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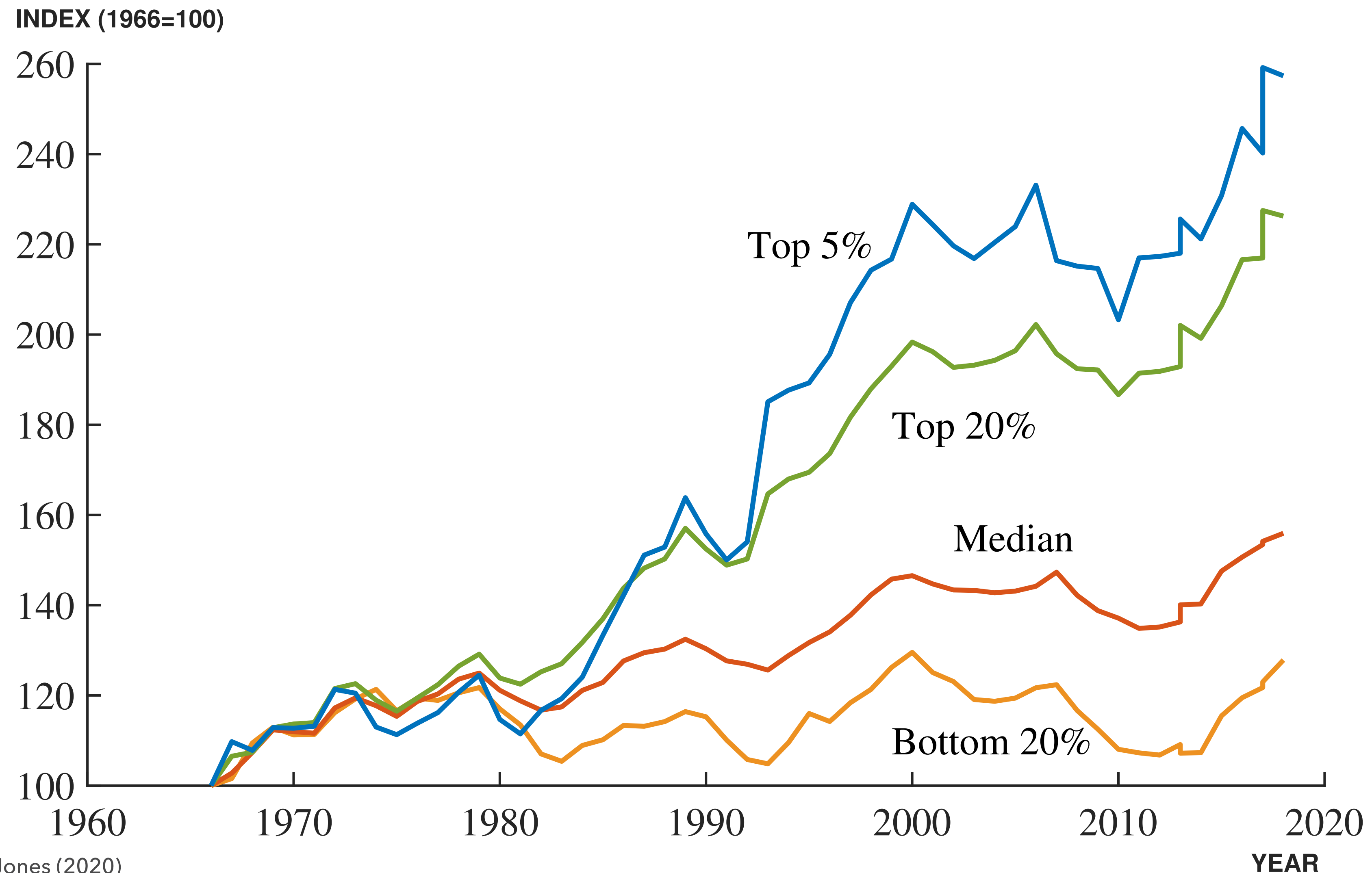
# Technological Change and Income Inequality

EC502 Macroeconomics  
Topic 5

Masao Fukui

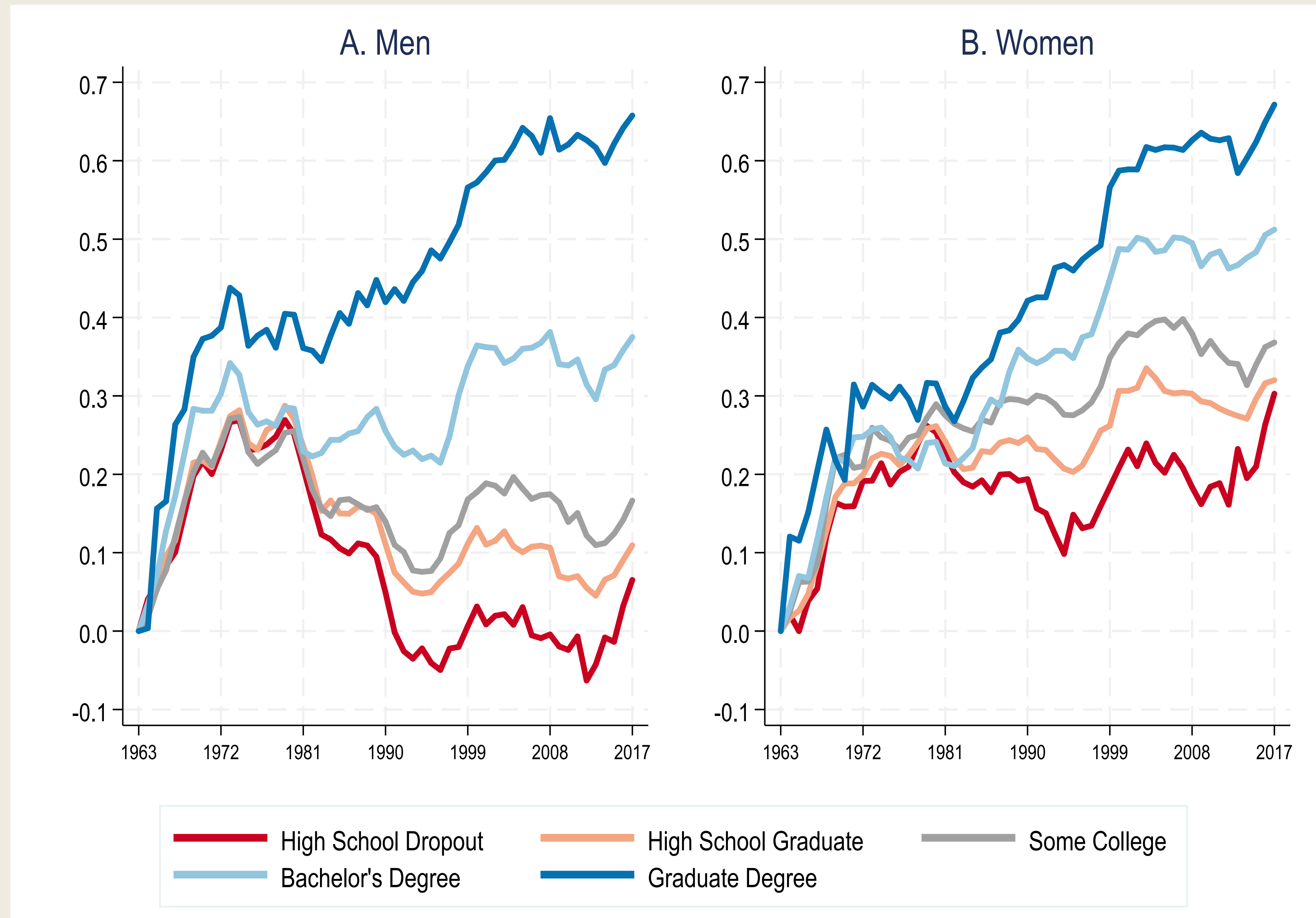
2025 Spring

# Growing Income Inequality in the US



Source: Jones (2020)

# Rising Real Wage Inequality Across Educational Groups



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# Skill-Biased Technical Change

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# Production Function

- Firms use high- and low-skill labor to produce output:

$$Y = F(L_L, L_H)$$

- $L_L$ : low-skill labor
- $L_H$ : high-skill labor
- $F$ : constant returns to scale

- Assume:

$$F(L_L, L_H) = \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

- $A_L$ : low-skill augmenting technology,  $A_H$ : high-skill augmenting technology
- $\sigma > 0$ : elasticity of substitution between high- and low-skill labor

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# Three Special Cases

$$F(L_L, L_H) = \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

1. If  $\sigma \rightarrow \infty$ , we have a linear production function:

$$F(L_L, L_H) = A_L L_L + A_H L_H$$

2. If  $\sigma = 1$ , we have a Cobb-Douglas production function:

$$F(L_L, L_H) = (A_L L_L)^{1/2} (A_H L_H)^{1/2}$$

3. If  $\sigma \rightarrow 0$ , we have a Leontief production function

$$F(L_L, L_H) = \min\{A_L L_L, A_H L_H\}$$

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# Firm's Profit Maximization

- Firms take the wage of each skill group as given and decide how many to hire

$$\max_{L_L, L_H} F(L_L, L_H) - w_L L_L - w_H L_H$$

- First-order conditions:

$$\underbrace{F_L(L_L, L_H)}_{\text{MPL of low-skill labor}} = w_L$$

$$\underbrace{F_H(L_L, L_H)}_{\text{MPL of high-skill labor}} = w_H$$

- Assume  $L_H$  and  $L_L$  are exogenous

# Labor Demand

- With our functional form,

$$w_H = A_H^{\frac{\sigma-1}{\sigma}} (L_H)^{-\frac{1}{\sigma}} \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$
$$w_L = A_L^{\frac{\sigma-1}{\sigma}} (L_L)^{-\frac{1}{\sigma}} \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

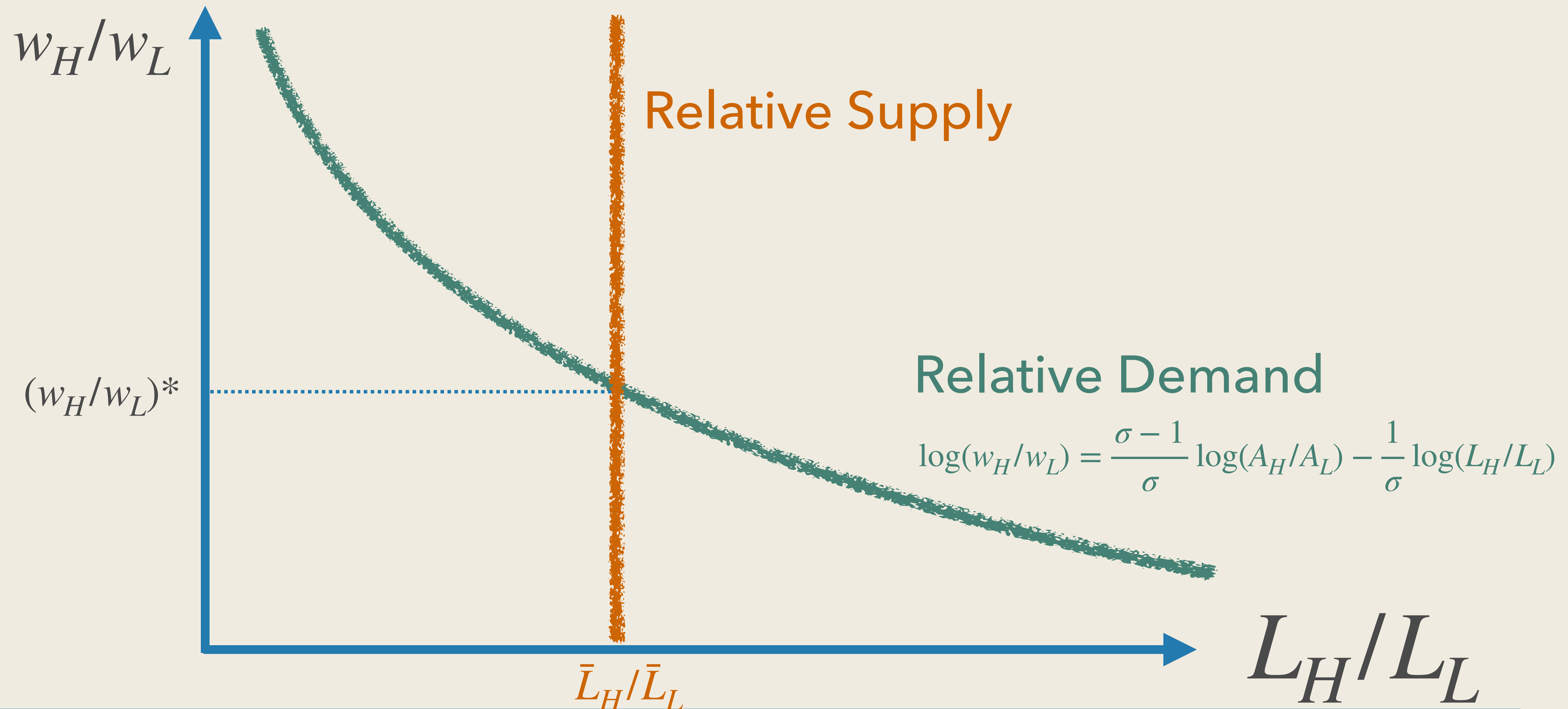
- Taking the ratio, relative labor demand,  $L_H/L_L$ , is

