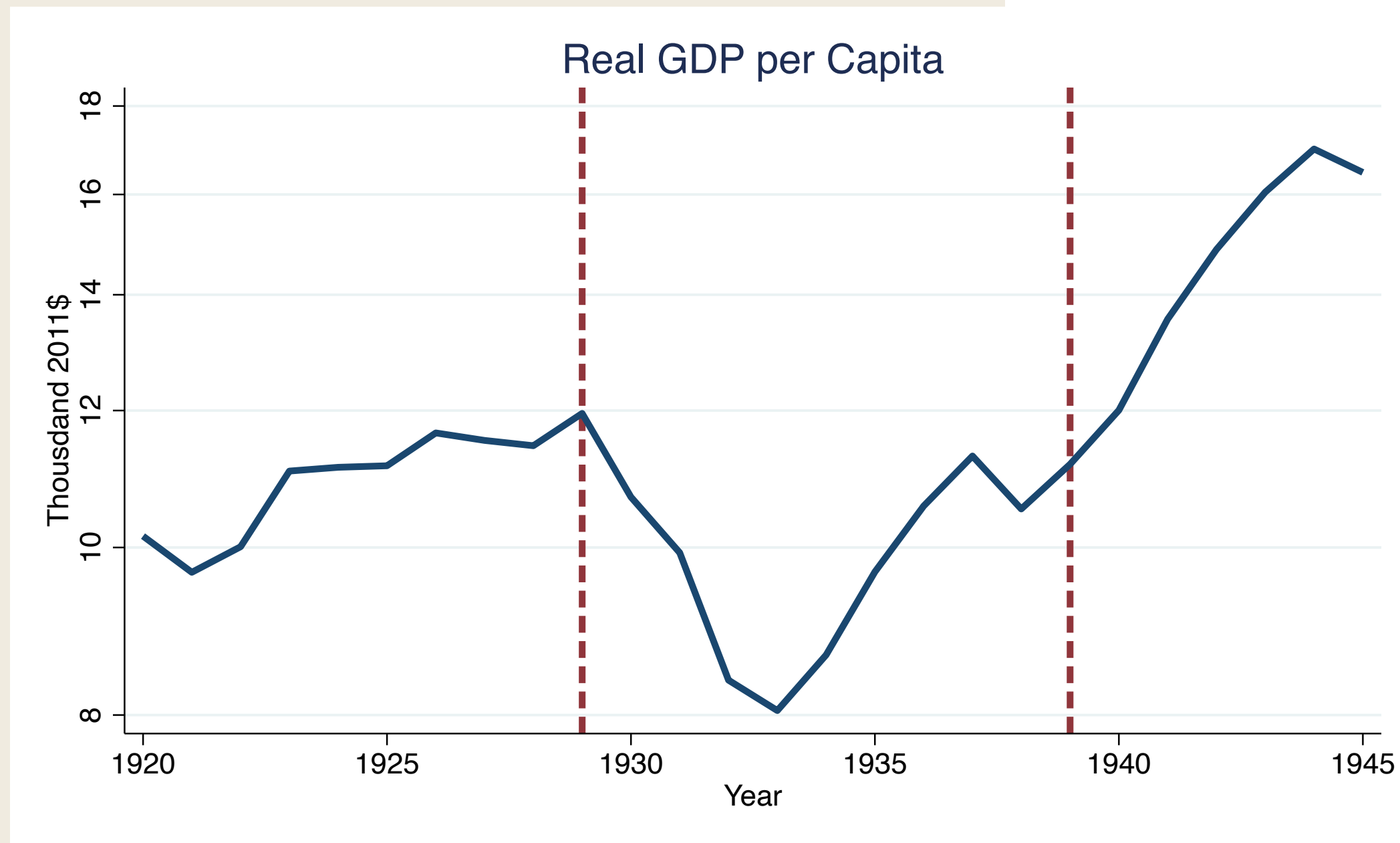
RESCUE GUEST FROM SMOKE

BLAZE IN HOTEL

UNDERGROUND TRAFFIC PLAN

First race, \$1,500 purse, 2-year-olds, 4-mile			
Moyn. 110, Inzelone	22.50	9.70	3.90
Sam Falso, 110, Cotticelli	8.20		2.90
Monter, 110, Leishman			2.50
Time—1:12 4-5. Also ran—Handeman, Kings Crer, Guthrie, House Knight, Timon, Black Cloud.			
Second race, \$1,300, claimant, 3-year-olds, 1 mile			
Donna Tina, 105, Serio	5.20	3.70	3.30
Loumora, 113, Abel		14.50	4.20
Lion Hearty, 110, F. Maus			4.20

Great Depression



How the Great Recession Started

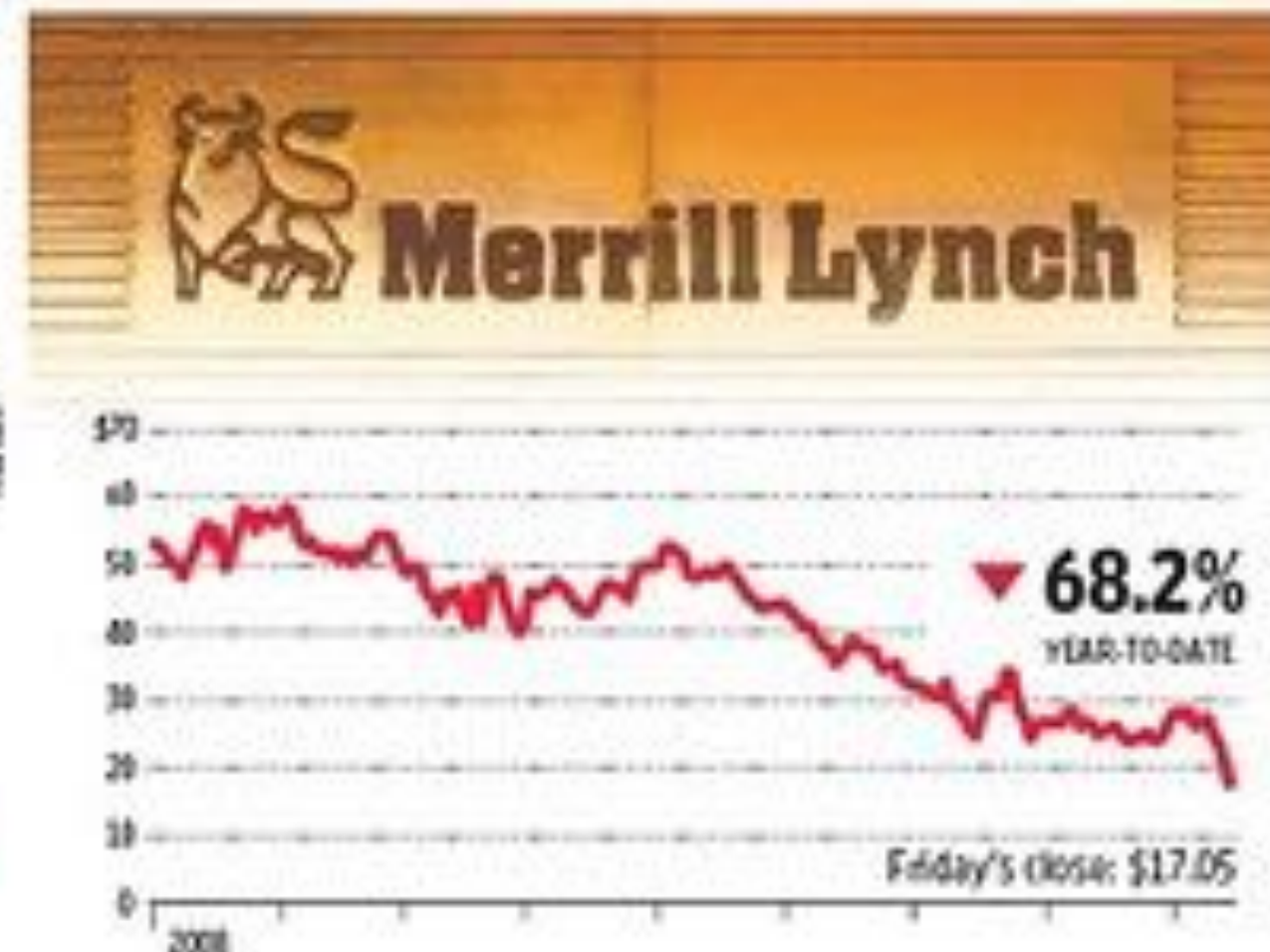
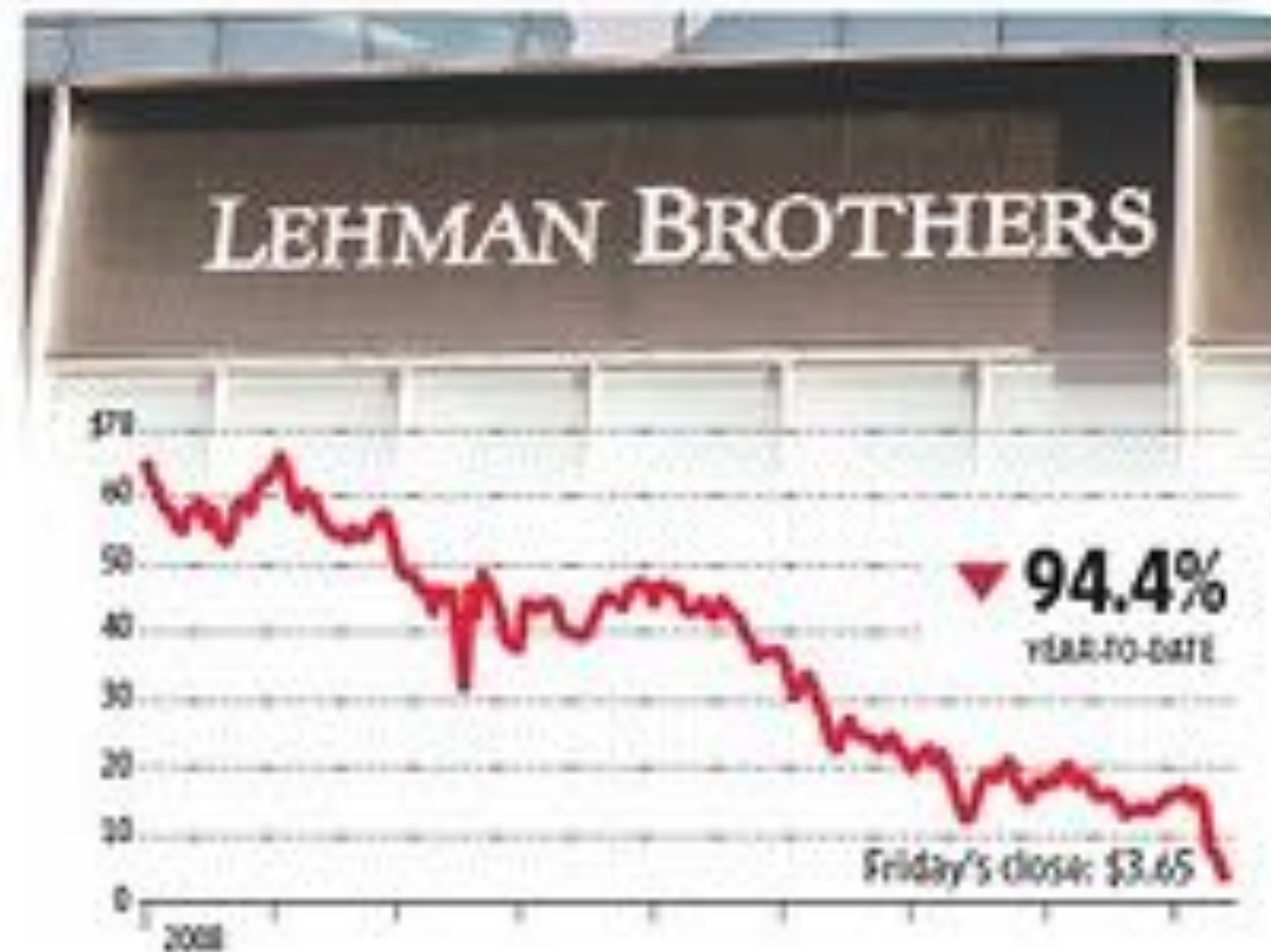
THE WALL STREET JOURNAL.

