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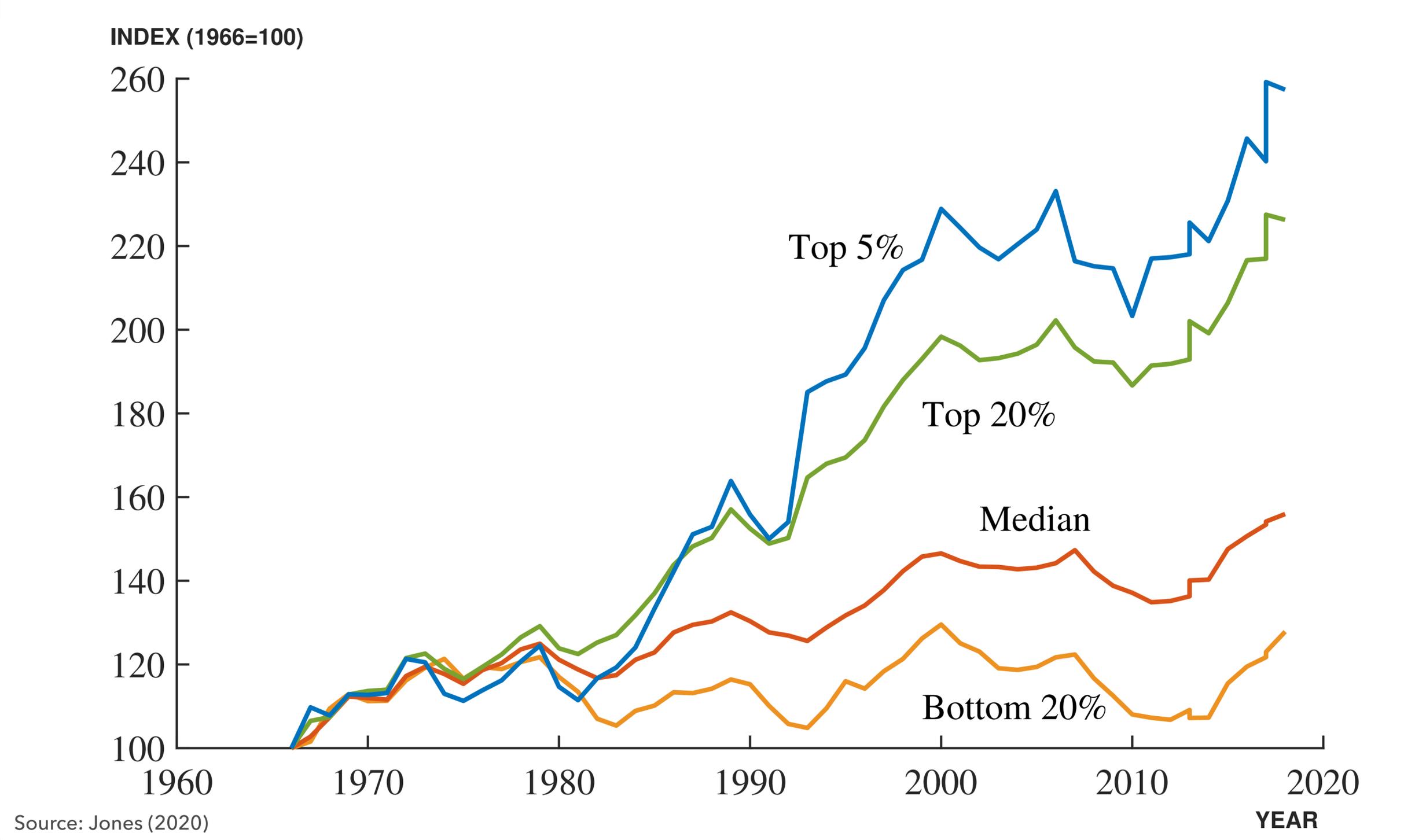
# Technological Change and Income Inequality