$$\log(L_H/L_L) = (\sigma - 1)\log(A_H/A_L) - \sigma \log(w_H/w_L)$$

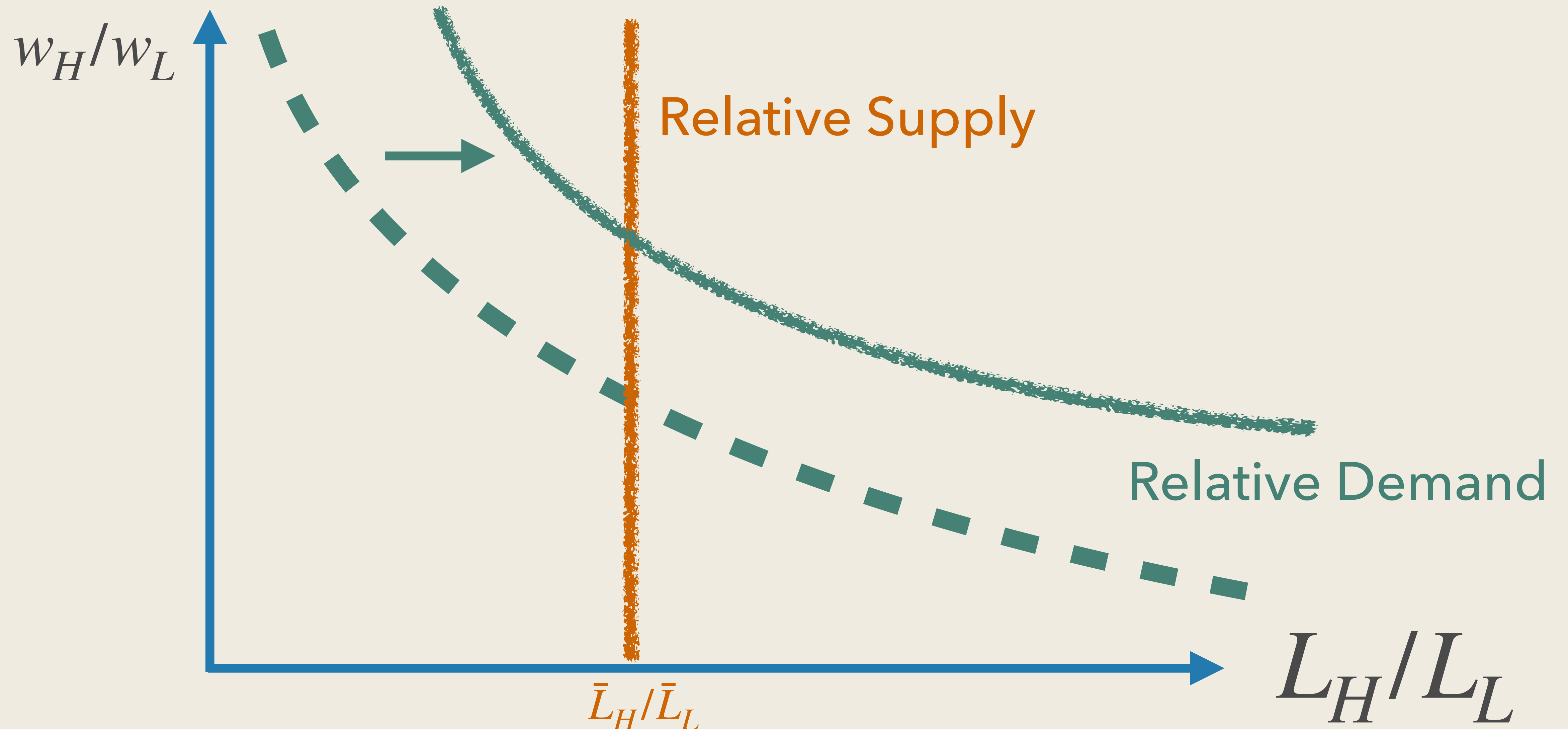
- A rise in  $A_H$  relative to  $A_L$ 
  - raises relative labor demand for skilled if  $\sigma > 1$  (substitutes).
  - lowers relative labor demand for skilled if  $\sigma < 1$  (complements)



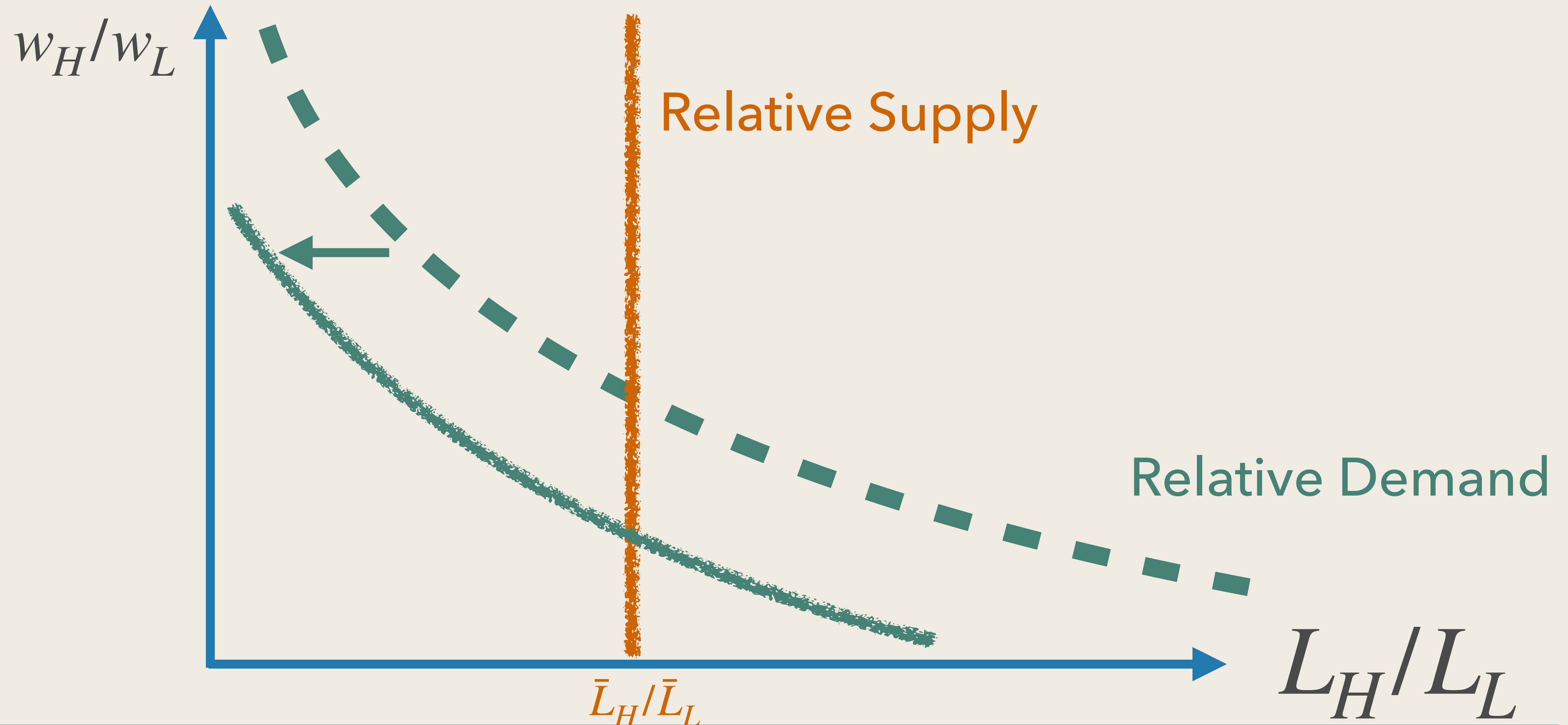
# Demand and Supply



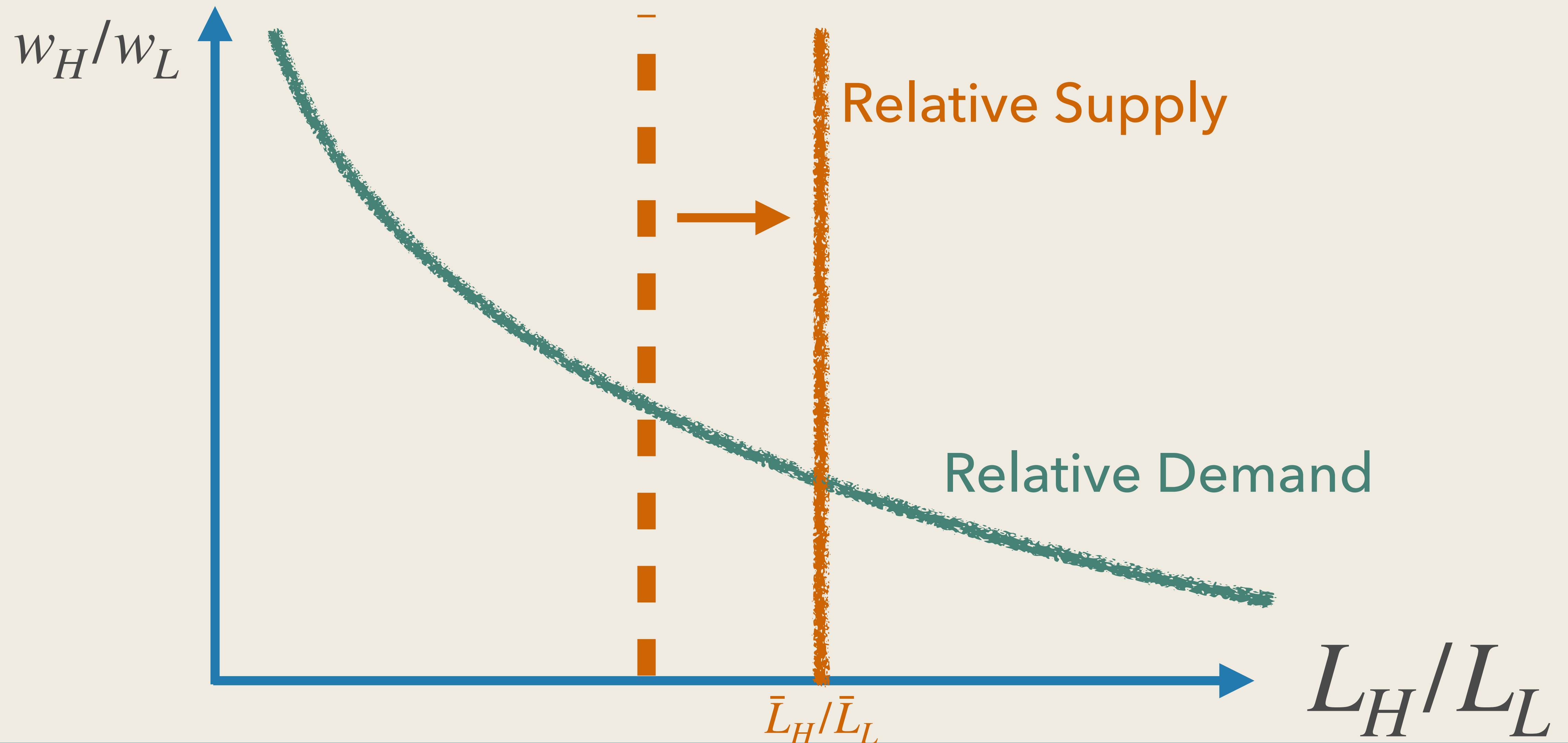
**Increase in  $A_H/A_L$  if  $\sigma > 1$**