DOW JONES
A DOW JONES CORPORATION COMPANY

MONDAY, SEPTEMBER 15, 2008 • VOL. CCLII NO. 64

★★★★ \$2.00

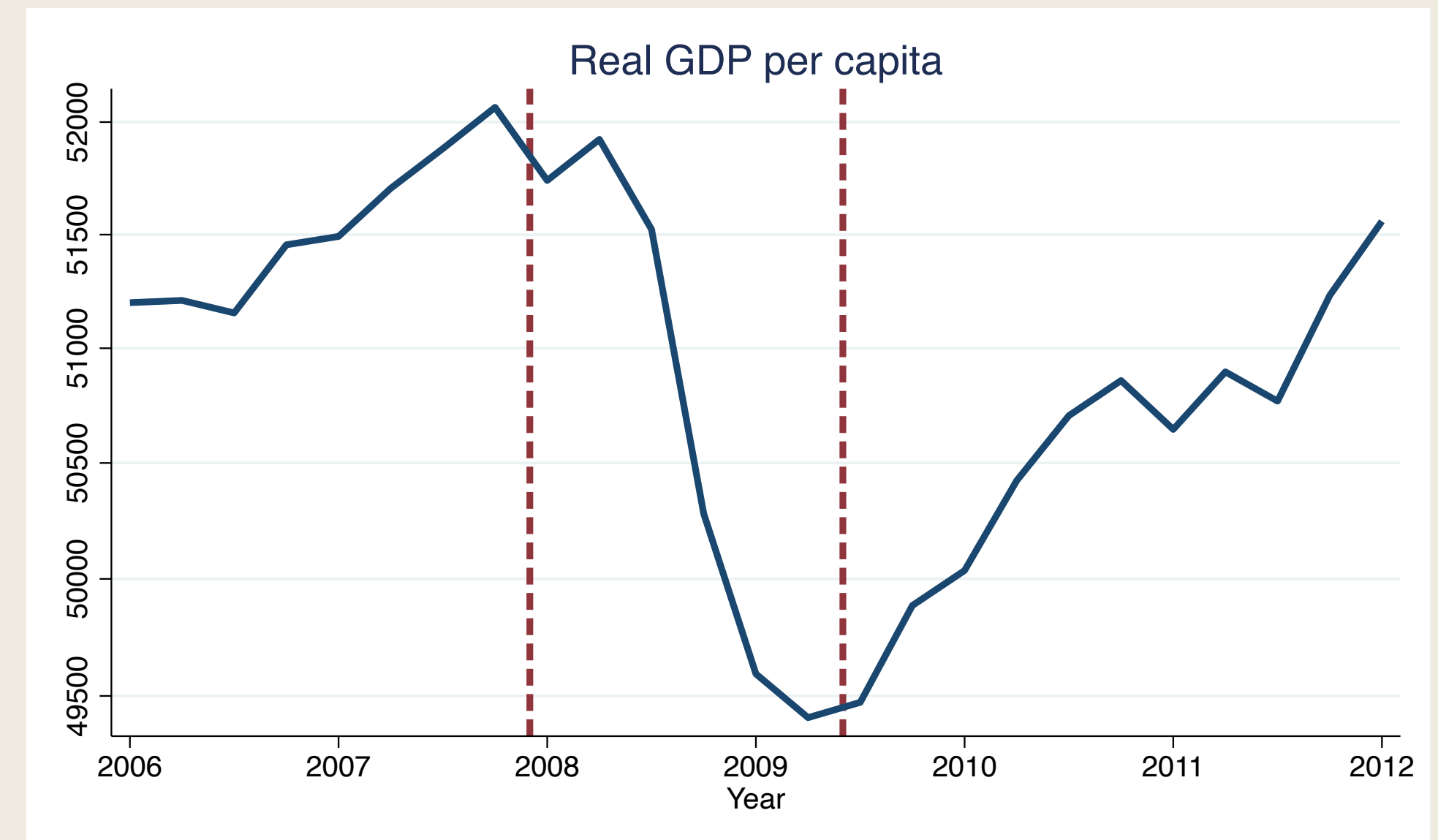
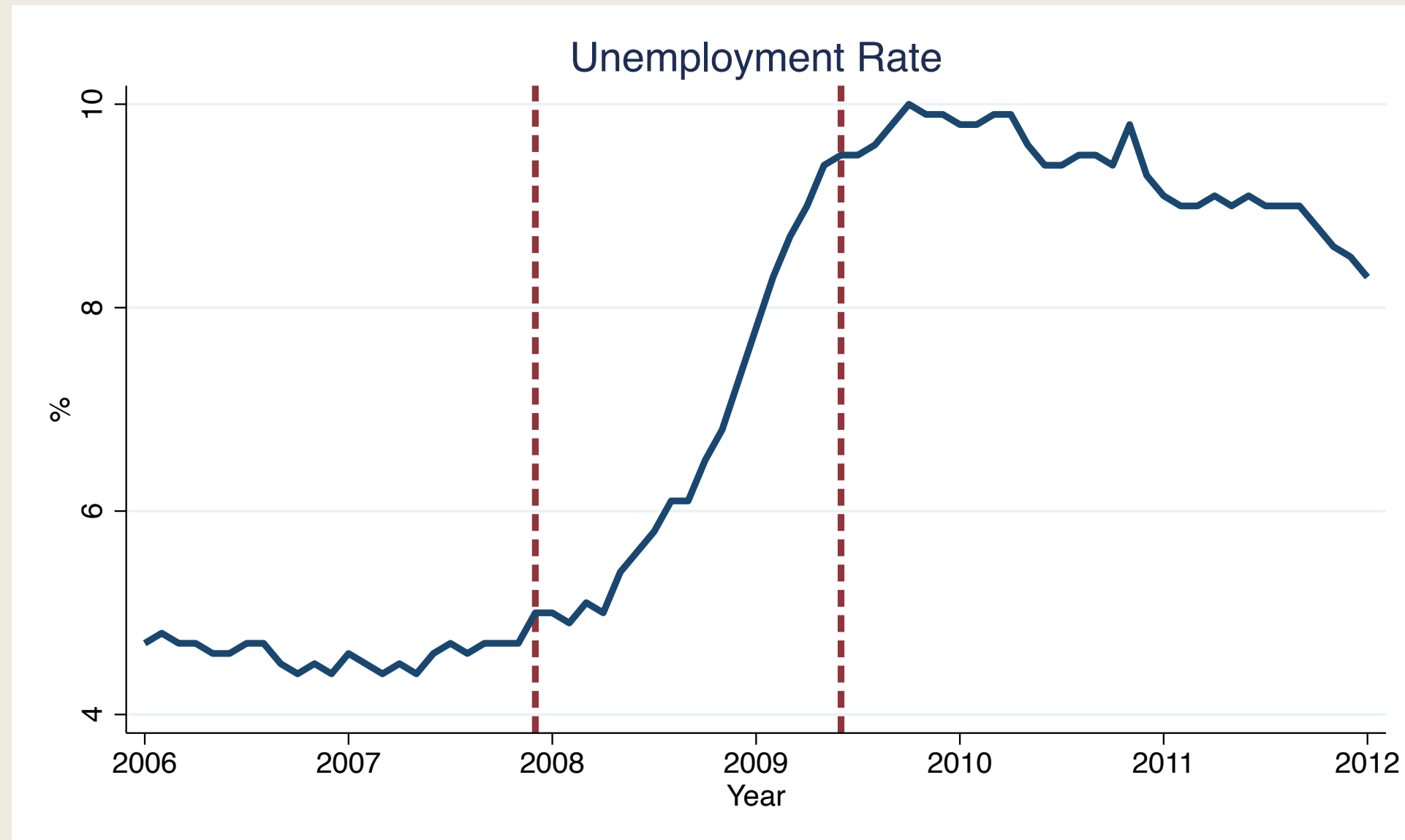
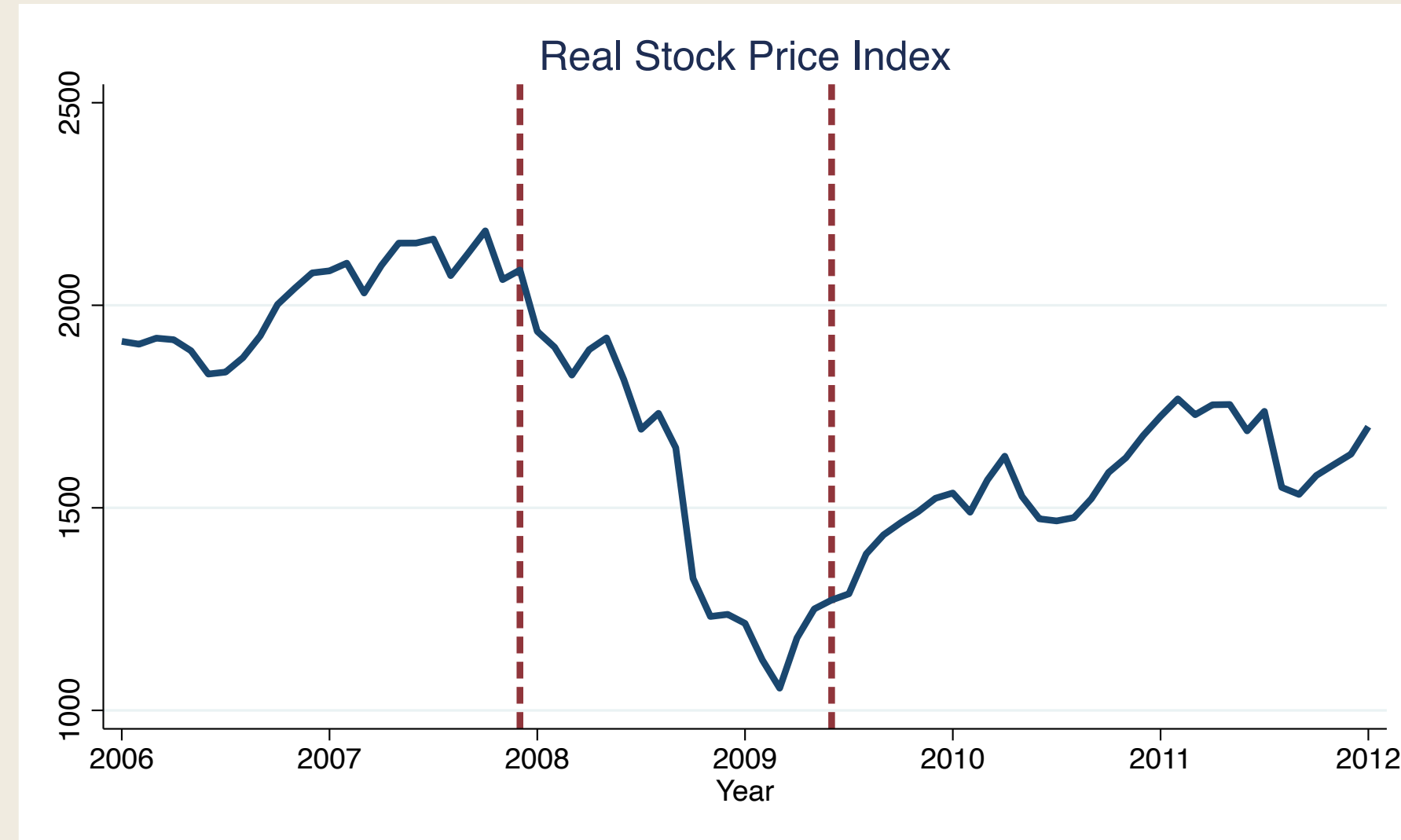
Last week: DJIA 11421.99 ▲201.03 1.8% NASDAQ 2261.27 ▲0.2% NIKKEI 12214.76 unch. DJ STOXX 50 2858.68 ▲3.8% 10-YR TREASURY ▼20/32, yield 3.730% OIL \$101.18 ▼\$5.05 EURO \$1.4217 YEN 107.87