EC502 Macroeconomics  
Topic 6

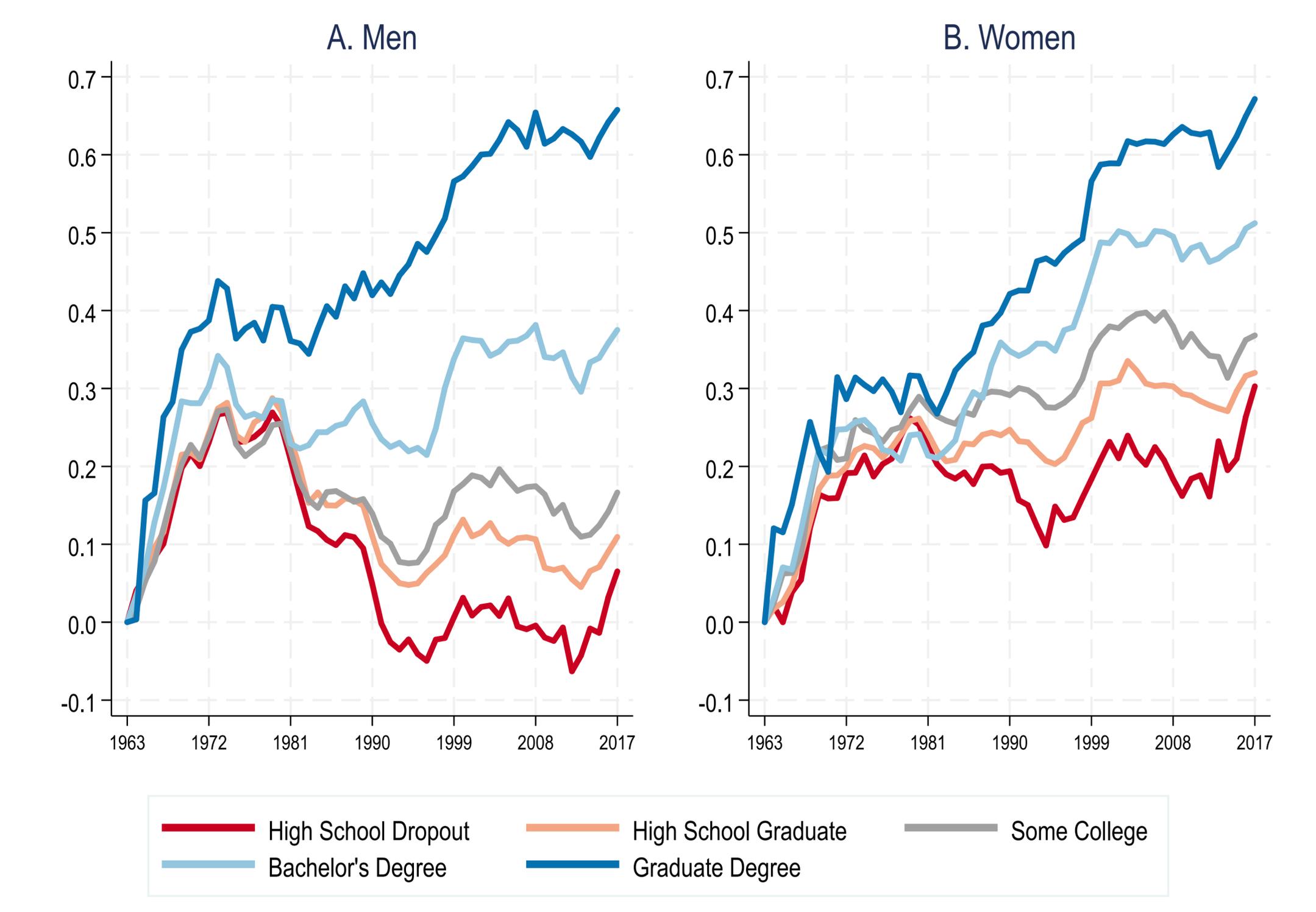
Masao Fukui

2026 Spring

# Growing Income Inequality in the US



# Rising Real Wage Inequality Across Educational Groups



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# **1. Skill-Biased Technological Change**

**– Katz and Murphy (1992)**

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# Production Function

- Firms use high- and low-skill labor to produce output:

$$Y = F(L_L, L_H)$$

- $L_L$ : low-skill labor
- $L_H$ : high-skill labor
- $F$ : constant returns to scale

- Assume:

$$F(L_L, L_H) = \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1 - \alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

- $A_L$ : low-skill augmenting technology,  $A_H$ : high-skill augmenting technology
- $\sigma > 0$ : elasticity of substitution between high- and low-skill labor

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# Three Special Cases

$$F(L_L, L_H) = \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1-\alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

1. If  $\sigma \rightarrow \infty$ , we have a linear production function:

$$F(L_L, L_H) = A_L L_L + A_H L_H$$

2. If  $\sigma = 1$ , we have a Cobb-Douglas production function:

$$F(L_L, L_H) = (A_L L_L)^\alpha (A_H L_H)^{1-\alpha}$$

3. If  $\sigma \rightarrow 0$ , we have a Leontief production function

$$F(L_L, L_H) = \min \left\{ \frac{1}{\alpha} A_L L_L, \frac{1}{1-\alpha} A_H L_H \right\}$$

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# Firm's Profit Maximization

- Firms take the wage of each skill group as given and decide how many to hire

$$\max_{L_L, L_H} F(L_L, L_H) - w_L L_L - w_H L_H$$

- First-order conditions:

$$\underbrace{\frac{\partial F(L_L, L_H)}{\partial L_L}}_{\text{MPL of low-skill labor}} = w_L$$

$$\underbrace{\frac{\partial F(L_L, L_H)}{\partial L_H}}_{\text{MPL of high-skill labor}} = w_H$$

- Assume  $L_H$  and  $L_L$  are exogenous

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# Labor Demand

- With our functional form,

$$w_L = \alpha^{\frac{1}{\sigma}} A_L^{\frac{\sigma-1}{\sigma}} (L_L)^{-\frac{1}{\sigma}} \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1-\alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