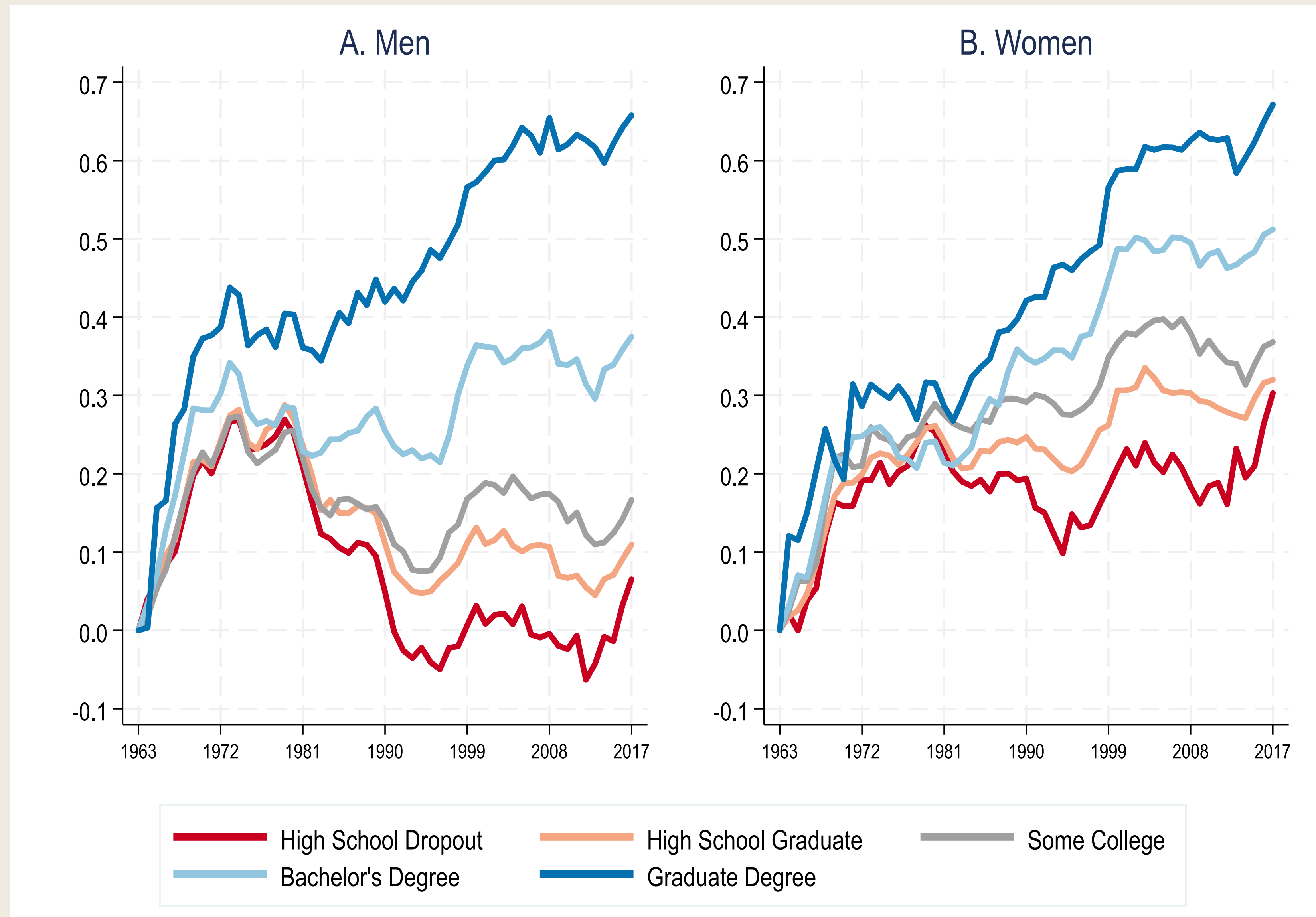
**Increase in  $A_H/A_L$  if  $\sigma < 1$**



# Increase in $\bar{L}_H/\bar{L}_L$

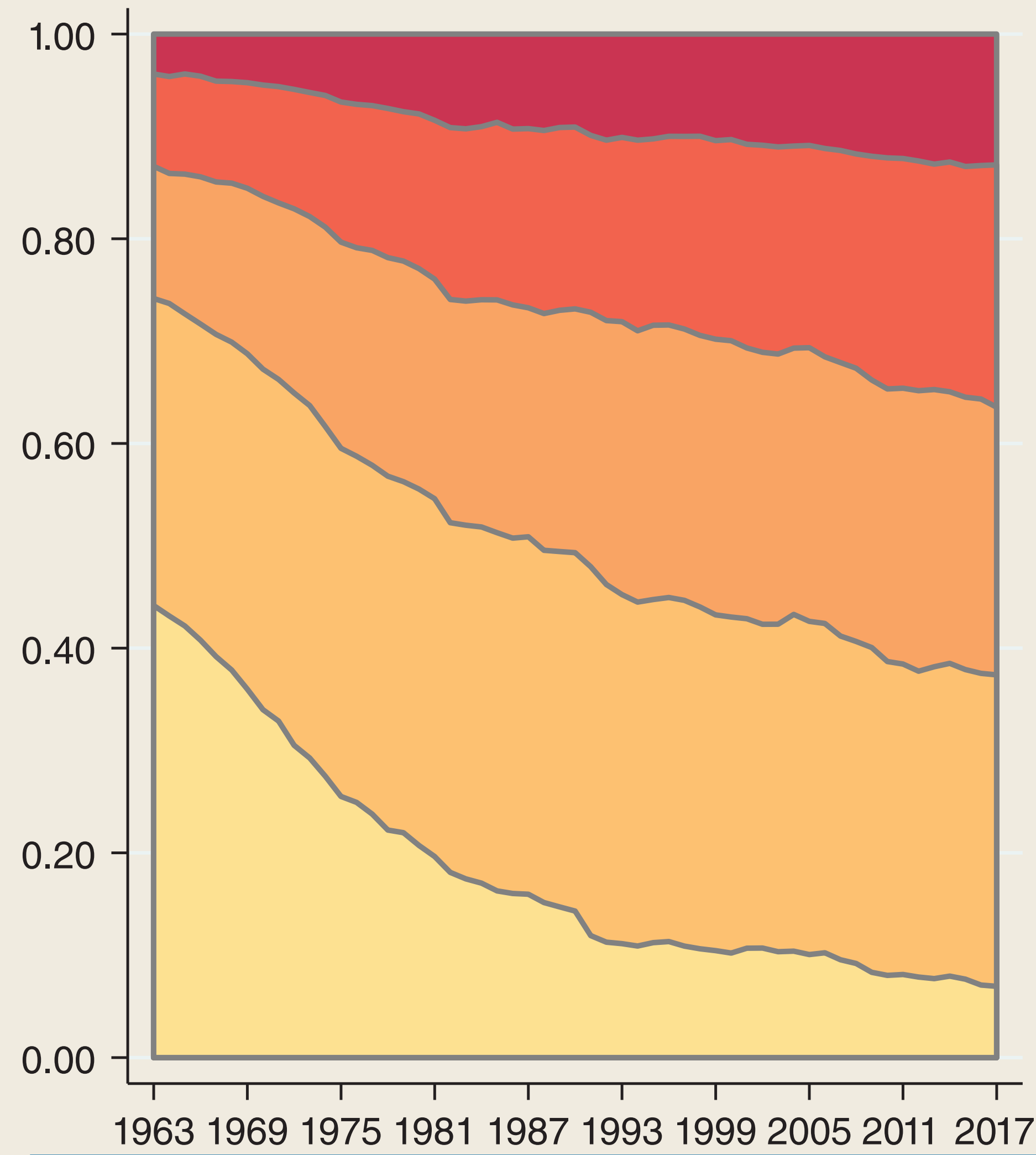


# Rising Real Wage Inequality Across Educational Groups

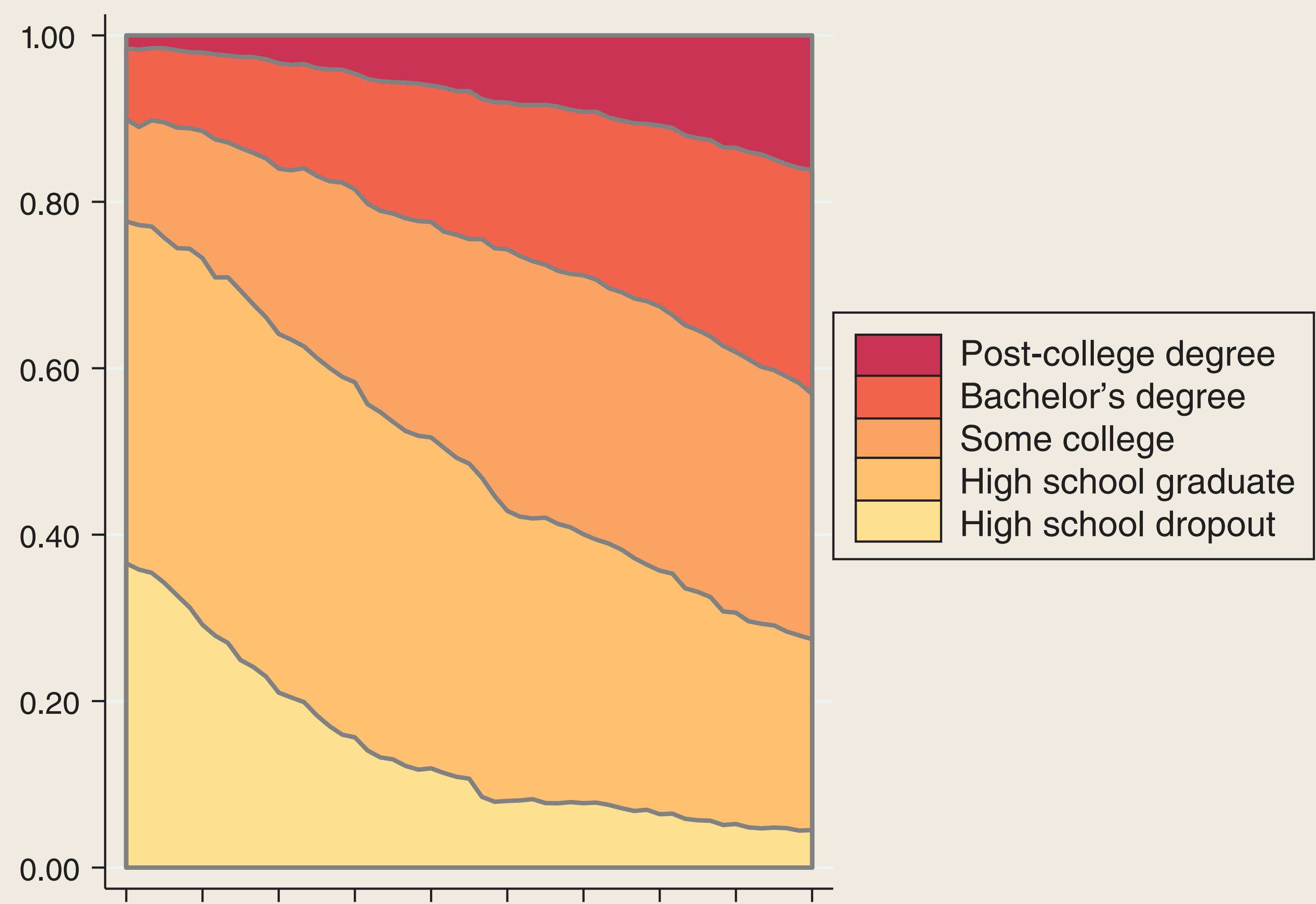


# Hours Worked Share

Panel A. Men



Panel B. Women



# What Has Happened?

$$\log(w_H/w_L) = \frac{\sigma - 1}{\sigma} \log(A_H/A_L) - \frac{1}{\sigma} \log(L_H/L_L)$$

Went up!

Went up!