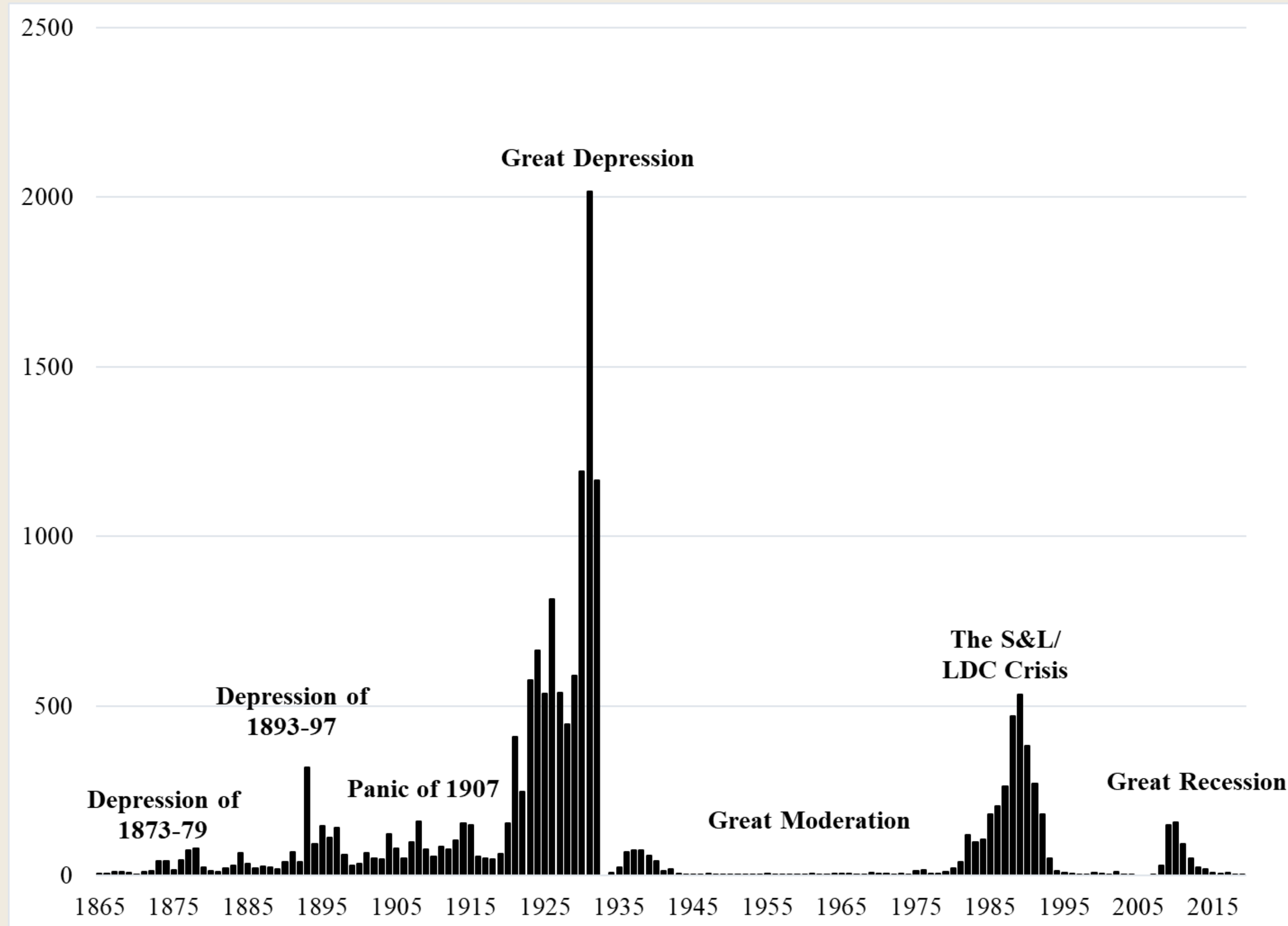
Crisis on Wall Street as Lehman Totters, Merrill Is Sold, AIG Seeks to Raise Cash

Fed Will Expand Its Lending Arsenal in a Bid to Calm Markets; Moves Cap a Momentous Weekend for American Finance

Great Recession



Number of Bank Failures



Cause or Consequence?

- Two views on bank failures:
 1. Bank failures are a **consequence** of the Great Depression/Great Recession
 2. Bank failures are the **cause** of the Great Depression/Great Recession
- The first view was dominant after the Great Depression
- In his 1983 paper, Bernanke brought a new perspective and argued for 2

Bernanke (1983)

$$\Delta Y_t = \alpha + \beta \times \Delta(\text{Bank Health})_t + \gamma' \mathbf{X}_t + \epsilon_t$$

$$(3) \quad Y_t = \begin{matrix} .613 & Y_{t-1} & - & .159 & Y_{t-2} & + & .332 & (M - M^e)_t & + & .113 & (M - M^e)_{t-1} & + & .110 & (M - M^e)_{t-2} \\ (9.86) & & & (-2.63) & & & (2.92) & & & (0.99) & & & (0.96) & \end{matrix}$$

$$+ \begin{matrix} .156 & (M - M^e)_{t-3} & - & .869E-04 & DBANKS_t & - & .406E-04 & DBANKS_{t-1} \\ (1.38) & & & (-4.24) & & & (-1.93) & \end{matrix}$$

$$- \begin{matrix} .258E-03 & DFAILS_t & - & .325E-03 & DFAILS_{t-1} \\ (-1.95) & & & (-2.47) & \end{matrix}$$

s.e. = .0249 *D.W.* = 1.99 Sample: 1/21-12/41

$$(4) \quad Y_t = \begin{matrix} .615 & Y_{t-1} & - & .131 & Y_{t-2} & + & .455 & (P - P^e)_t & + & .231 & (P - P^e)_{t-1} & - & .004 & (P - P^e)_{t-2} \\ (9.76) & & & (-2.13) & & & (3.99) & & & (1.97) & & & (-0.03) & \end{matrix}$$

$$+ \begin{matrix} .024 & (P - P^e)_{t-3} & - & .799E-04 & DBANKS_t & - & .337E-04 & DBANKS_{t-1} \\ (0.22) & & & (-4.03) & & & (-1.66) & \end{matrix}$$

$$- \begin{matrix} .202E-03 & DFAILS_t & - & .242E-03 & DFAILS_{t-1} \\ (-1.52) & & & (-1.83) & \end{matrix}$$

s.e. = .0246 *D.W.* = 1.98 Sample: 1/21-2/41

Notes: Y_t = rate of growth of industrial production (*Federal Reserve Bulletin*), relative to exponential trend.
 $(M - M^e)_t$ = rate of growth of M1, nominal and seasonally adjusted (Friedman and Schwartz, Table 4-1), less predicted rate of growth.
 $(P - P^e)_t$ = rate of growth of wholesale price index (*Federal Reserve Bulletin*), less predicted rate of growth.
 $DBANKS_t$ = first difference of deposits of failing banks (deflated by wholesale price index).
 $DFAILS_t$ = first difference of liabilities of failing businesses (deflated by wholesale price index).
 Data are monthly; *t*-statistics are shown in parentheses.

(More) Credible Identification

1. **Chodorow-Reich (2014)**: Firm-level cross-sectional regression:

$$\Delta Y_i = \beta \times \Delta(\text{Bank Health})_i + \gamma' \mathbf{X}_i + \epsilon_i$$

- $(\text{Bank Health})_i$: health of banks that the firm i had a relationship with
- Using data from the US 2007-2009, find $\beta > 0$

2. **Huber (2018)**: County-level cross-sectional regression:

$$\Delta Y_c = \beta \times \Delta(\text{Bank Health})_c + \gamma' \mathbf{X}_c + \epsilon_c$$

- $(\text{Bank Health})_c$: average health of banks in county c
- Using data from the Germany 2007-2012, find $\beta > 0$

The Role of Cross-Sectional Identification

A common critique of estimates based on cross-sectional identification in macroeconomics is that they don't answer the right question. While it is true that these estimates don't directly provide estimates of aggregate responses, they often provide a great deal of indirect evidence by helping researchers discriminate between different theoretical views of how the world works.... This “piecemeal” form of inference will, therefore, result in partial identification on the model space.

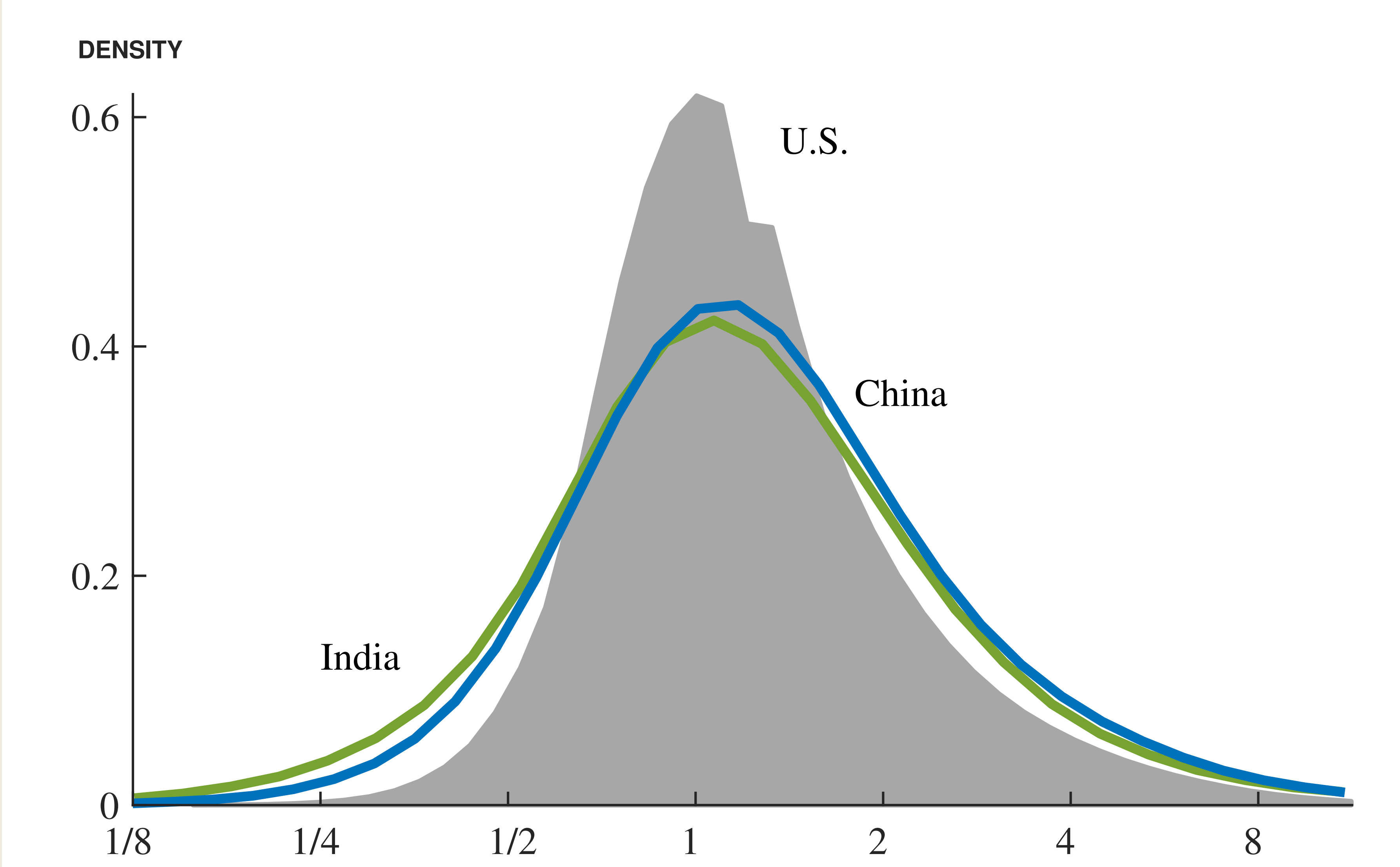
— Nakamura and Steinsson (2018) “Identification in Macroeconomics”

Do Financial Frictions Matter in the Long-Run?