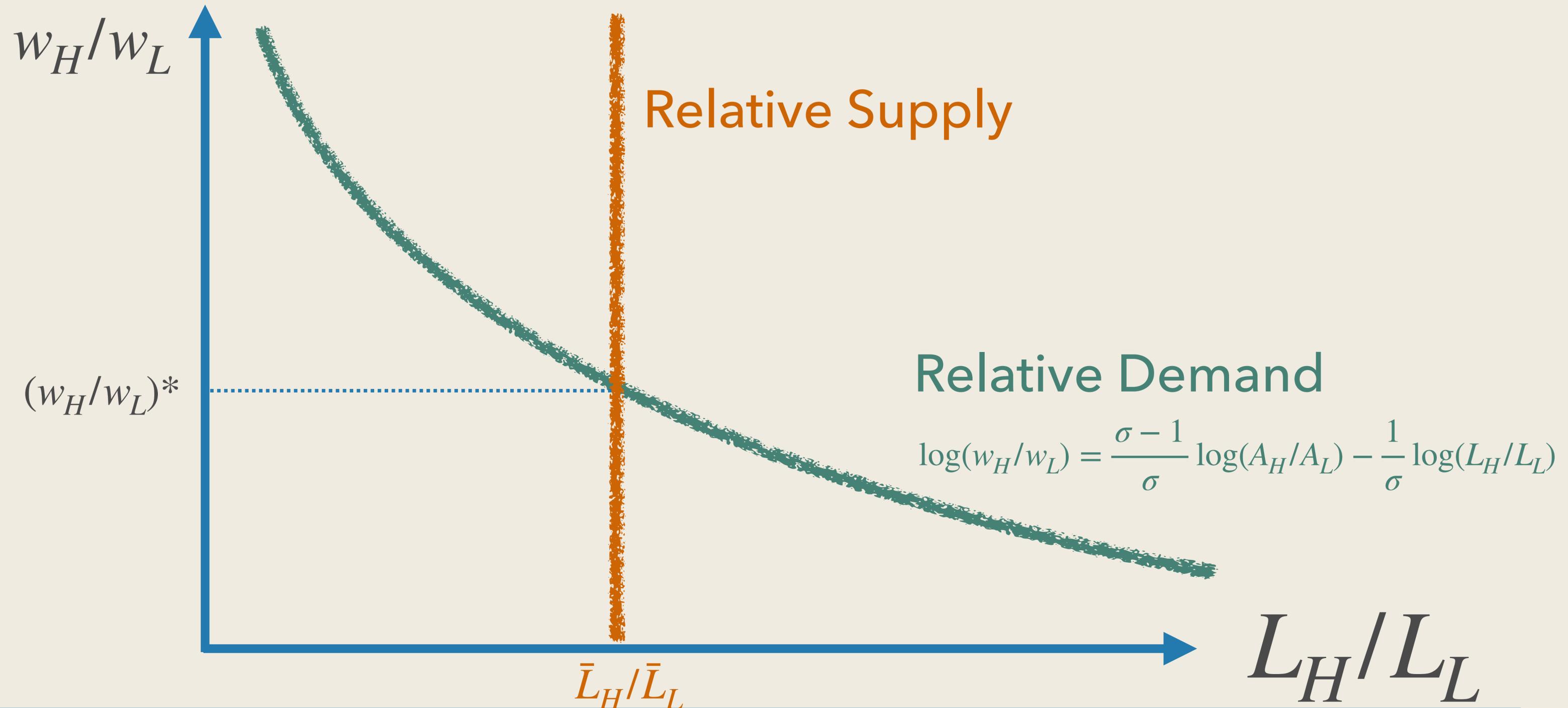
$$w_H = (1-\alpha)^{\frac{1}{\sigma}} A_H^{\frac{\sigma-1}{\sigma}} (L_H)^{-\frac{1}{\sigma}} \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1-\alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

- Taking the ratio, relative labor demand,  $L_H/L_L$ , is

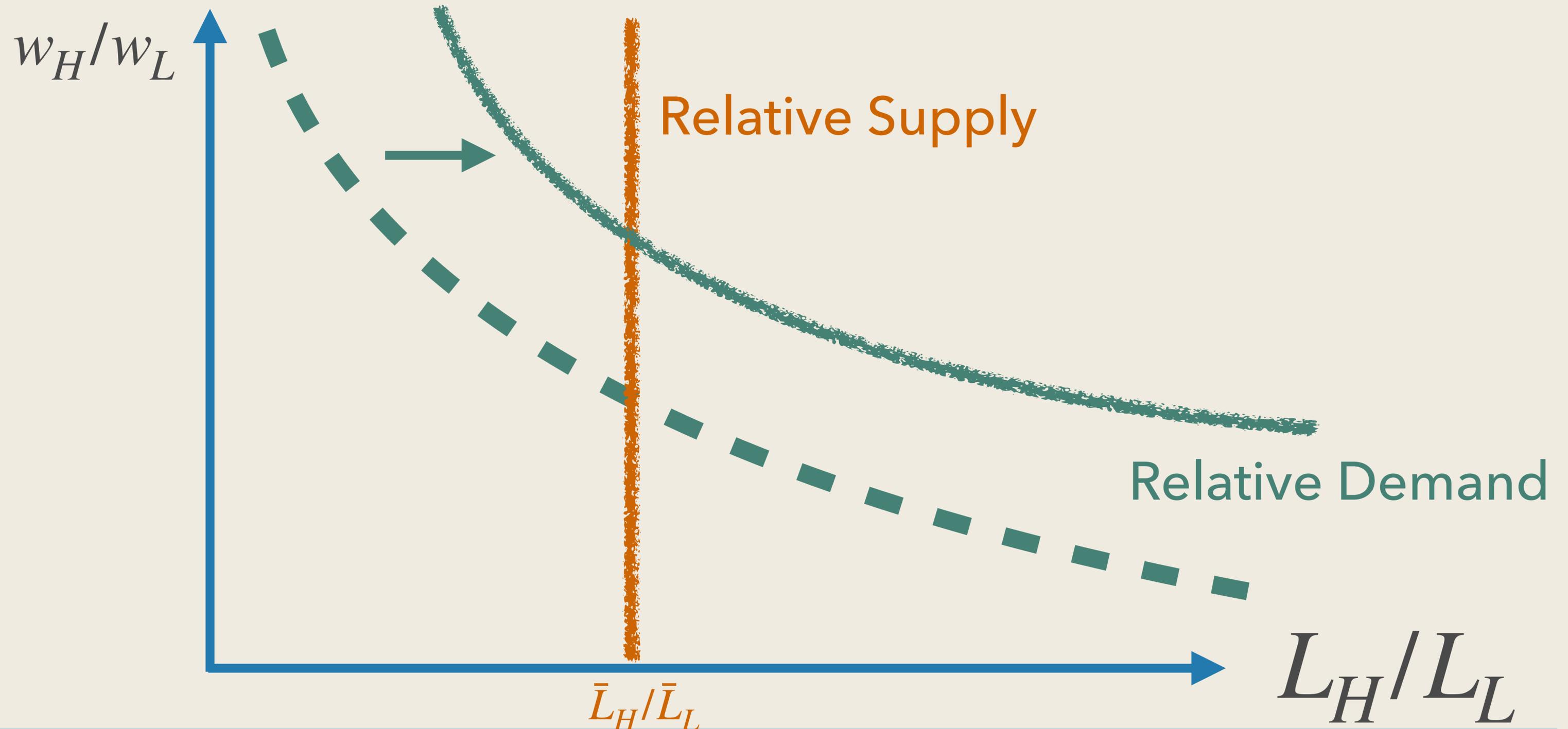
$$\log(L_H/L_L) = (\sigma - 1)\log(A_H/A_L) - \sigma \log(w_H/w_L) + \log((1 - \alpha)/\alpha)$$