- What needs to have happened to  $A_H/A_L$  in the past?
- If  $\sigma > 1$ ,  $A_H/A_L$  must have been rising (**skill-biased technical change**)
- The consensus among macroeconomists is that  $\sigma > 1$

# Inferring $A_H$ and $A_L$

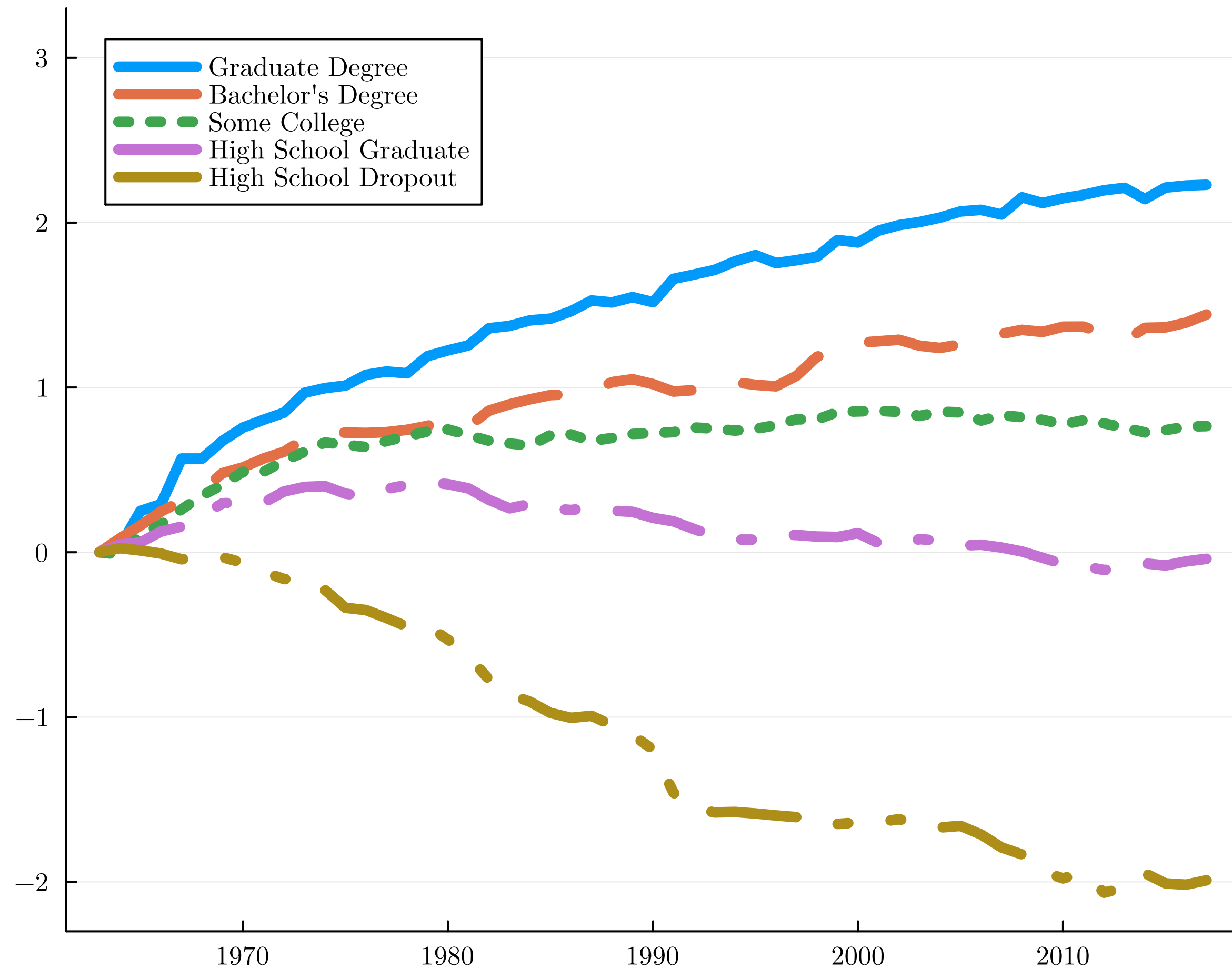
$$w_H = A_H^{\frac{\sigma-1}{\sigma}} (L_H)^{-\frac{1}{\sigma}} \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$
$$w_L = A_L^{\frac{\sigma-1}{\sigma}} (L_L)^{-\frac{1}{\sigma}} \left( (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

- Suppose we know  $\sigma$  (consensus around  $\sigma \in [2,5]$ )
- We observe  $(L_H, L_L)$  and  $(w_H, w_L)$  in the data
- We can reverse-engineer  $(A_H, A_L)$  in the data
  - Just as in how we constructed aggregate TFP (Solow residual)
  - Now each for different groups of people!
- Implement with more than two skill groups:
  - post-college, college, some college, high-school, high-school dropout

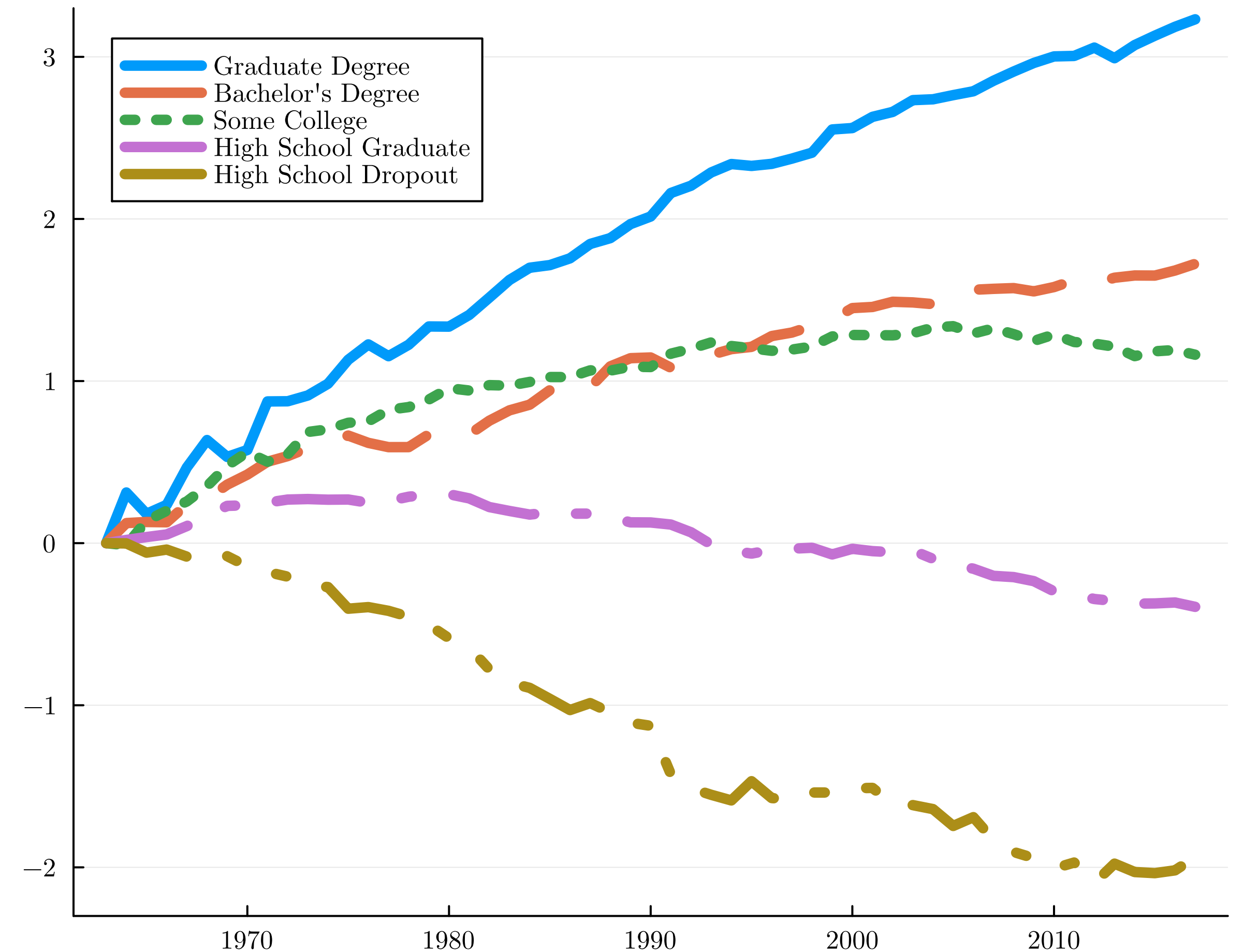


# Inferred $A$ with $\sigma = 2$

Inferred  $A$  for Men (in log)

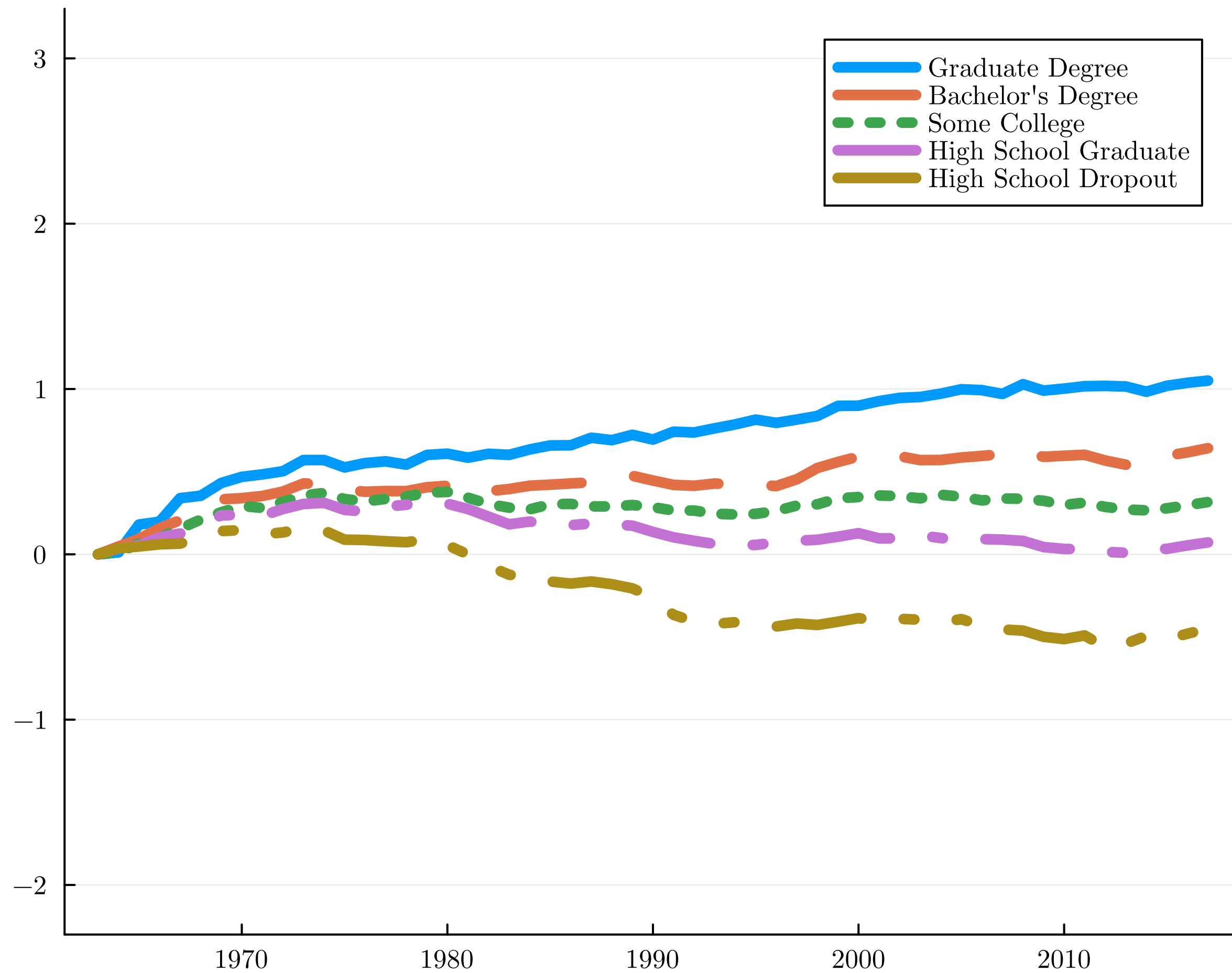


Inferred  $A$  for Women (in log)