Misallocation Hypothesis

- Large cross-country TFP differences. Why?
- Hsieh & Klenow (2007): misallocation
 - Measure marginal product of capital at the firm level:
$$MPK_i = f'_i(k)$$
 - Efficiency requires $MPK_i = \overline{MPK}$ for all i
 - If $f_i(k) = A_i k^\alpha$, then $MPK_i = \alpha y_i / k_i \Rightarrow$ can measure MPK_i from microdata
- Implement in the context of manufacturing in the US, India, and China

MPK Dispersion



Financial Friction

- Why are MPK not equalized?
- A potentially important source is financial friction
- Firms cannot borrow as much as they want
 - Financially constrained firms have higher MPK
 - Unconstrained firms have lower MPK

Financial Frictions and Misallocation

–Based on Moll (2015)

Entrepreneurs

- The economy is populated by a unit mass of entrepreneurs indexed by $i \in [0,1]$

- Preferences:

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \ln c_t^i$$

- The technology of an entrepreneur with productivity z_t^i is:

$$y_t^i = z_t^i k_t^i$$

- Assume no depreciation of capital k_t^i

- Productivity z_t evolves according to a Markov process

- Let $f(z' | z)$ denote the probability density of z' conditional on z
- Assume $z_t \in [0, \bar{z}]$ (bounded)

Borrowing Constraint

■ Budget constraint:

$$c_t^i + a_{t+1}^i = z_t^i k_t^i - r_t k_t^i + (1 + r_t) a_t^i$$

- a_t^i : networth, k_t^i : capital, r_t : rental price of capital

■ Borrowing constraint:

$$k_t^i \leq \lambda a_t^i$$

- Can only rent capital up to $\lambda \geq 1$ times networth

■ Microfoundation:

- borrowers can steal $1/\lambda$ fraction of the rented capital k^i
- if borrowers steal, lenders can seize the networth of borrowers a^i
- In equilibrium, lenders are willing to lend

$$(1/\lambda)k^i \leq a^i \iff k^i \leq \lambda a^i$$

Equilibrium Definition

- Given $\{r_t\}_{t=0}^{\infty}$, entrepreneurs choose $\{c_t^i, a_{t+1}^i, k_t^i\}_{t=0}^{\infty}$ to maximize utility
- Markets clear

$$\int_0^1 a_t^i di = \int_0^1 k_t^i di$$

No Financial Friction

No Financial Friction

- Suppose there is no financial friction $\lambda = \infty$
- Entrepreneur's problem in a recursive form:

$$V_t(a_t, z_t) = \max_{k_t \geq 0, c_t, a_{t+1}} \ln c_t + \beta \mathbb{E}_t V_{t+1}(a_{t+1}, z_{t+1})$$

s.t. $c_t + a_{t+1} = z_t k_t - r_t k_t + (1 + r_t) a_t$

- Consider a sub-problem where entrepreneurs choose k_t to solve

$$\max_{k_t \geq 0} z_t k_t - r_t k_t$$

Solutions:

$$k_t = \begin{cases} \infty & \text{if } z_t > r_t \\ \tilde{k} \in [0, \infty] & \text{if } z_t = r_t \\ 0 & \text{if } z_t < r_t \end{cases}$$

Equilibrium Interest Rate

- In the absence of borrowing constraints,

$$r_t = \bar{z}$$

- If $r_t > \bar{z}$, everyone will lend
- If $r_t < \bar{z}$, entrepreneurs with $z \in (r_t, \bar{z}]$ will infinitely borrow

- As a result, all agents solve:

$$V(a_t) = \max_{c_t, a_{t+1}} \ln c_t + \beta V(a_{t+1})$$

$$\text{s.t. } c_t + a_{t+1} = \underbrace{\max_{k_t \geq 0} \{z_t k_t - r_t k_t\} + (1 + r_t) a_t}_{(1 + \bar{z}) a_t}$$

- Guess and verify:

$$c_t(a_t) = (1 - \beta)(1 + \bar{z})a_t, \quad a_{t+1}(a_t) = \beta(1 + \bar{z})a_t$$

No Financial Friction: Aggregation

- The economy follows

$$Y_t = \bar{z}K_t$$

$$K_{t+1} = \beta(1 + \bar{z})K_t$$

- Exogenous TFP. This is a standard AK economy

Financial Friction

Frictional Financial Market

- Now consider financial friction $\lambda < \infty$

$$\max_{k_t \in [0, \lambda a_t]} z_t k_t - r_t k_t$$

Solutions:

$$k_t(a_t, z_t) = \begin{cases} \lambda a_t & \text{if } z_t > r_t \\ \tilde{k} \in [0, \lambda a_t] & \text{if } z_t = r_t \\ 0 & \text{if } z_t < r_t \end{cases}$$

- The budget constraint of entrepreneur with productivity z_t is

$$c_t + a_{t+1} = (1 + \pi_t(z_t))a_t$$

where

$$\pi(z; r_t) \equiv \begin{cases} (z - r_t)\lambda + r_t & \text{for } z \geq r_t \\ r_t & \text{for } z < r_t \end{cases}$$

- Entrepreneurs with $z > r_t$ earn (finite) excess returns

Bellman Equation

$$V_t(a_t, z_t) = \max_{c_t, a_{t+1}} \ln c_t + \beta \mathbb{E}_t V_{t+1}(a_{t+1}, z_{t+1})$$
$$\text{s.t. } c_t + a_{t+1} = (1 + \pi(z_t; r_t))a_t$$

- Expectation is taken over z_{t+1}
- Guess and verify:

$$c_t(a_t, z_t) = (1 - \beta)(1 + \pi(z, r_t))a_t, \quad a_{t+1}(a_t, z_t) = \beta(1 + \pi(z; r_t))a_t$$

Aggregation

- Let $g_t(a, z)$ denote the density of the joint distribution of (a, z)

- The capital market clearing implies

$$\int_{\underline{z}}^{\bar{z}} \int_0^{\infty} a g_t(a, z) da dz = \int_{r_t}^{\bar{z}} \int_0^{\infty} \lambda a g_t(a, z) da dz = K_t \quad (1)$$

- Define wealth share held by entrepreneurs with productivity z as

$$\omega_t(z) = \frac{1}{K_t} \int_0^{\infty} a g_t(a, z) da \quad (2)$$

Note $\int_{\underline{z}}^{\bar{z}} \omega_t(z) dz = 1$

- Using (2) to rewrite (1) as

$$\lambda \int_{r_t}^{\bar{z}} \omega_t(z) dz = 1$$

- Given $\{\omega_t(z)\}_{z'}$, this pins r_t with lower $\lambda \Rightarrow$ lower r_t
- Financial friction depresses interest rate

Aggregate Output

- The aggregate output is

$$\begin{aligned} Y_t &= \int_{r_t}^{\bar{z}} \int_0^{\infty} z \lambda a_t g_t(a, z) da dz \\ &= \lambda \int_{r_t}^{\bar{z}} z \omega_t(z) dz K_t \\ &= \frac{1}{\int_{r_t}^{\bar{z}} \omega_t(z) dz} \int_{r_t}^{\bar{z}} z \omega_t(z) dz K_t \\ &\quad \underbrace{\hspace{10em}}_{\equiv \mathbb{E}_{\omega}[z|z \geq r_t]} \\ &\equiv Z_t K_t \end{aligned}$$

- Total factor productivity Z_t is endogenous to wealth distribution:
 - Wealth weighted average of z conditional on $z \geq r_t$
- Depressed interest rate $r_t \Rightarrow$ low z produce \Rightarrow misallocation

Evolution of Capital Stock

- The evolution of capital stock is

$$\begin{aligned} K_{t+1} &= \int_{\underline{z}}^{\bar{z}} \int_0^{\infty} a_{t+1}(a, z) g_t(a, z) da dz \\ &= K_t \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(z; r_t)) \underbrace{\frac{1}{K_t} \int_0^{\infty} a g_t(a, z) da}_{= \omega_t(z)} dz \\ &= K_t \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(z; r_t)) \omega_t(z) dz \end{aligned}$$

Wealth Shares as Sufficient Statistics

- So far, we have characterized the determination of all the aggregates:
 - r_t
 - Y_t
 - Z_t
 - K_{t+1}.... given K_t and wealth shares $\{\omega_t(z)\}$
- But how do the wealth shares $\{\omega_t(z)\}$ evolve starting from $\{\omega_0(z)\}$?

Evolution of Distribution

- Law of motion for $g_t(a, z)$

$$\Pr(a_{t+1} \leq a, z_{t+1} = z) = \int_{\underline{z}}^{\bar{z}} \int_0^{\infty} g_t(\tilde{a}, \tilde{z}) \mathbb{1}[a_{t+1}(\tilde{a}, \tilde{z}) \leq a] f(z | \tilde{z}) d\tilde{a} d\tilde{z}$$

- Recalling $a_{t+1}(\tilde{a}, \tilde{z}) = \beta(1 + \pi(\tilde{z}; r_t))\tilde{a}$,

$$\Pr(a_{t+1} \leq a, z_{t+1} = z) = \int_{\underline{z}}^{\bar{z}} \int_0^{\frac{a}{\beta(1 + \pi(\tilde{z}; r_t))}} g_t(\tilde{a}, \tilde{z}) f(z | \tilde{z}) d\tilde{a} d\tilde{z}$$

- Since $g_{t+1}(a, z) \equiv \partial_a \Pr(a_{t+1} \leq a, z_{t+1} = z)$

$$g_{t+1}(a, z) = \int_{\underline{z}}^{\bar{z}} \frac{1}{\beta(1 + \pi(\tilde{z}; r_t))} g_t\left(\frac{a}{\beta(1 + \pi(\tilde{z}; r_t))}, \tilde{z}\right) f(z | \tilde{z}) d\tilde{a} d\tilde{z}$$