- A rise in  $A_H$  relative to  $A_L$ 
  - raises relative labor demand for skilled if  $\sigma > 1$  (substitutes).
  - lowers relative labor demand for skilled if  $\sigma < 1$  (complements)

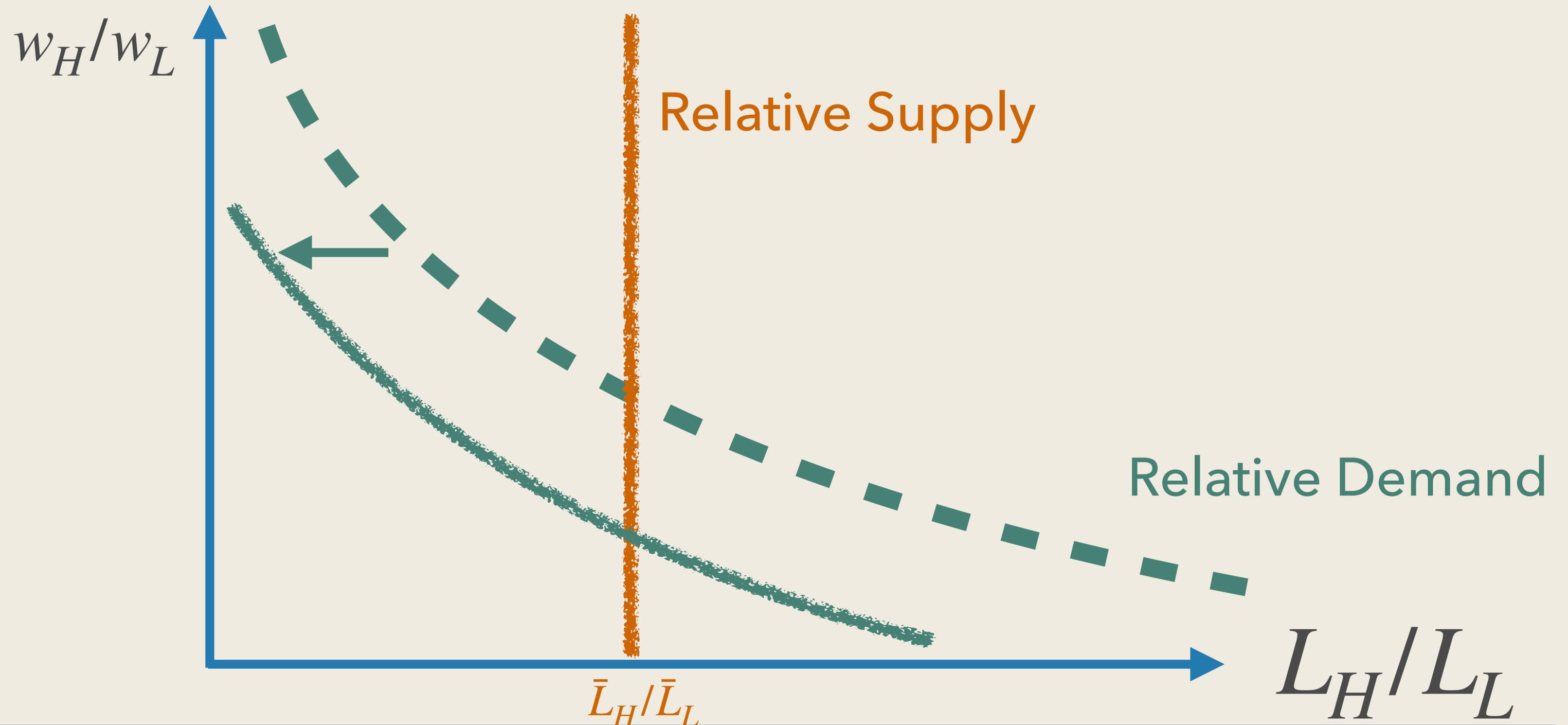
# Demand and Supply



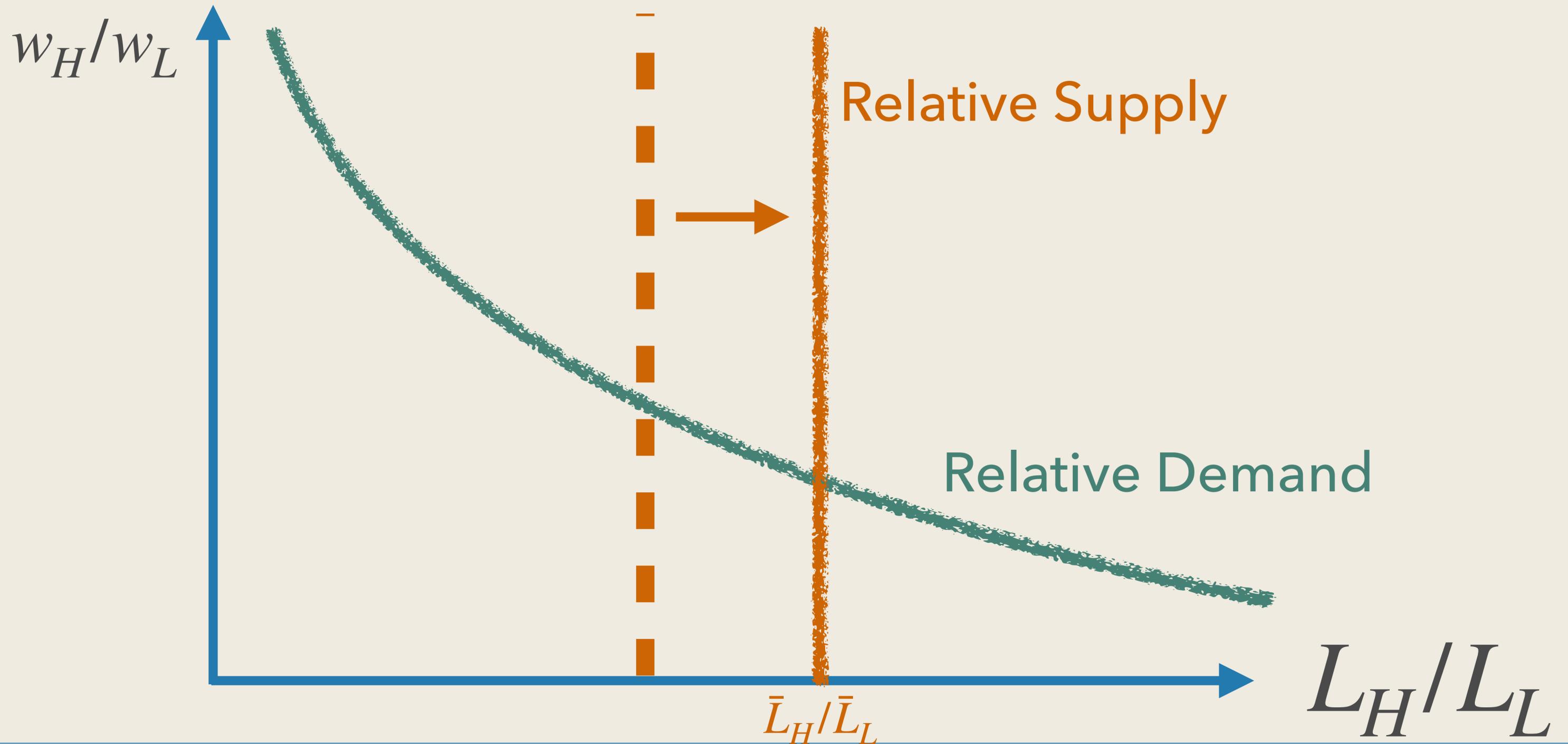
# Increase in $A_H/A_L$ if $\sigma > 1$



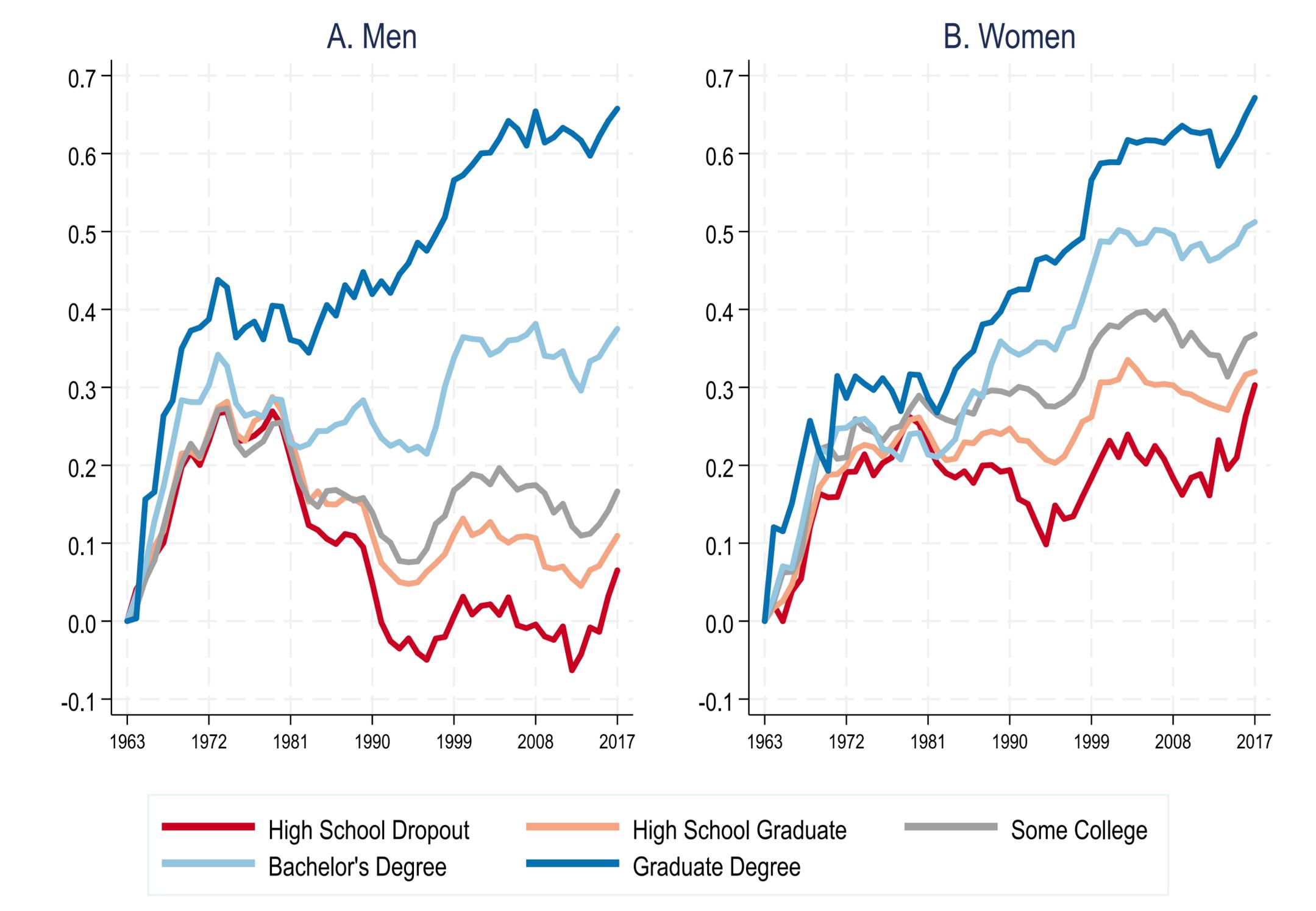