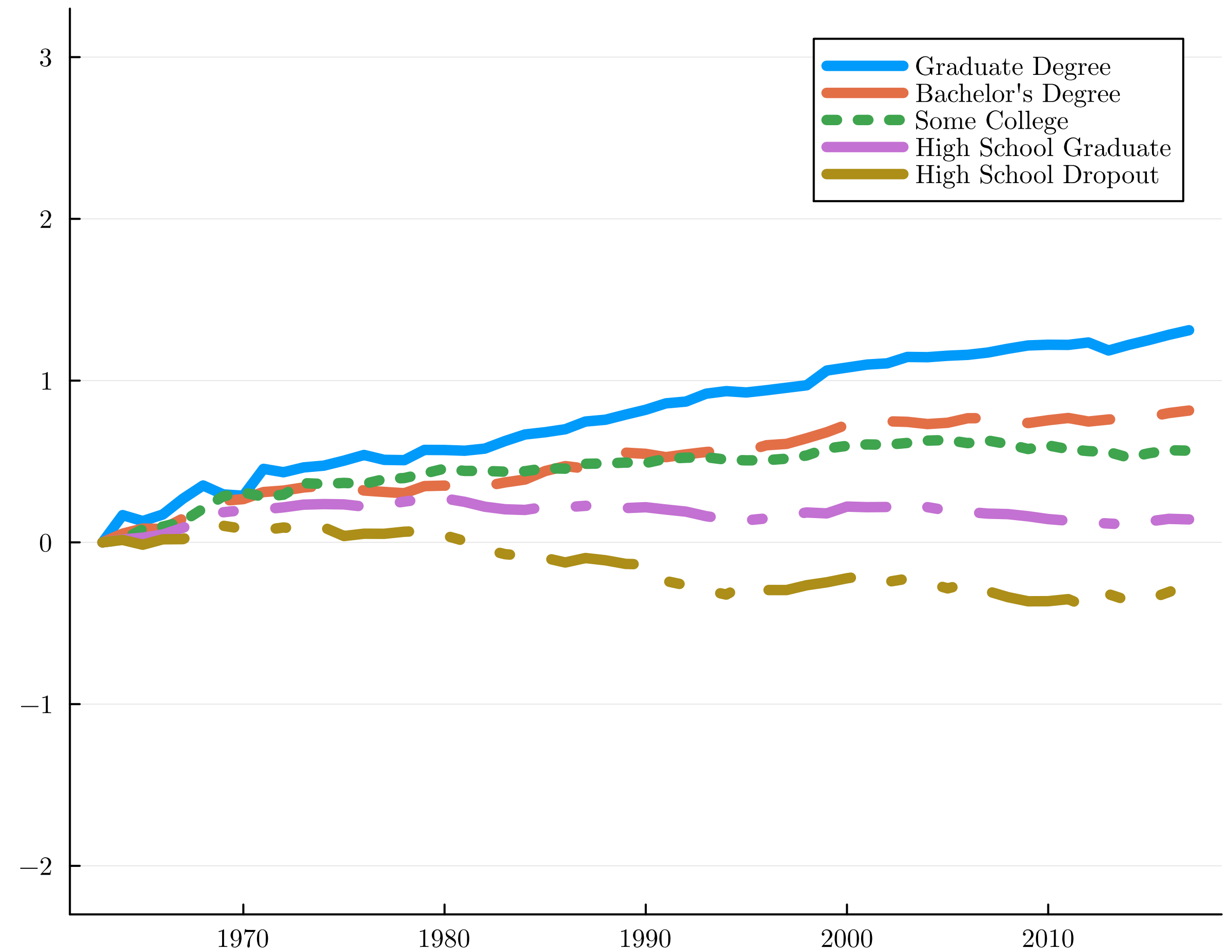


# Inferred $A$ with $\sigma = 5$

Inferred  $A$  for Men (in log)



Inferred  $A$  for Women (in log)



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# Takeaway

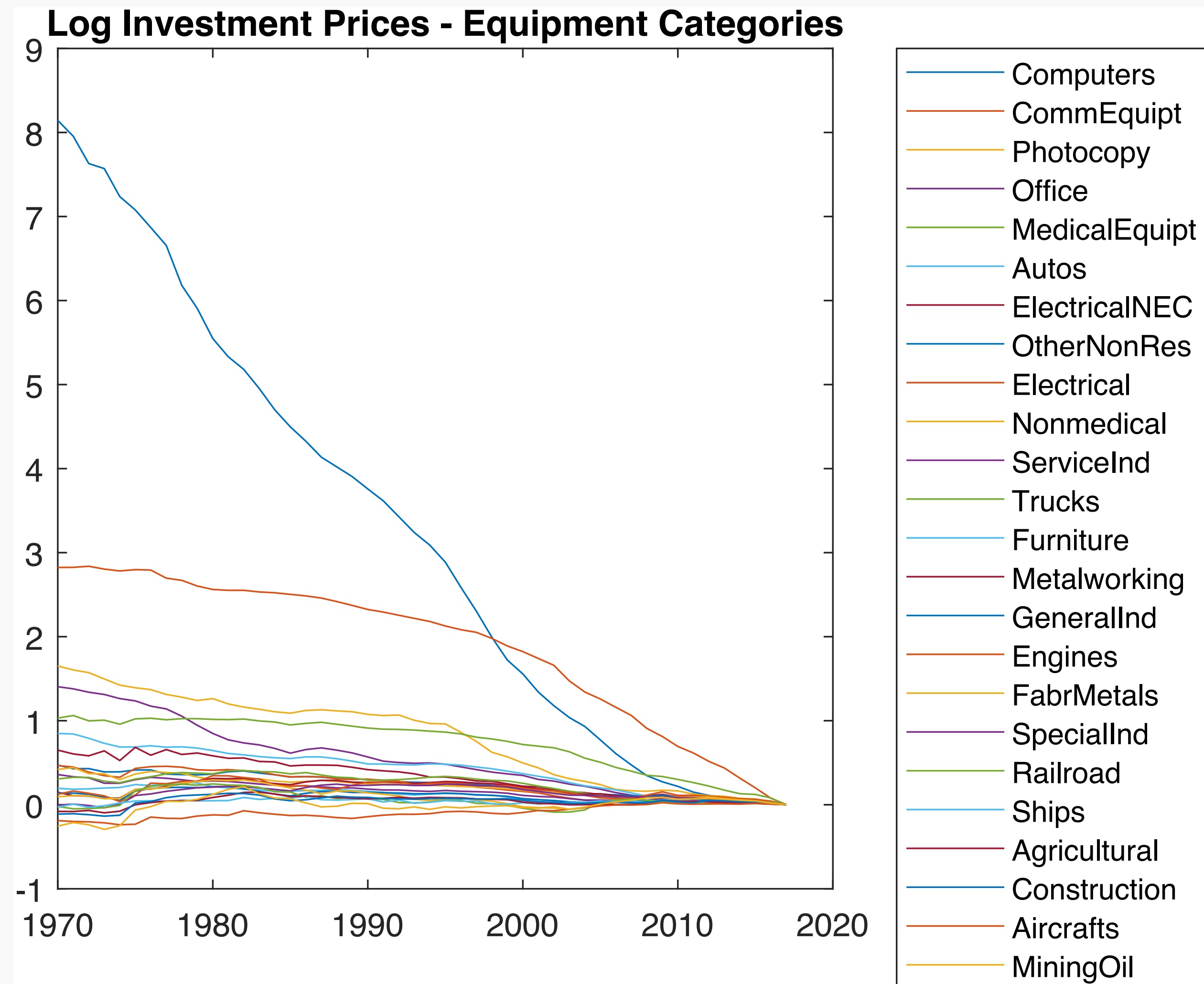
- Productivity of more educated groups sharply increasing over time
  - 50-300% **increase** during 1962-2017
- Productivity of less educated groups sharply declining over time
  - 50-250% **decrease** during 1962-2017
- We infer a substantial degree of “skill-biased technological change”
- What exactly are these technological changes?
- Let us try to understand  $A_H$  and  $A_L$  through two cases

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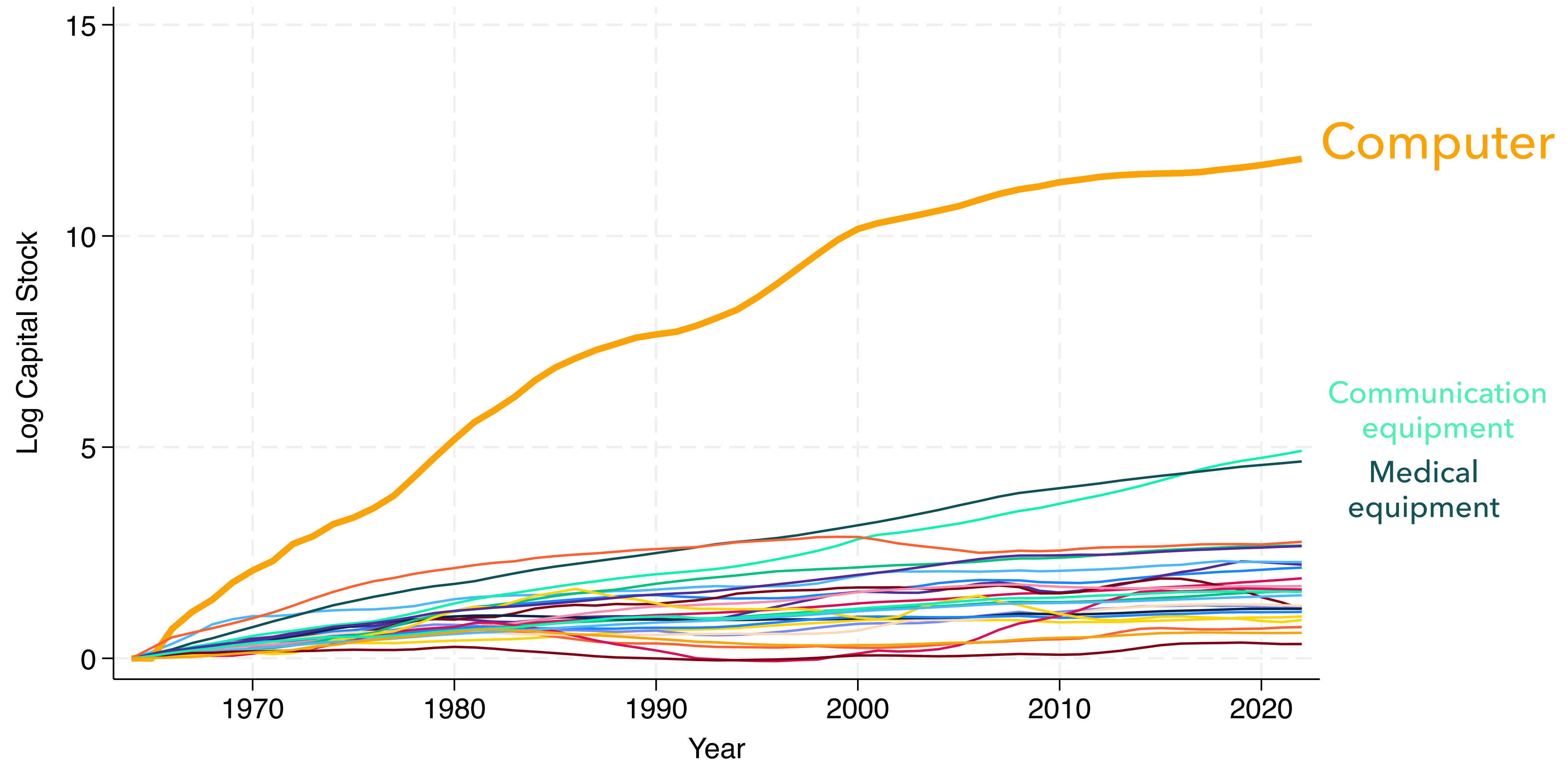
# **1. Information & Communication Technology**

## **– Akerman, Gaarder& Mogstad (2015)**

# Declining ICT Equipment Prices



# Surge in ICT Capital Stock



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# Question

- How do the recent advancements in IC technology affect inequality?
- Setup: Norway 2001-2007
- Institutional background: National Broadband Policy
  - Goal: nationwide broadband access at uniform pricing
  - Means: infrastructure investments, local gov't mandates
- 428 municipalities differed in the timing of the rollout of broadband internet
  - compare municipality with early rollout to the late rollout
- Skill groups: (i) skill (college); (ii) medium (high-school); (iii) low (less than high-school)