Evolution of Wealth Share

- Using the previous relationship

$$\begin{aligned}
 \omega_{t+1}(z) &\equiv \frac{1}{K_{t+1}} \int_0^\infty a g_{t+1}(a, z) da \\
 &= \frac{1}{K_{t+1}} \int_0^\infty \int_{\underline{z}}^{\bar{z}} \frac{1}{\beta(1 + \pi(\tilde{z}; r_t))} a g_t \left(\frac{a}{\beta(1 + \pi(\tilde{z}))}, \tilde{z} \right) f(z | \tilde{z}) d\tilde{z} da \\
 &= \frac{K_t}{K_{t+1}} \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(\tilde{z}; r_t)) \underbrace{\frac{1}{K_t} \int_0^\infty \tilde{a} g_t(\tilde{a}, \tilde{z}) d\tilde{a}}_{\equiv \omega_t(z)} f(z | \tilde{z}) d\tilde{z} \\
 &= \frac{K_t}{K_{t+1}} \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(\tilde{z}; r_t)) \omega_t(\tilde{z}) f(z | \tilde{z}) d\tilde{z}
 \end{aligned}$$

Change of variable:

$$\tilde{a} = \frac{a}{\beta(1 + \pi(\tilde{z}))}$$

System of Equations

- Given $\{\omega_0(z)\}$ and K_0 , equilibrium $\{Y_t, Z_t, K_{t+1}, r_t, \omega_{t+1}(z)\}$ solve

$$Y_t = Z_t K_t$$

$$Z_t = \mathbb{E}_\omega[z | z \geq r_t] \equiv \frac{1}{\int_{r_t}^{\bar{z}} \omega_t(z) dz} \int_{r_t}^{\bar{z}} z \omega_t(z) dz$$

$$K_{t+1} = K_t \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(z; r_t)) \omega_t(z) dz$$

$$\lambda \int_{r_t}^{\bar{z}} \omega_t(z) dz = 1$$

$$\omega_{t+1}(z) = \frac{K_t}{K_{t+1}} \int_{\underline{z}}^{\bar{z}} \beta(1 + \pi(\tilde{z}; r_t)) \omega_t(\tilde{z}) f(z | \tilde{z}) d\tilde{z}$$

Balanced Growth Path

- We define the balanced growth path (BGP) of this economy as the one
 - $\{Z_t, r_t, \omega_t(z)\}$ are constant over time: $Z_t = Z, r_t = r, \omega_t(z) = \omega(z)$
 - K_t and Y_t keep growing at the constant rate, $1 + g \equiv Y_{t+1}/Y_t = K_{t+1}/K_t$

Long-Run Cost of Financial Friction

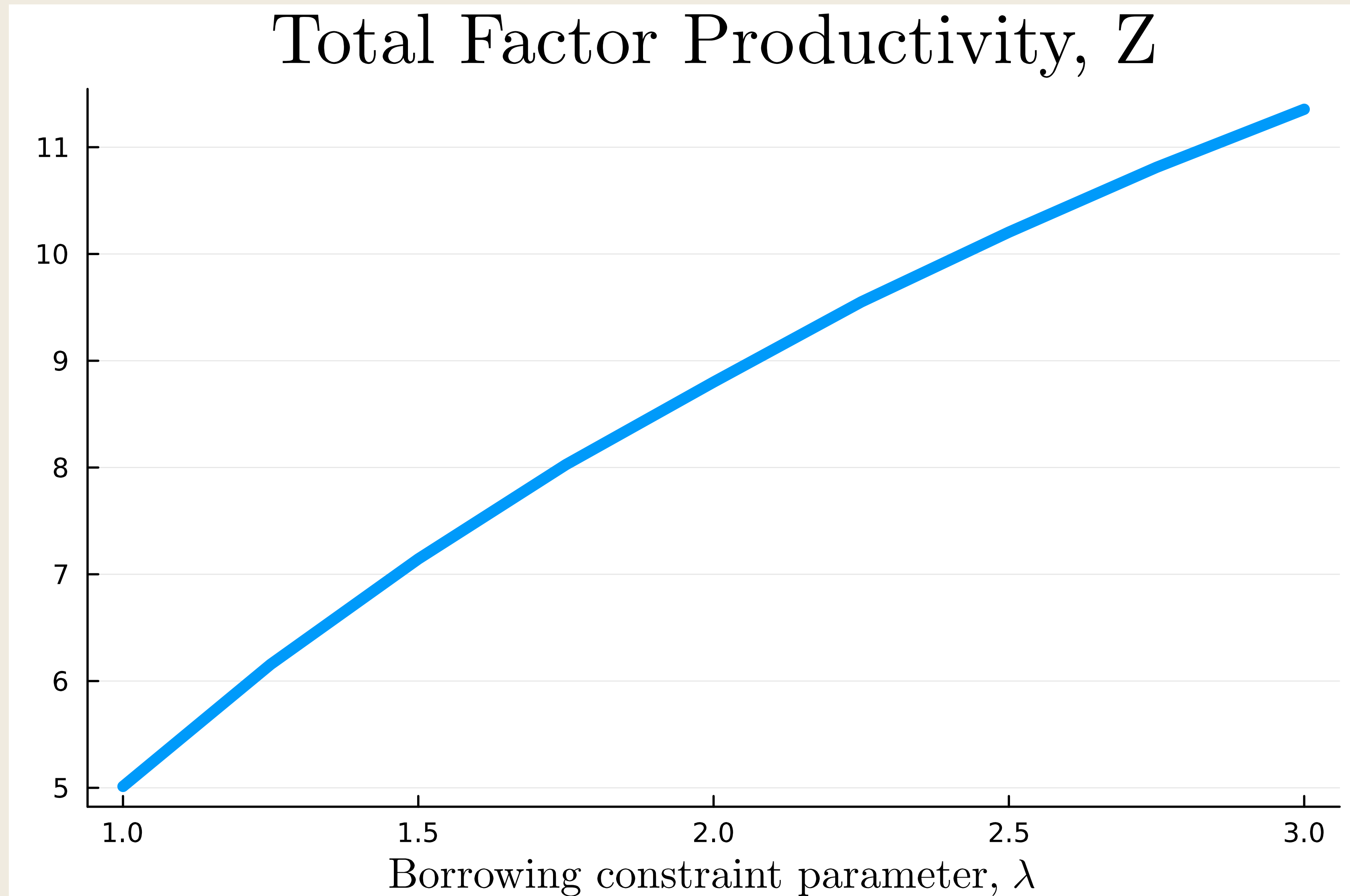
Calibration

- A period is a year. Set $\beta = 0.96$
- Parameterize the productivity process $f(z' | z)$ as

$$\log z_{t+1} = \rho_z \log z_t + \epsilon_{t+1}, \quad \epsilon_{t+1} \sim N(0, (1 - \rho_z^2) \sigma_z^2)$$

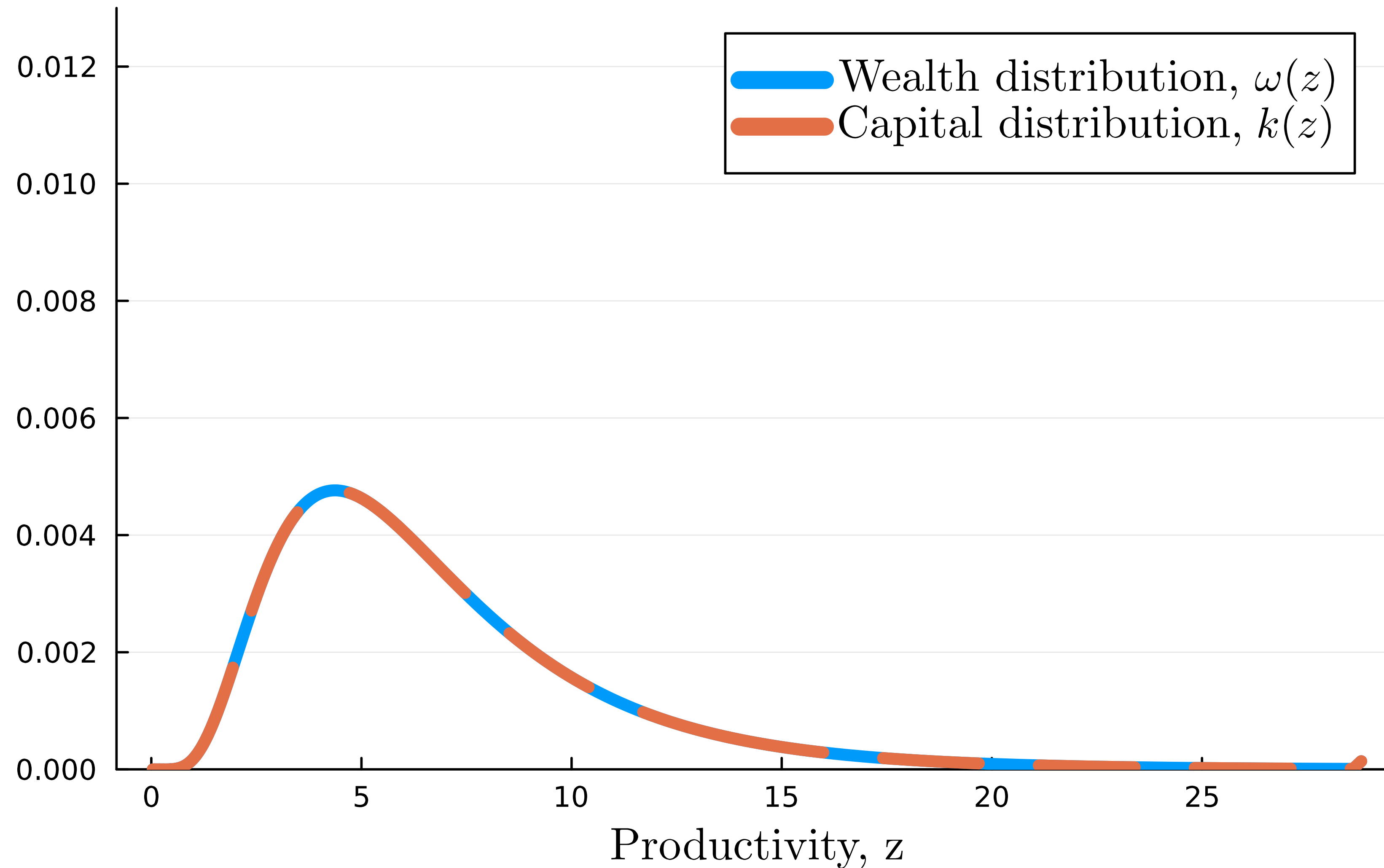
- $\rho_z \in [0, 1)$ governs the persistence, and σ_z governs the variance
 - The unconditional distribution of $\log z$ is $\log z \sim N(0, \sigma_z^2)$
 - We truncate the distribution at $[-6\sigma_z, 6\sigma_z]$
- Set $\rho_z = 0.85$ and $\sigma_z = 0.56$
 - The average reported in Asker, Collard-Wexler & De Loecker (2013)
 - Focus on the BGP and ask:
How does financial friction, λ , affect the total factor productivity Z ?