# Increase in $A_H/A_L$ if $\sigma < 1$



# Increase in $\bar{L}_H/\bar{L}_L$

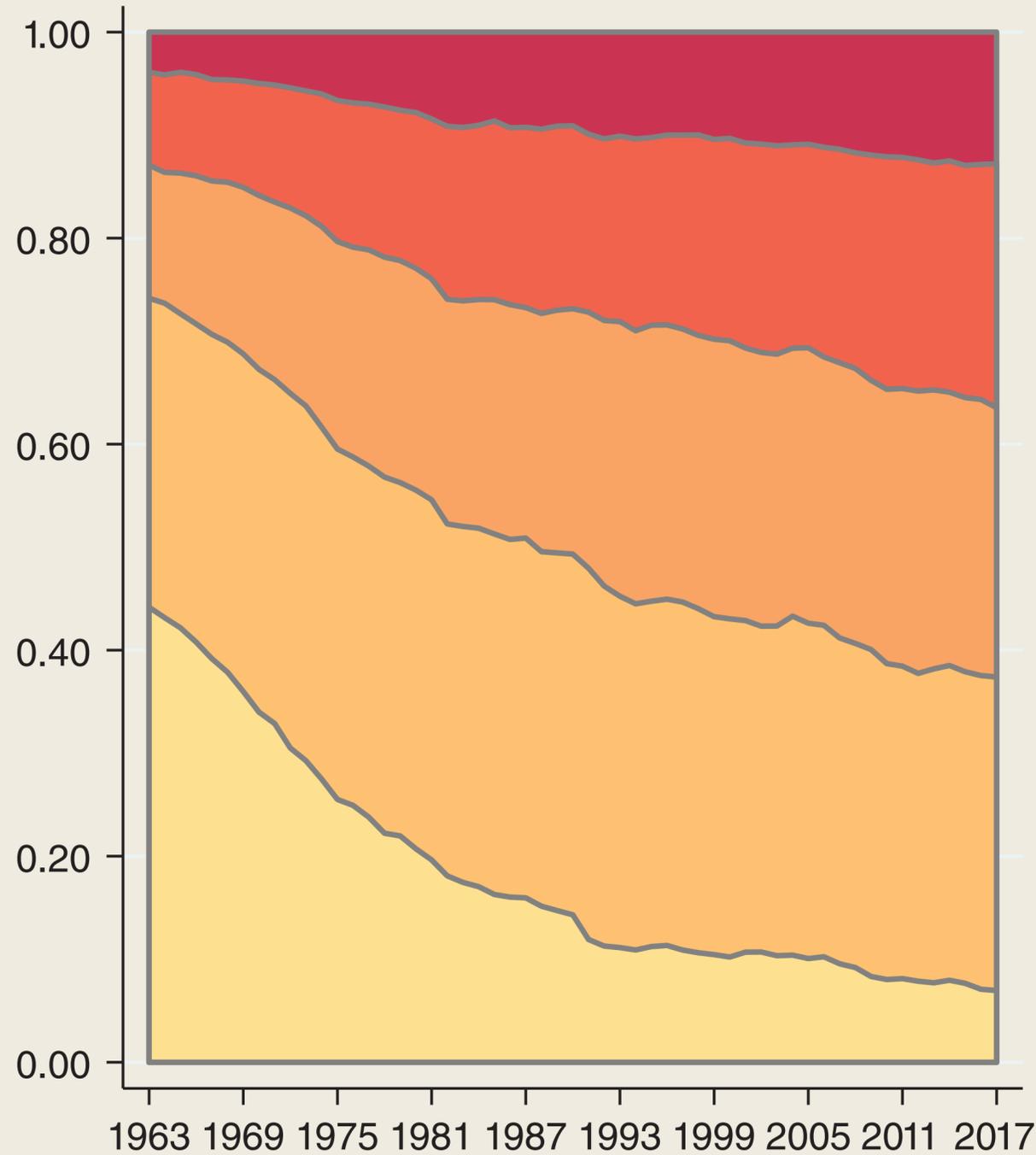


# Rising Real Wage Inequality Across Educational