# Broadband Internet Availability in Norway

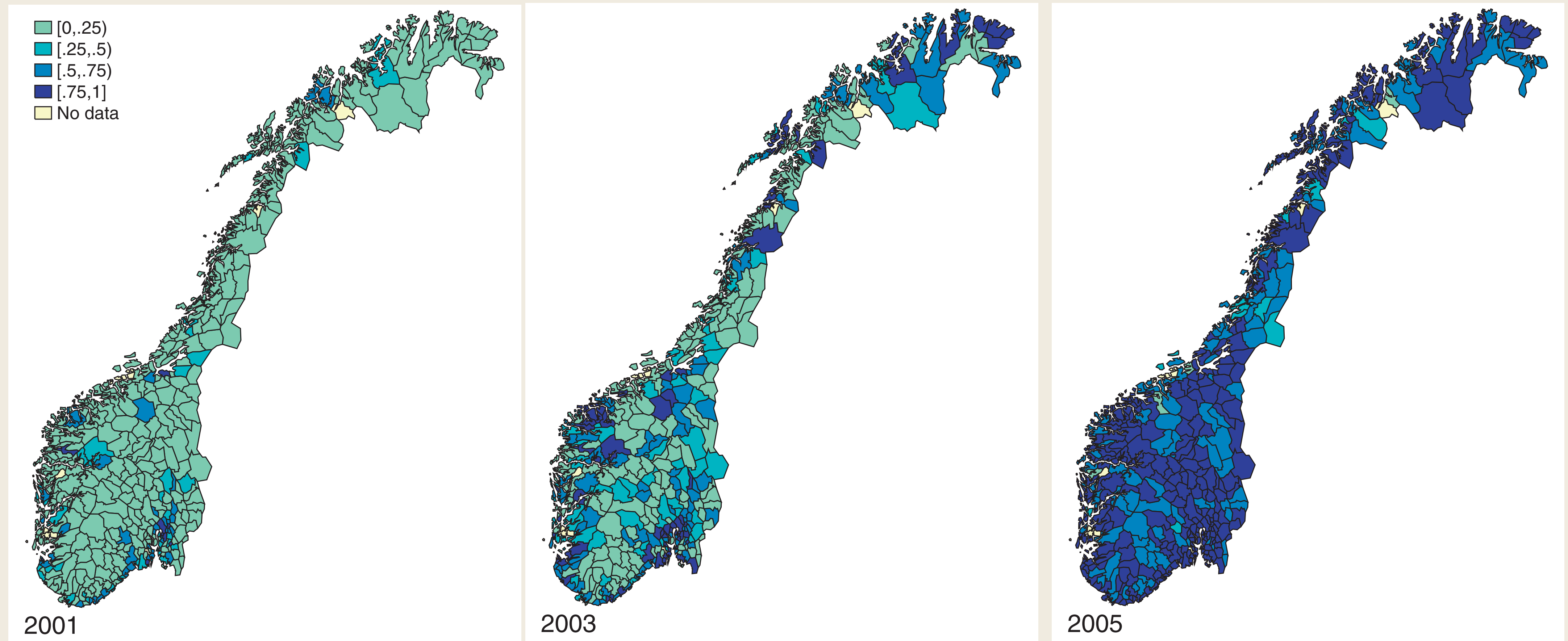


FIGURE I

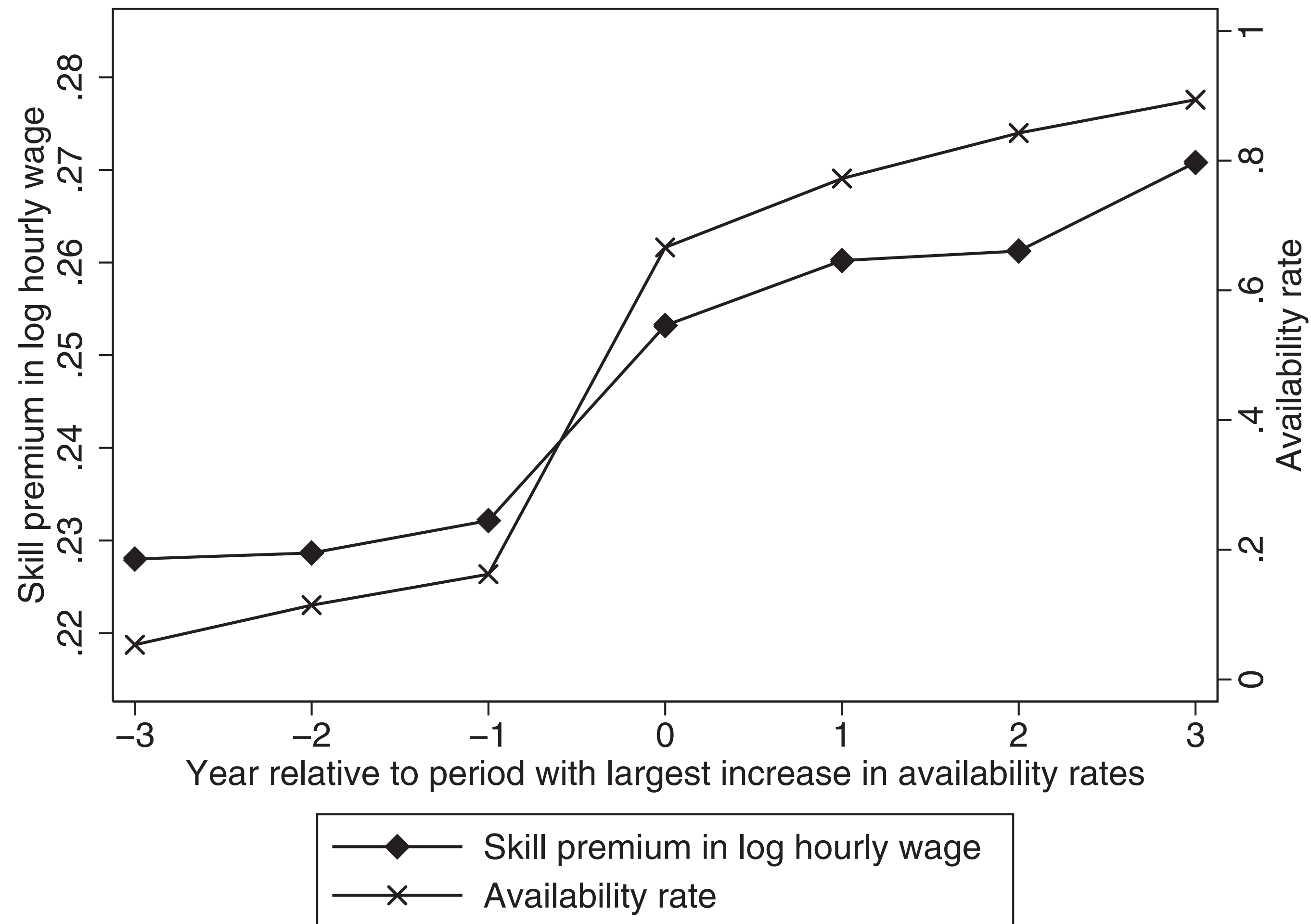
Geographical Distribution of Broadband Availability Rates

The graphs show the geographical distribution of broadband availability rates of households in 2001, 2003, and 2005.



# Impact of the Broadband Internet on Skill Premium

(c) Return to Skill: Hourly wage



# Impact on Wages and Employment

Dependent variable	(1)	(2)	(3)	(4)
	Log hourly wage		Employment	
	2 skills	3 skills	2 skills	3 skills
Availability × Unskilled	−0.00622 (0.00455)		0.000794 (0.00252)	
Low skilled		−0.0108*** (0.00325)		−0.00392 (0.00244)
Medium skilled		−0.00793 (0.00600)		0.00388 (0.00281)
Skilled	0.0178** (0.00720)	0.0202*** (0.00692)	0.0208** (0.00920)	0.0225** (0.00892)
Worker-year observations	8,759,388	8,759,388	20,327,515	20,327,515
		<i>p</i> -values		
Test for no skill bias	.000	.000	.012	.001

## ■ Availability of internet...

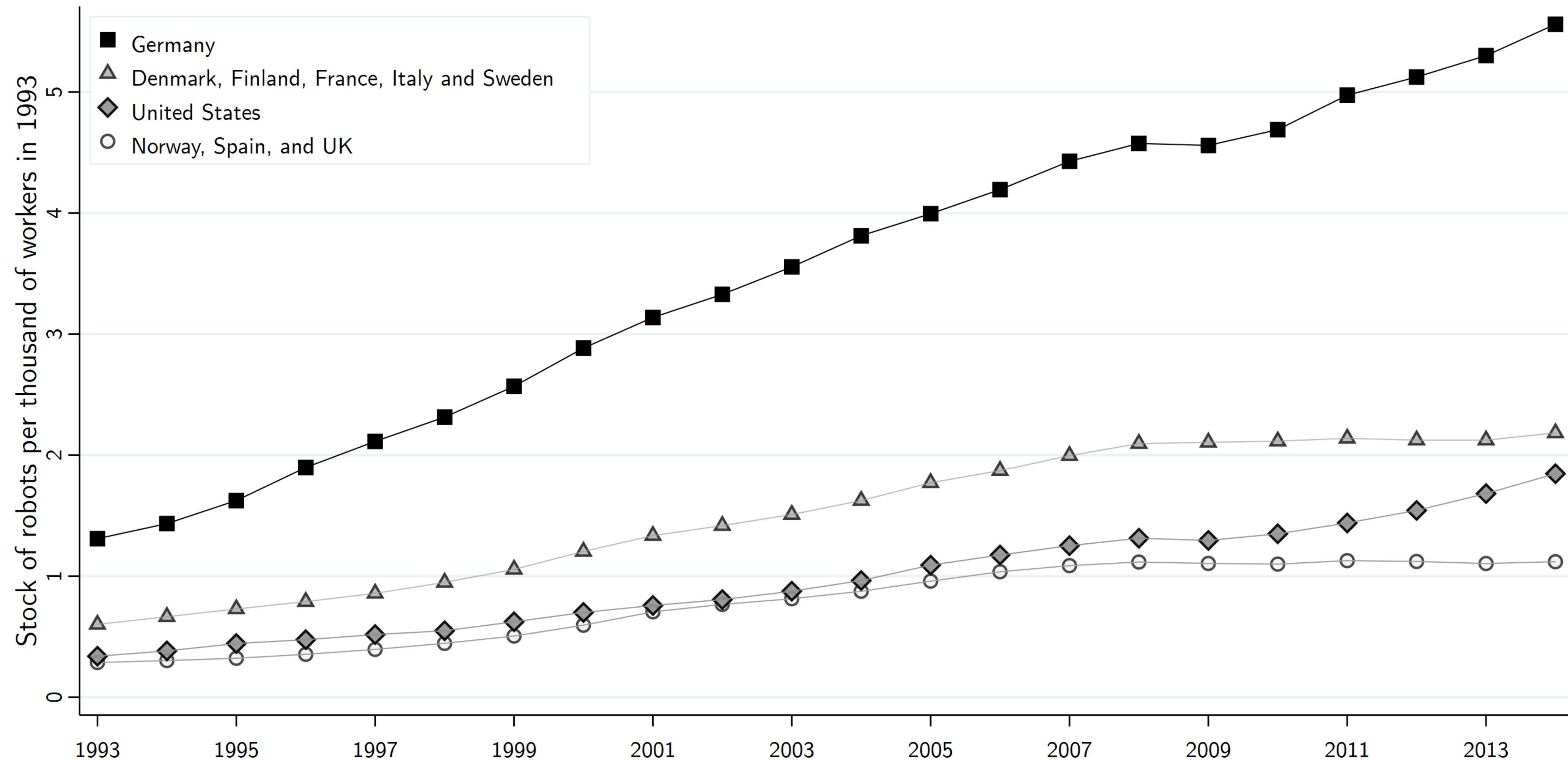
(i) raises skilled wage by 2%; (ii) reduces low skilled wage by 1%

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## **2. Automation and Industrial Robots**

### **– Acemoglu and Restrepo (2020)**

# Industrial Robots per Thousand Workers



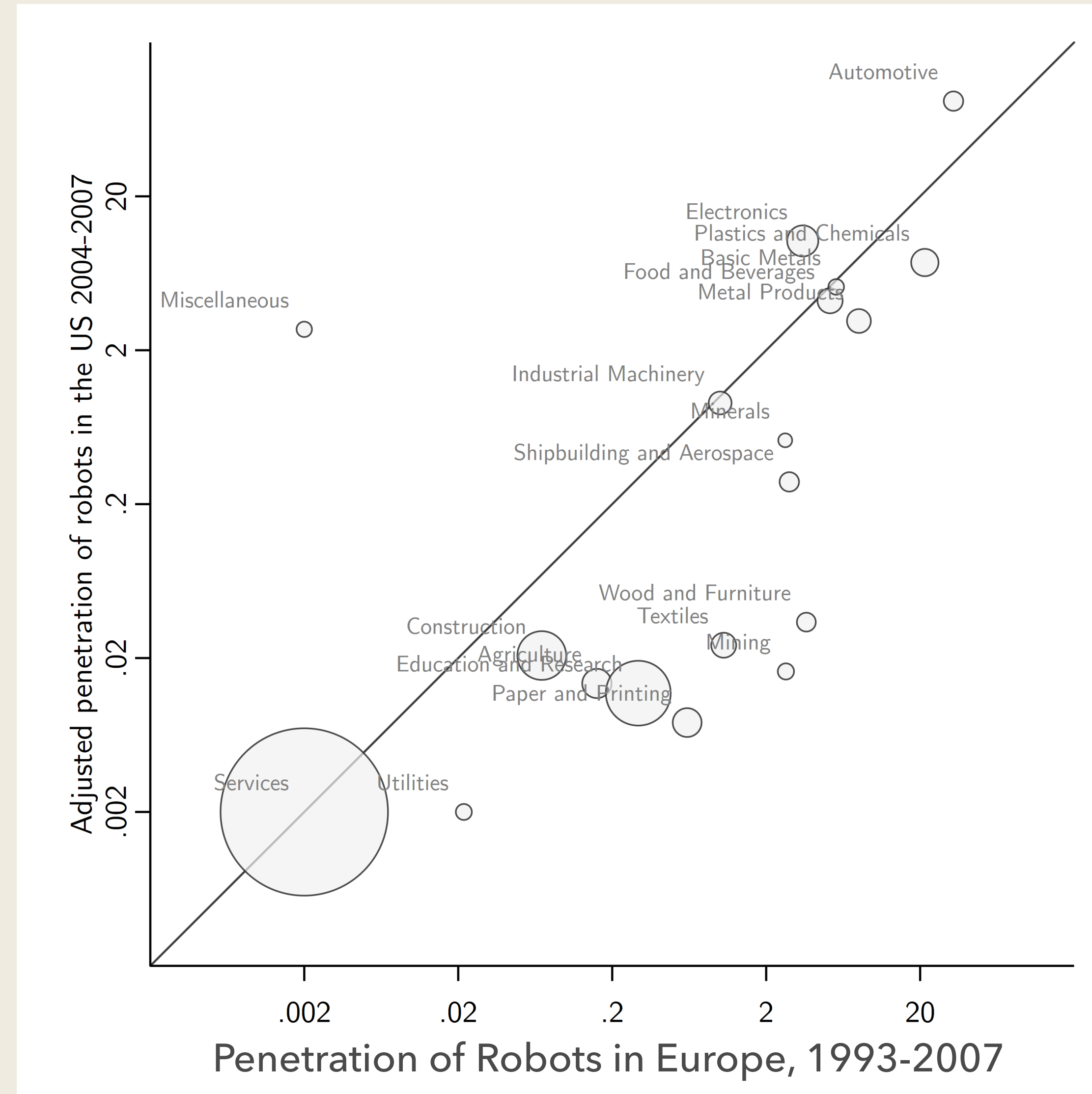
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# Robots and Jobs