TFP Losses from Financial Friction



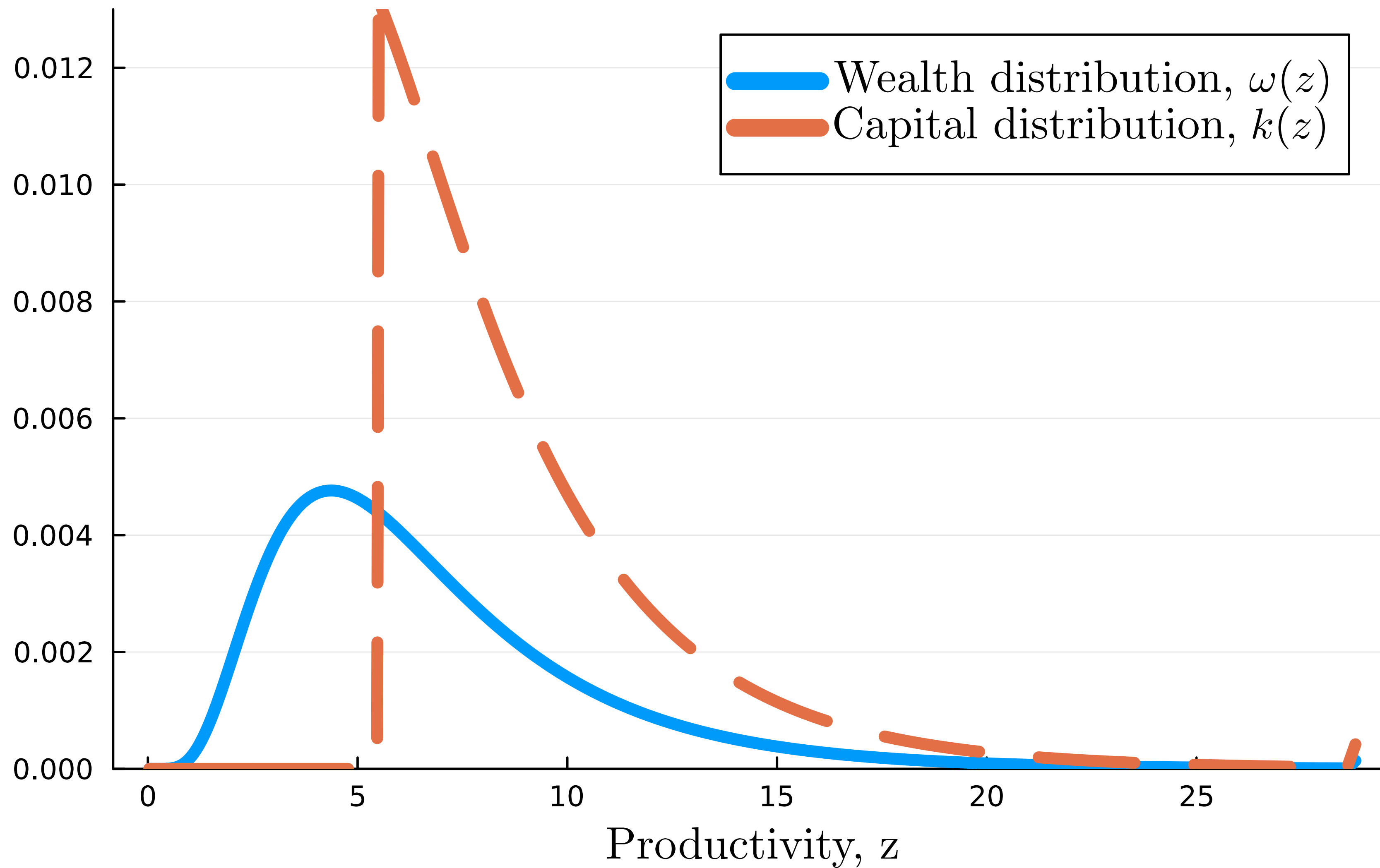
Wealth and Capital Distribution

$$\lambda = 1.0$$



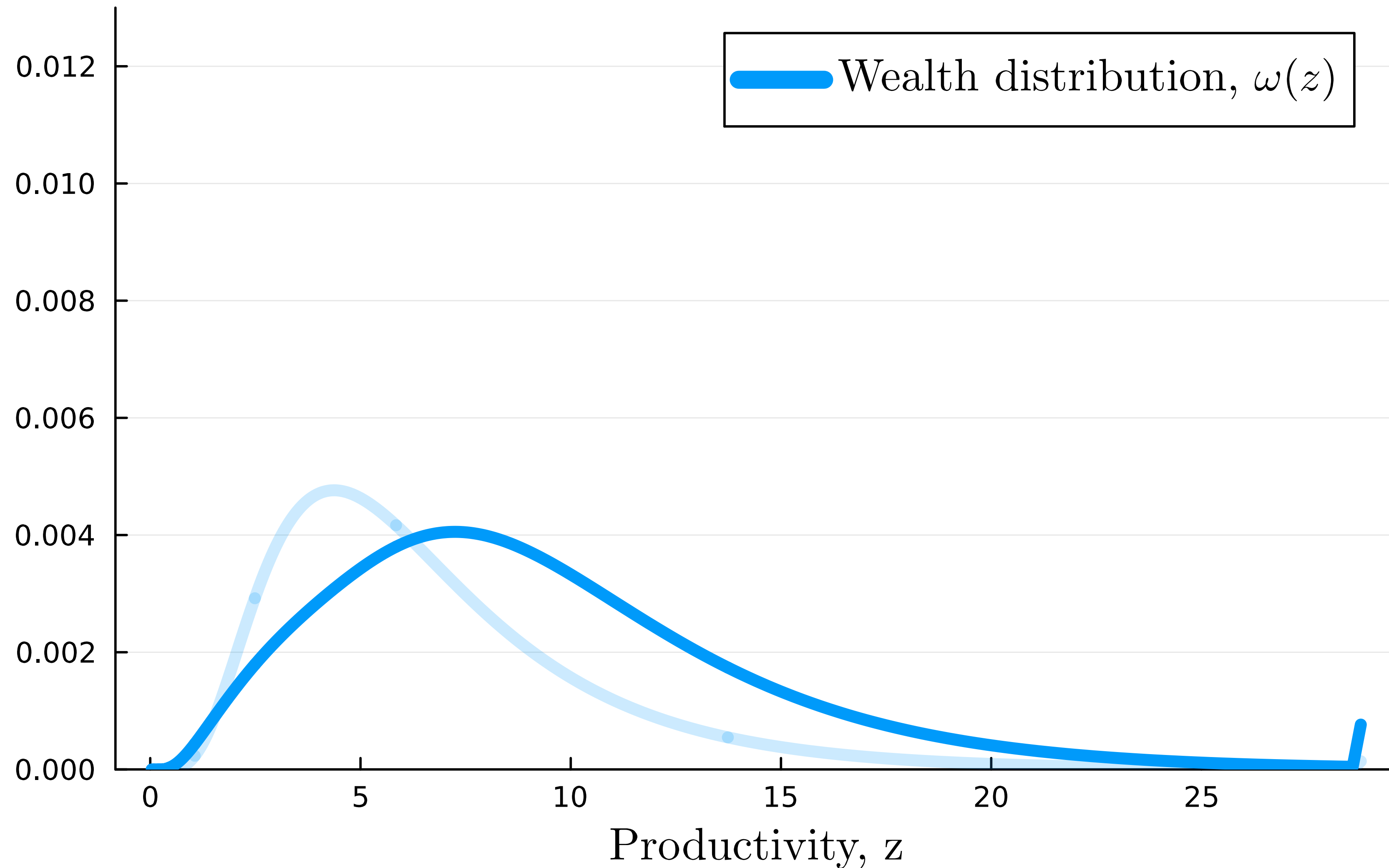
Short-Run Effect of Higher λ

$$\lambda = 3.0$$



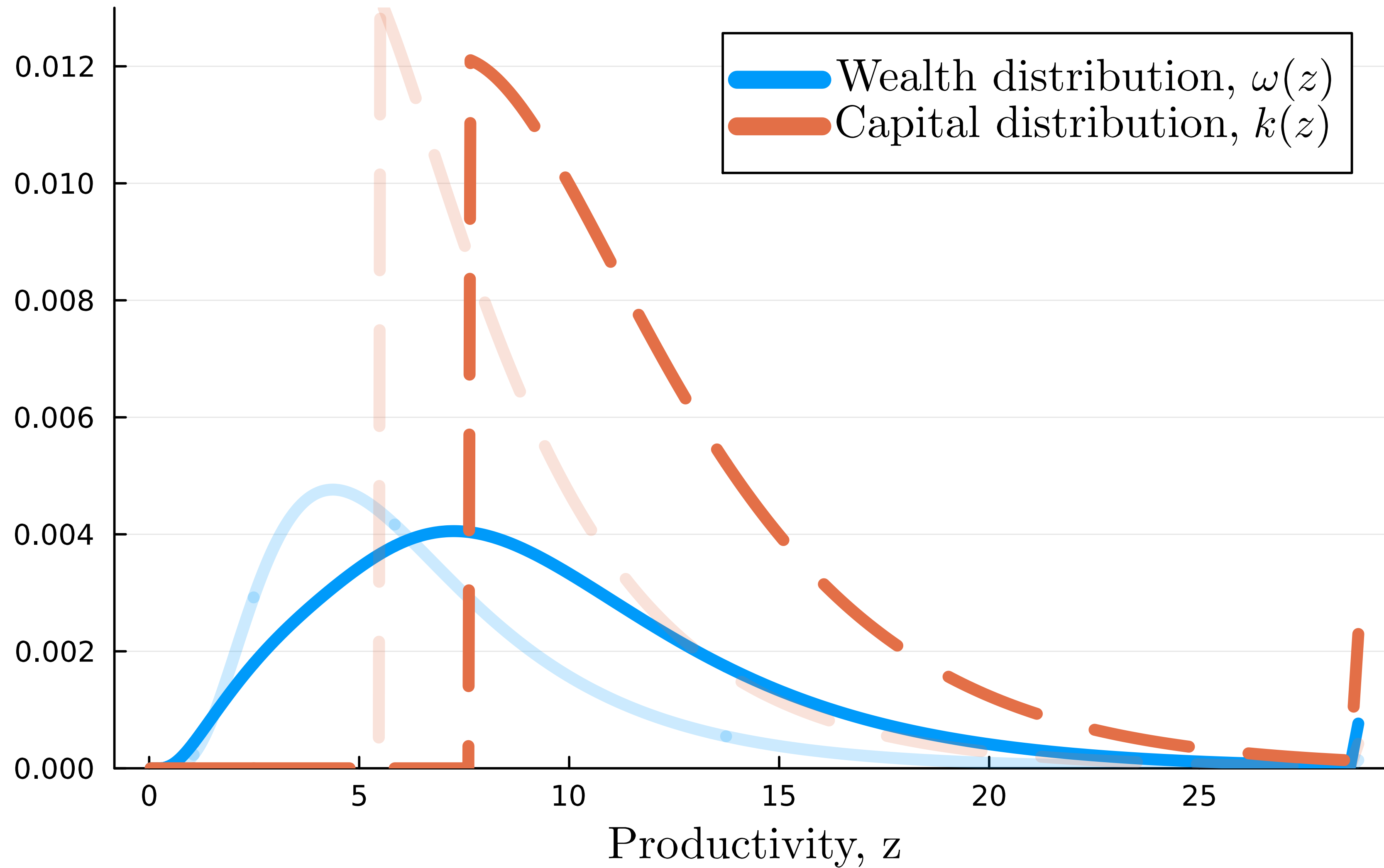
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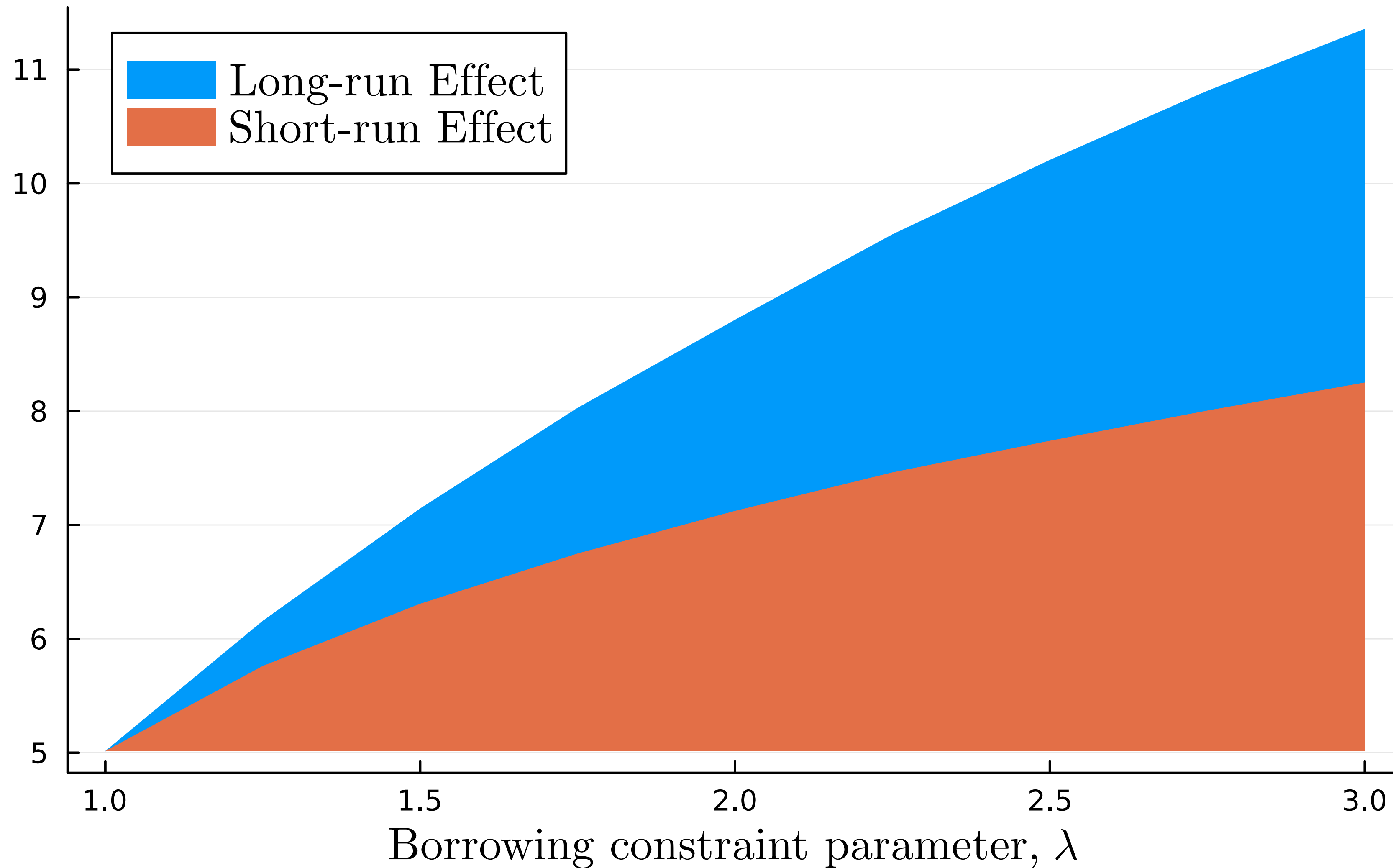
Long-Run Effect of Higher λ