Groups

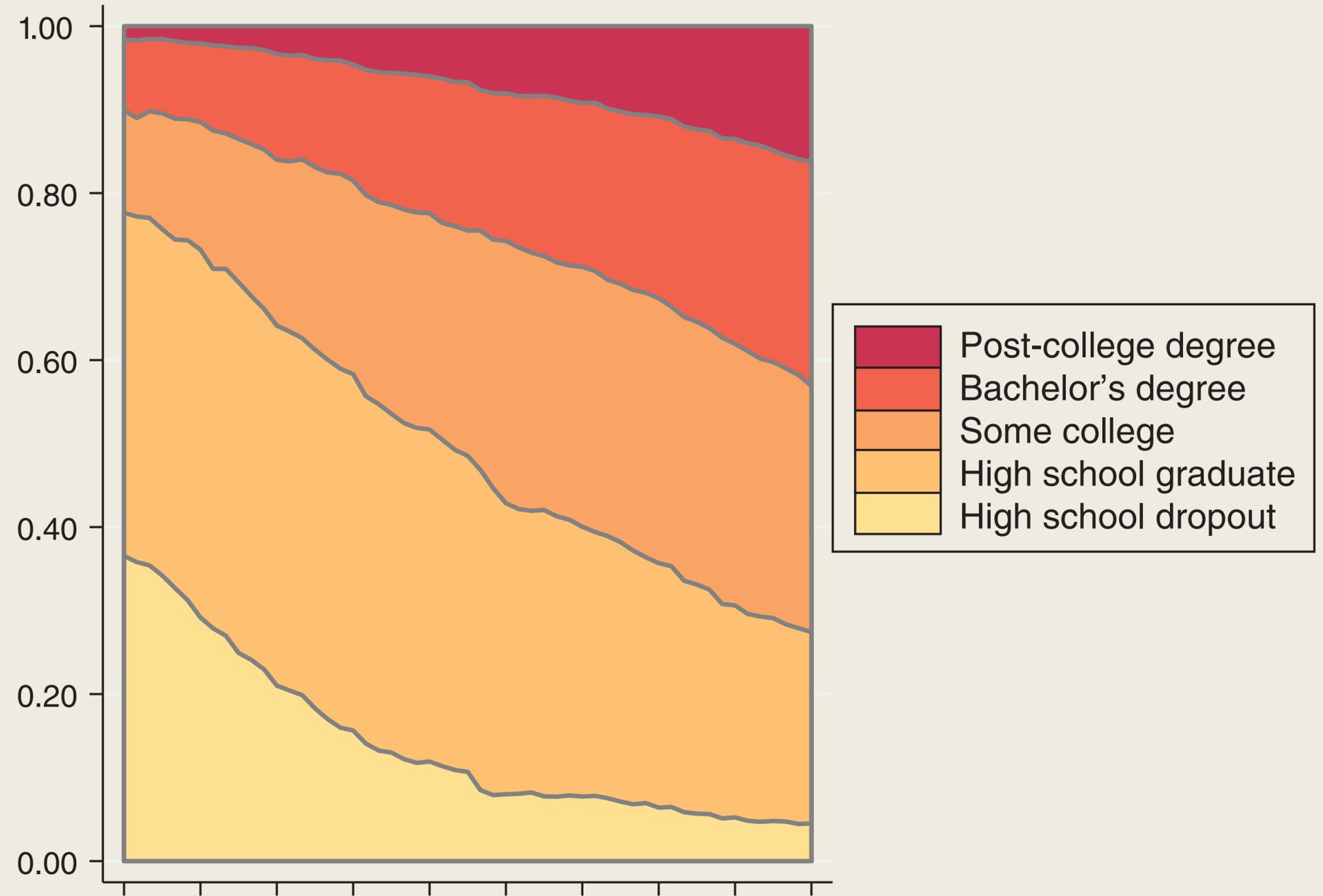


# Hours Worked Share

Panel A. Men



Panel B. Women



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# What Has Happened?