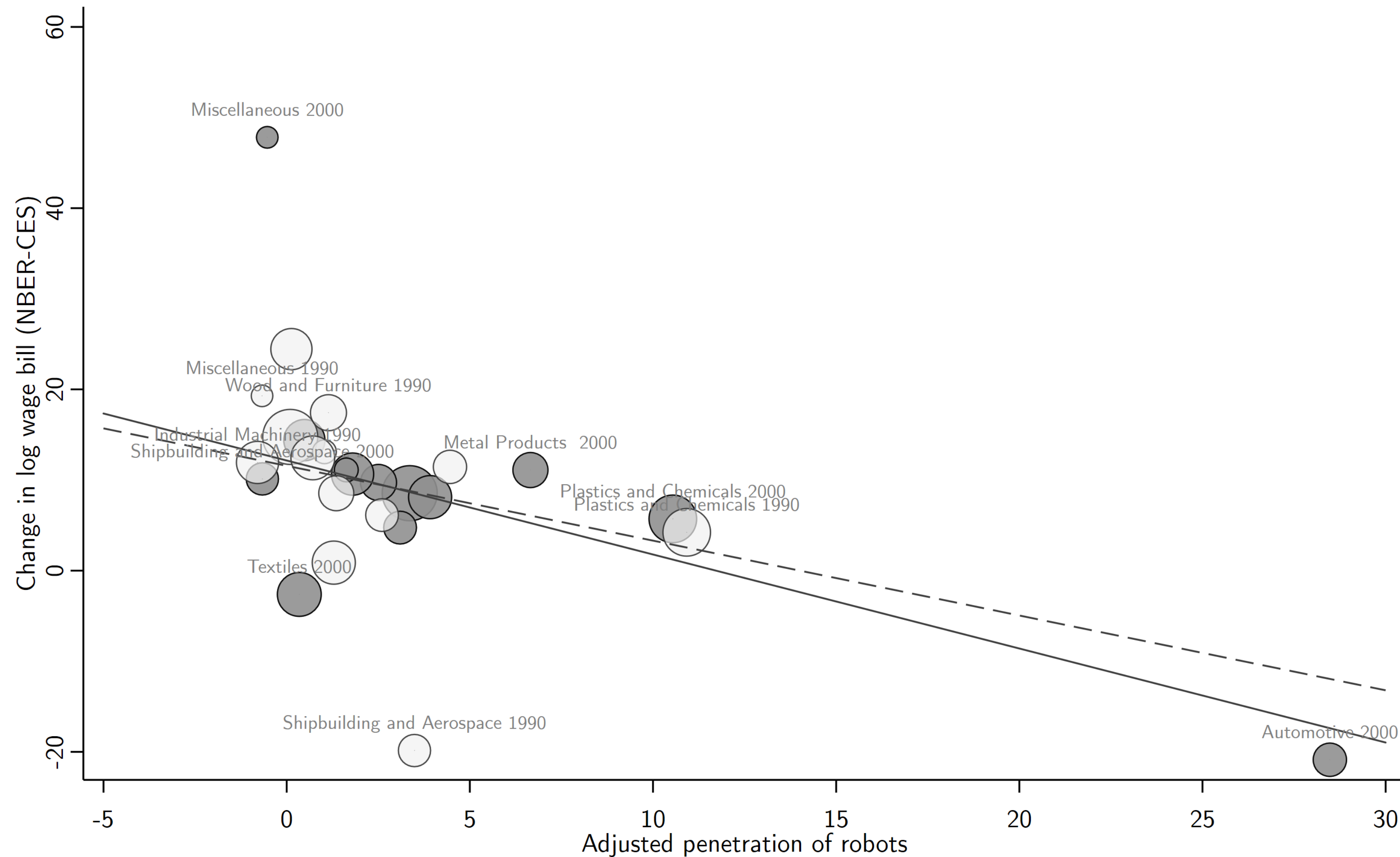
*Labor will become less and less important...More and more workers will be replaced by machines. I do not see that new industries can employ everybody who wants a job.*