$$\lambda = 3.0$$



Decomposition

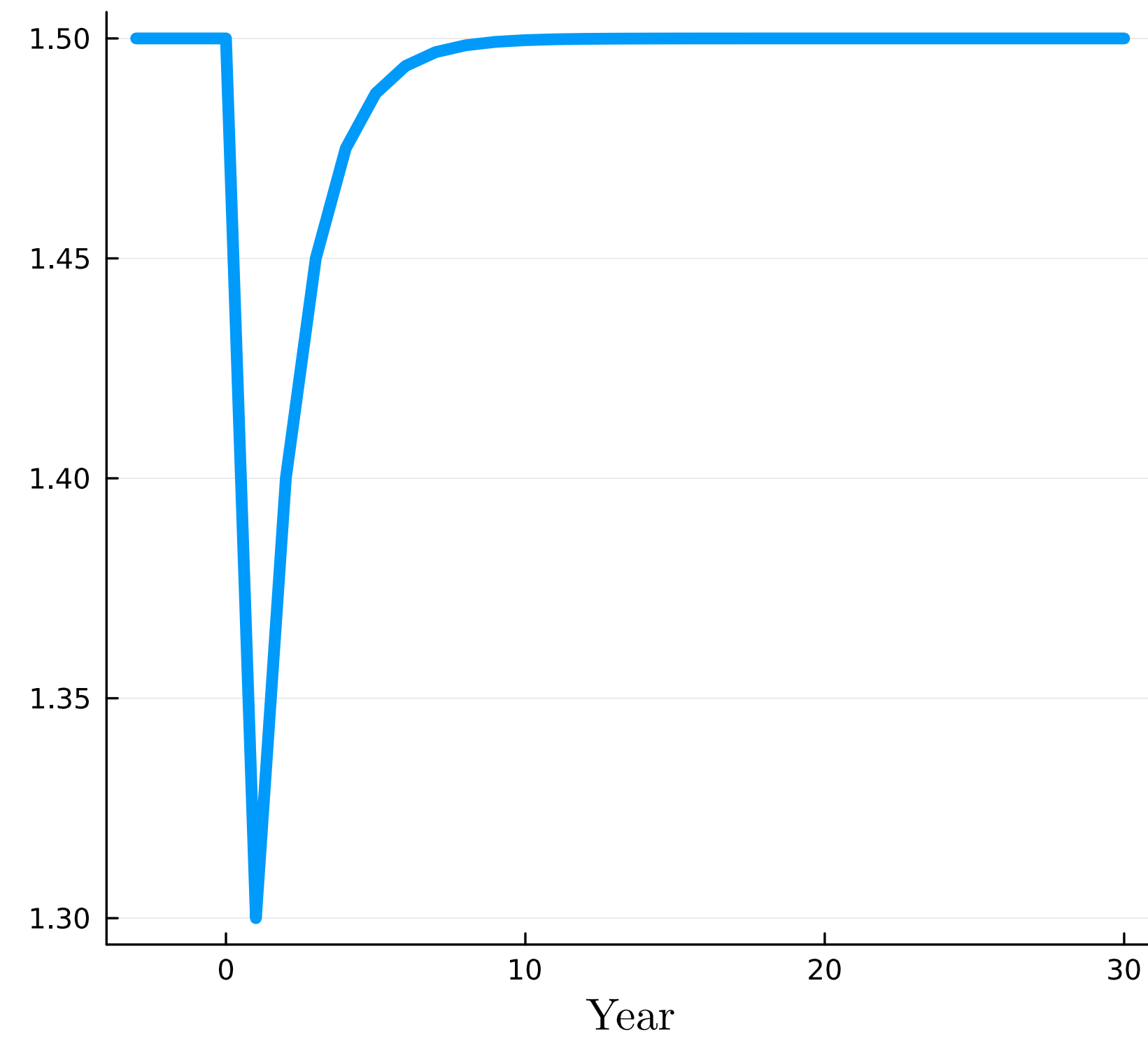
Total Factor Productivity, Z



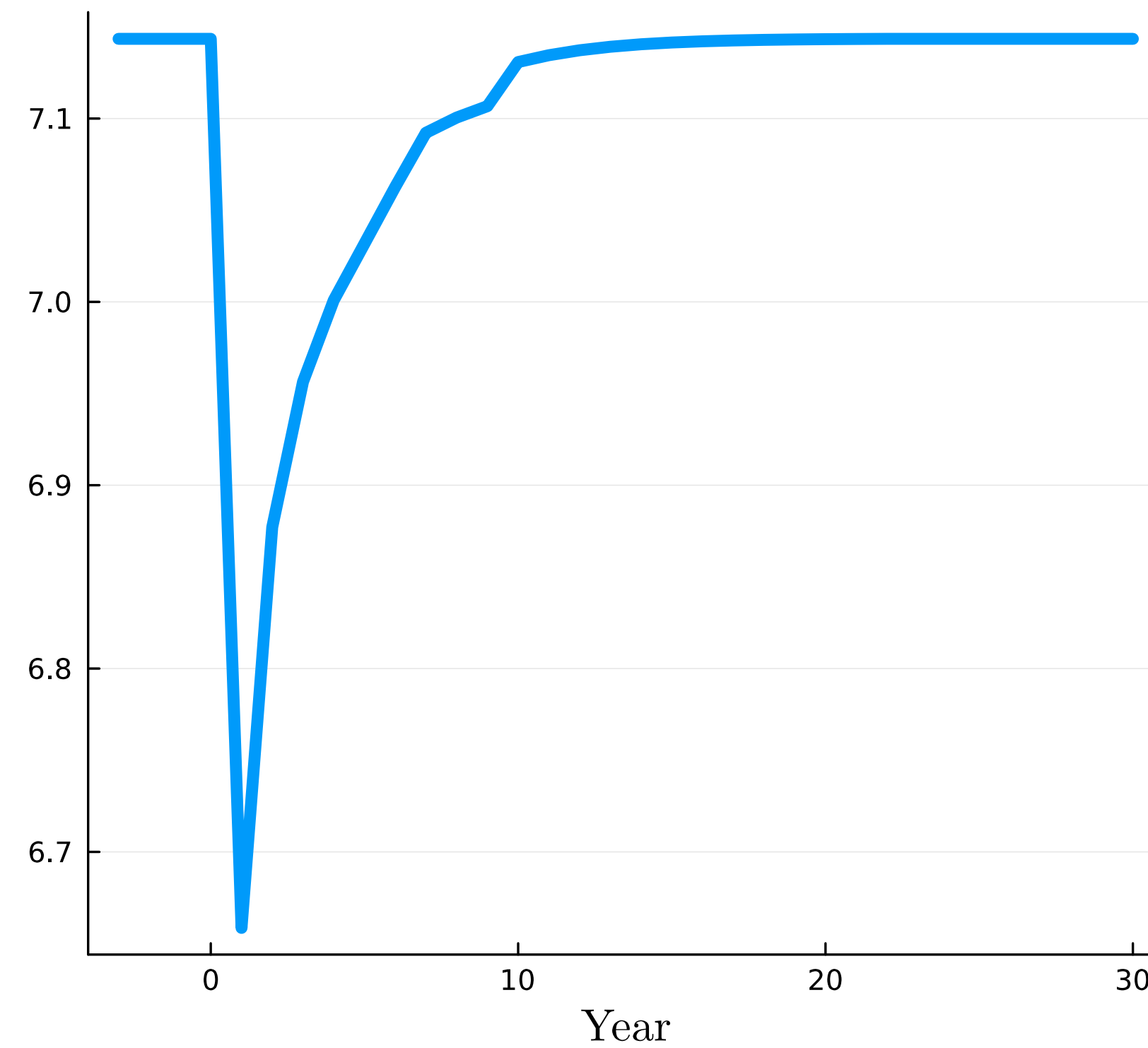
Short-Run Impact of Disruption in Financial Intermediation