– Wassily Leontief

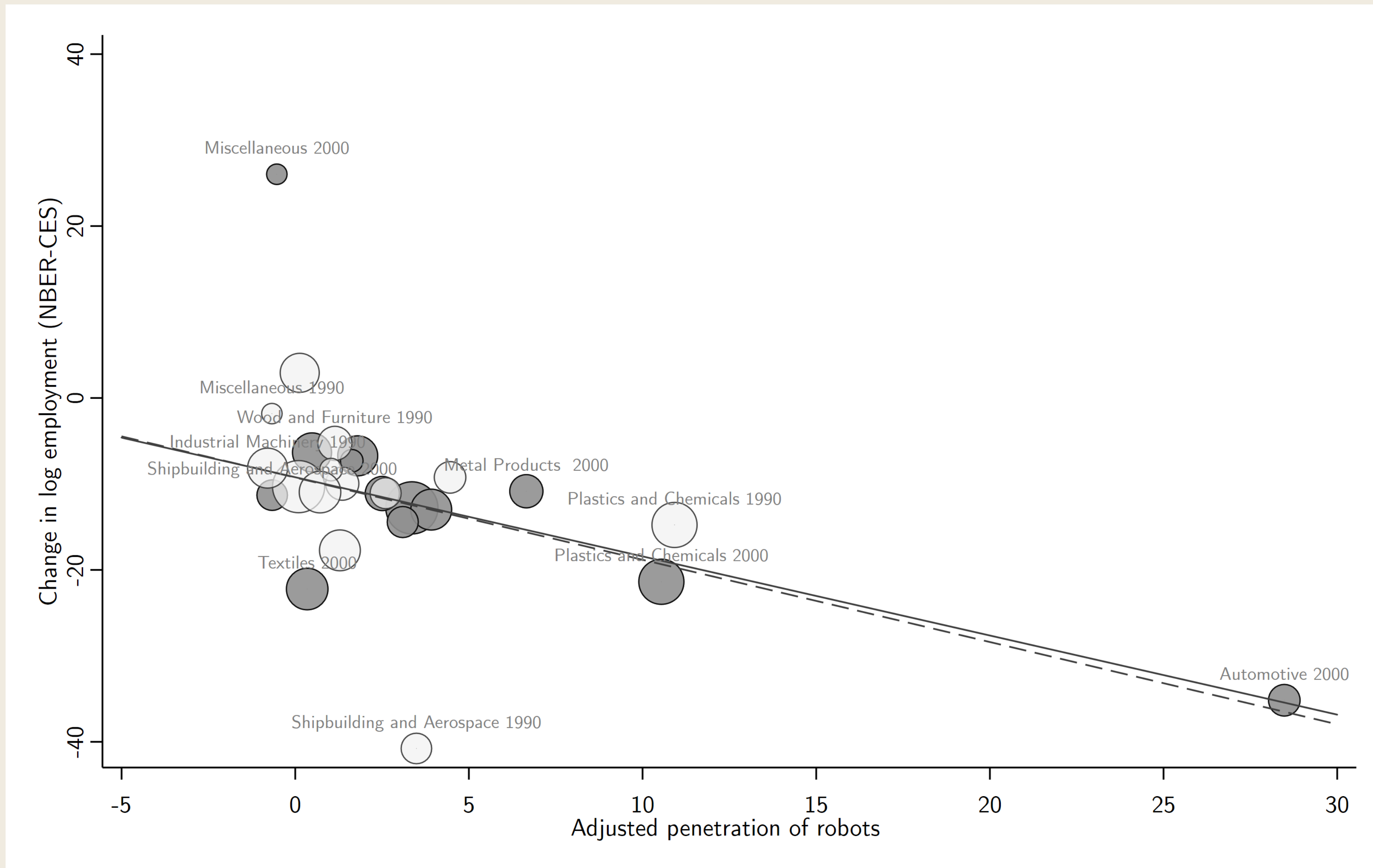
# Industry Variation



# Robot Penetration and Industry Wages



# Robot Penetration and Industry Employment



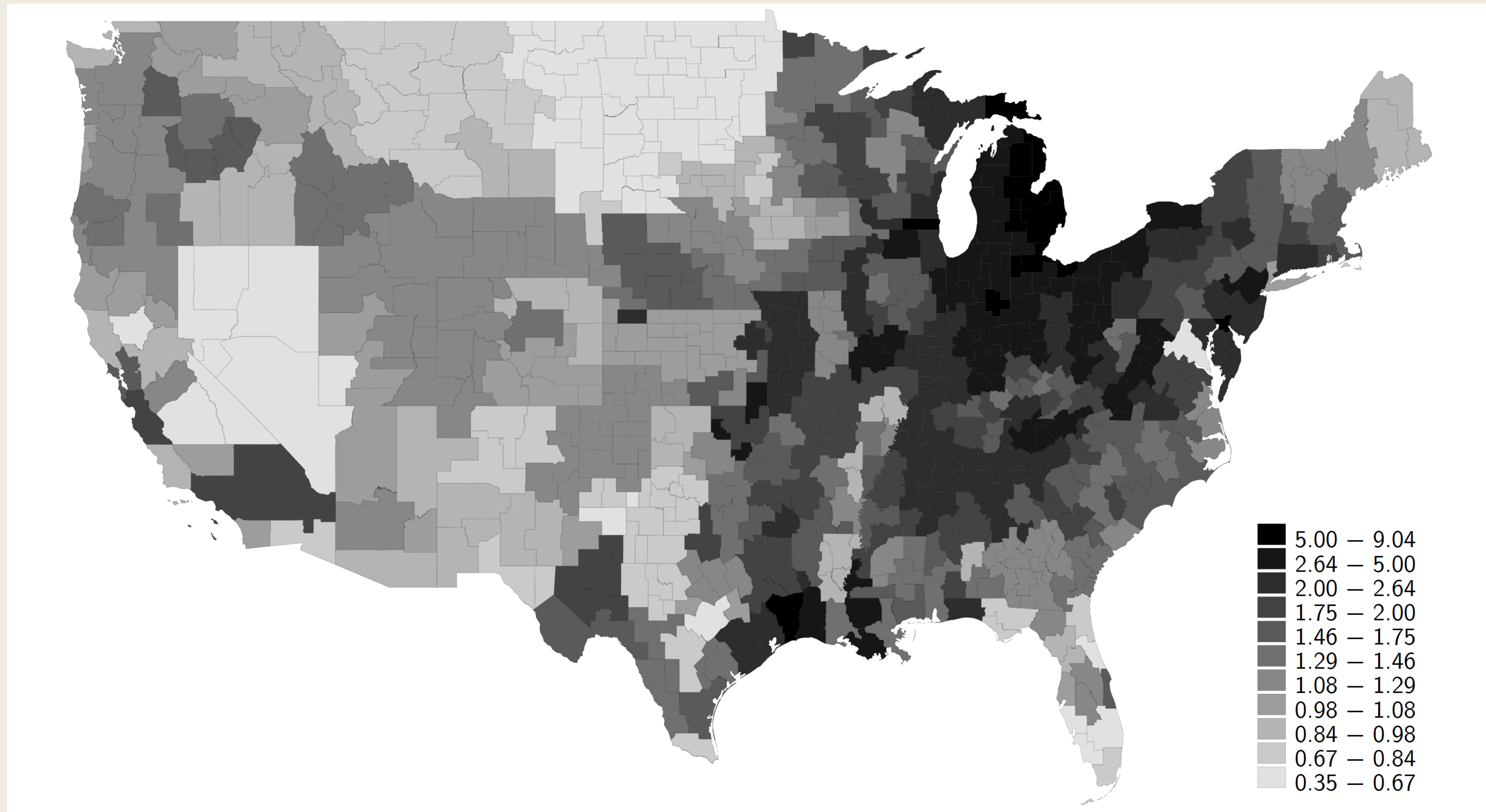


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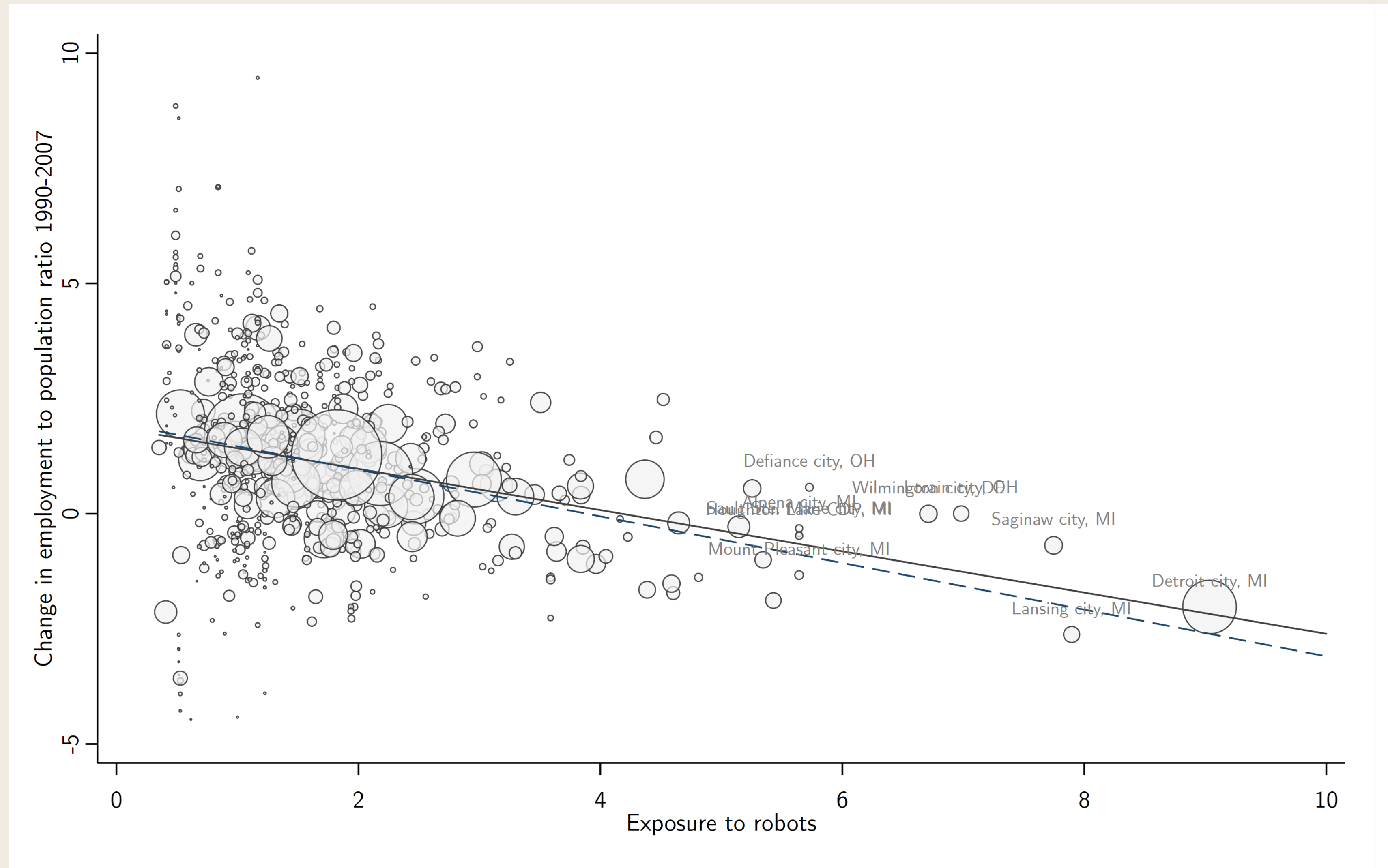
# Regional Exposure to Robots

- At the industry level, one more robot per thousand workers is associated with
  - a reduction in wages by 0.9%
  - a reduction in employment by 1.1%
  
- We now turn to regional analysis. Why regional?
  - It captures the local labor market *equilibrium* effect of automation
    - spillovers to people not working or leaving the directly affected industries
  
- US regions greatly differed in industry compositions
  - ⇒ they greatly differed also in exposures to robots

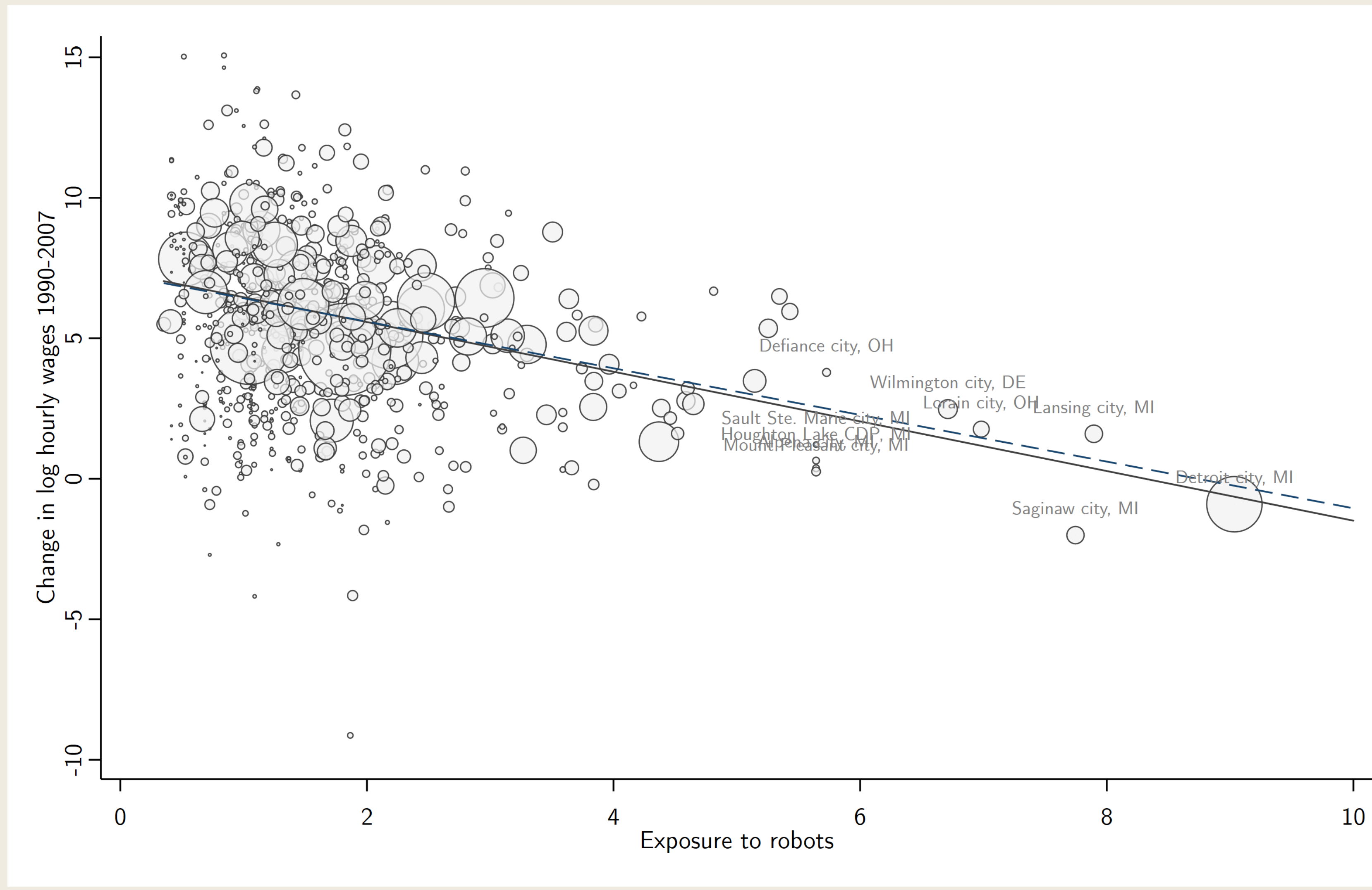
# Exposure to Robots



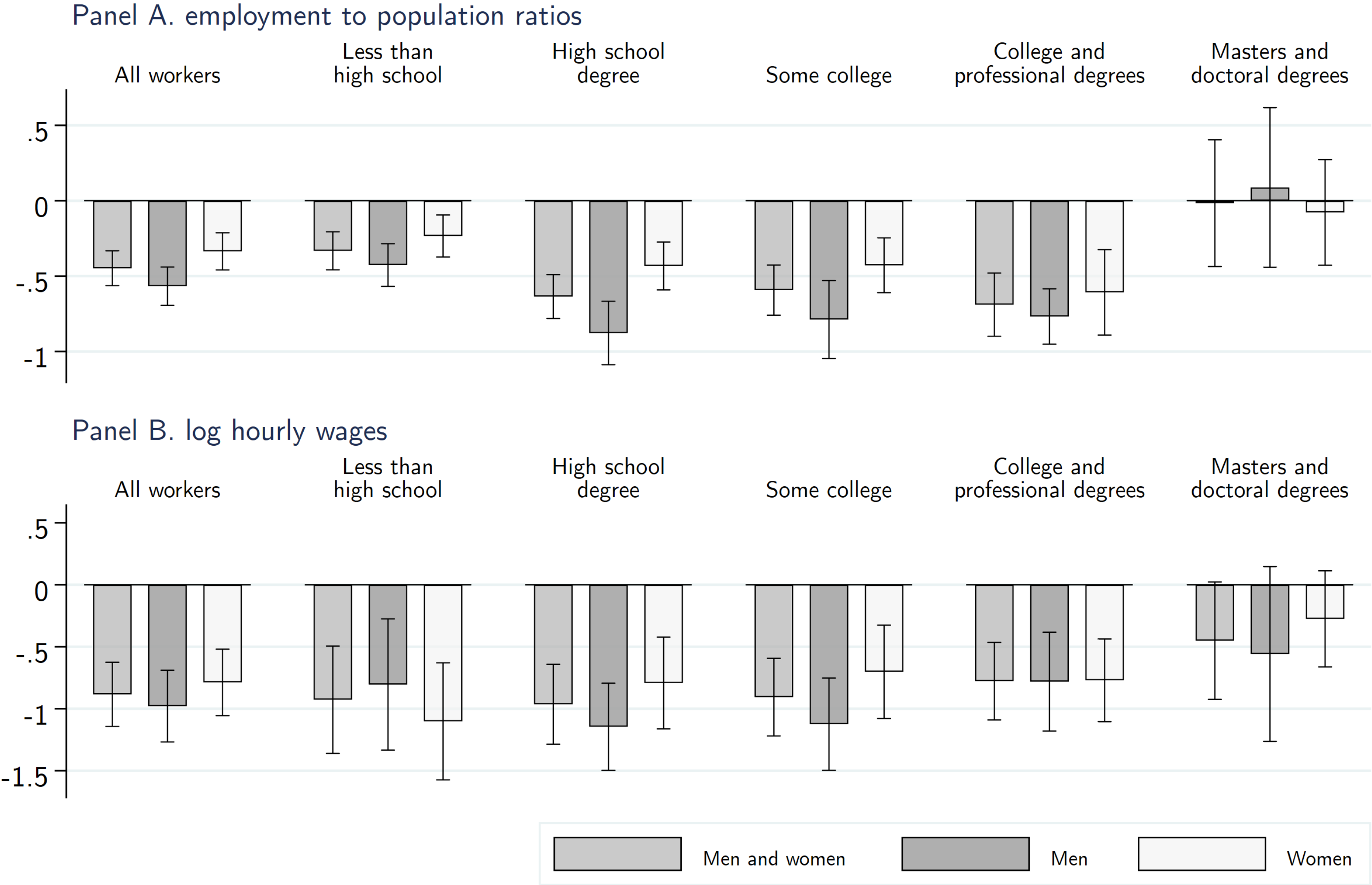
# Robots and Regional Employment



# Robots and Regional Wages



# Effect by Educational Groups





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# Quantitative Magnitude

- Robots per thousand workers increased by 1.5 in 1993-2014
- This implies
  - 0.3 p.p. decline in employment-to-population ratio
  - 0.42% decline in overall wages
- Robots reduce wages because they displace workers

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# Takeaway

- In order to explain the sharp rise in the wage inequality in the US,
  - Productivity of more-educated workers needs to be sharply rising
  - Productivity of less-educated workers needs to be falling
- What exactly are these “skill biased technological changes”? We looked at
  1. Internet
  2. Automation
- Technological advancement benefits the economy overall, but accrue unequally