Impulse Response to Credit Crunch

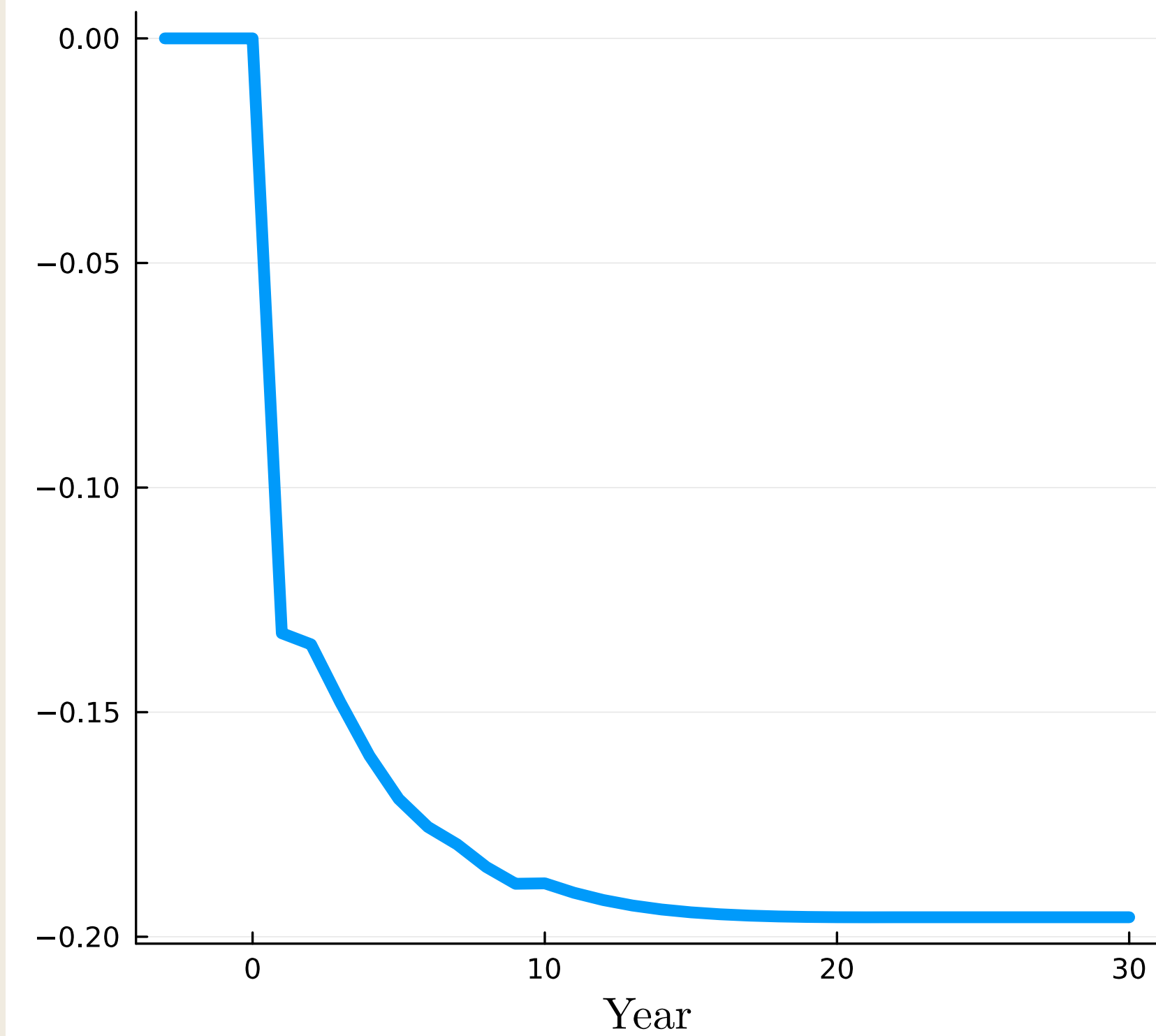
Borrowing constraint, λ



Total Factor Productivity, Z



Log Output, $\log(Y)$

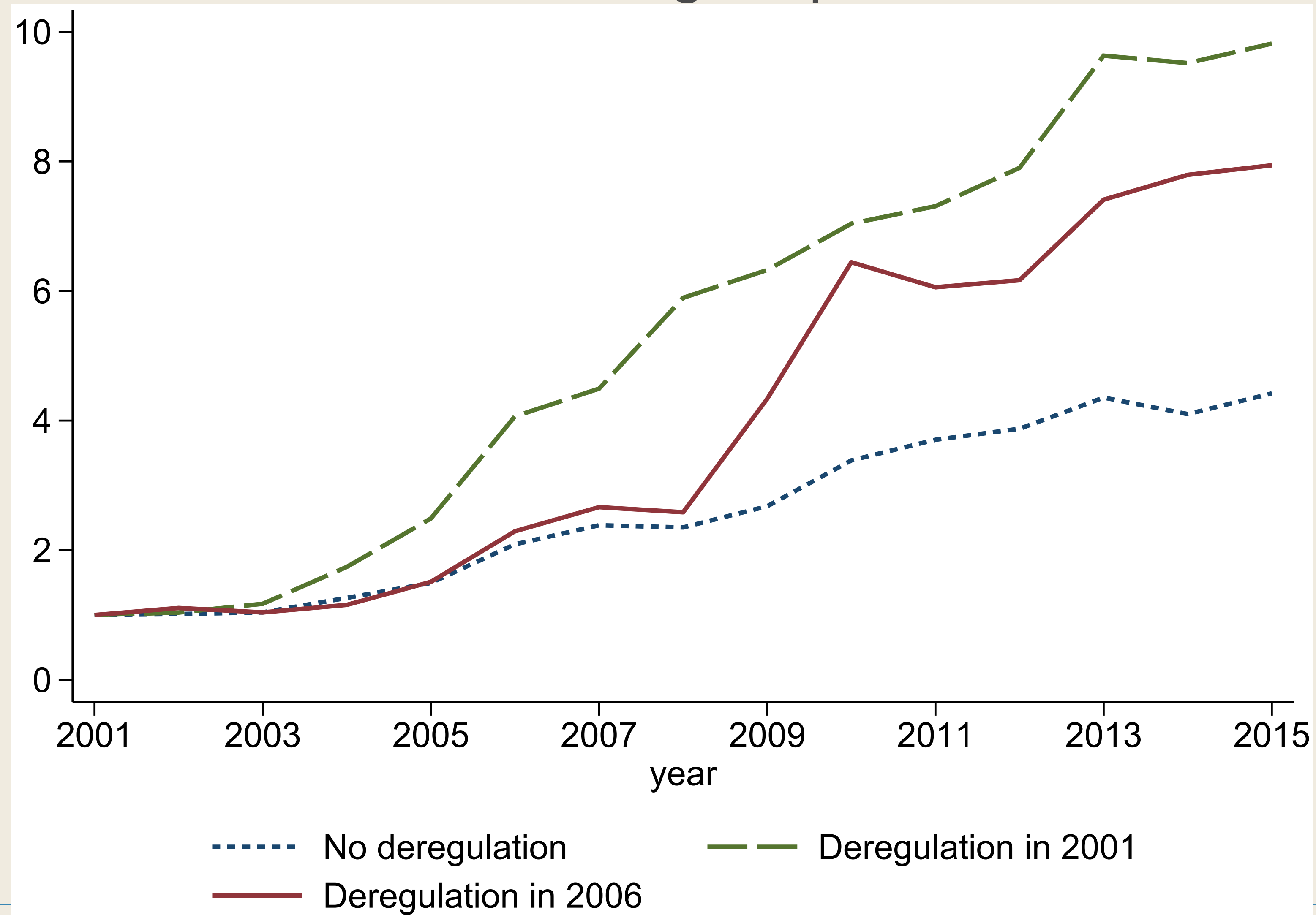


Misallocation and Capital Market Integration

– **Bau and Matray (2023)**

India's FDI Deregulation

Flow of Foreign Equities



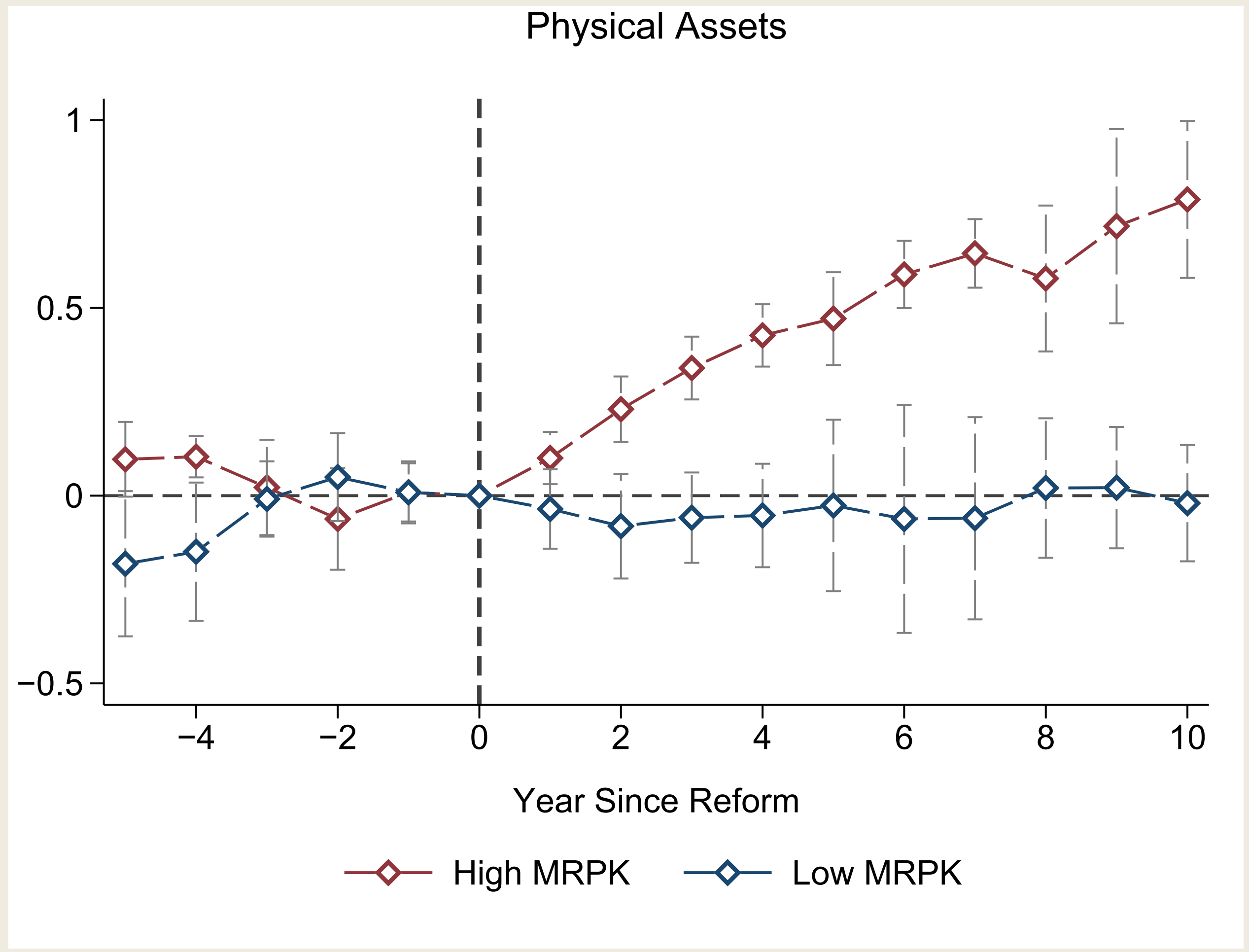
Econometric Model

$$Outcome_{ijt} = \beta_1 Reform_{jt} + \beta_2 Reform_{jt} \times I_i^{High\ MRPK} + \mathbf{\Gamma X}_{it} + \theta_i + \delta_t + \epsilon_{ijt},$$

i : firm, j : industry, t : year, $MRPK$: proxied by $ARPK$ (valid under Cobb-Douglas)

- FDI deregulation \approx relaxation of borrowing limit λ
- Model predicts:
 - More productive (high MPRK) firms expand
 - Less productive firms should see no effect or contract

Main Result



Aggregate Impact of FDI Deregulation

- A simple aggregation:
India's FDI deregulation in the 2000s increased TFP by 3-16%