$$\log(w_H/w_L) = \frac{\sigma - 1}{\sigma} \log(A_H/A_L) - \frac{1}{\sigma} \log(L_H/L_L) + \log((1 - \alpha)/\alpha)$$

**Went up!**

**Went up!**

- What needs to have happened to  $A_H/A_L$  in the past?
- If  $\sigma > 1$ ,  $A_H/A_L$  must have been rising (**skill-biased technical change**)
- The consensus among macroeconomists is that  $\sigma > 1$

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# Inferring $A_H$ and $A_L$

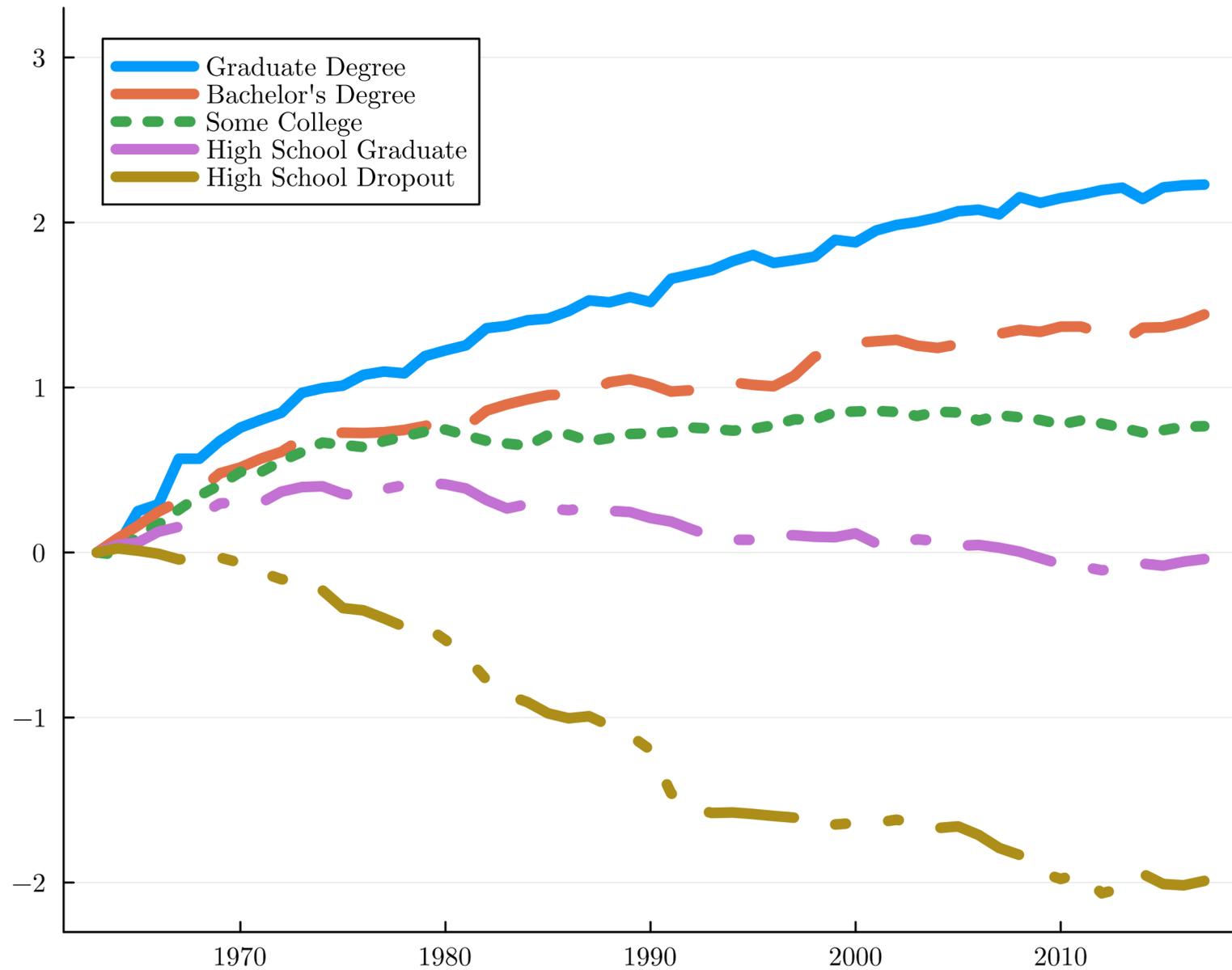
$$w_L = \alpha^{\frac{1}{\sigma}} A_L^{\frac{\sigma-1}{\sigma}} (L_L)^{-\frac{1}{\sigma}} \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1-\alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

$$w_H = (1-\alpha)^{\frac{1}{\sigma}} A_H^{\frac{\sigma-1}{\sigma}} (L_H)^{-\frac{1}{\sigma}} \left( \alpha^{\frac{1}{\sigma}} (A_L L_L)^{\frac{\sigma-1}{\sigma}} + (1-\alpha)^{\frac{1}{\sigma}} (A_H L_H)^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}}$$

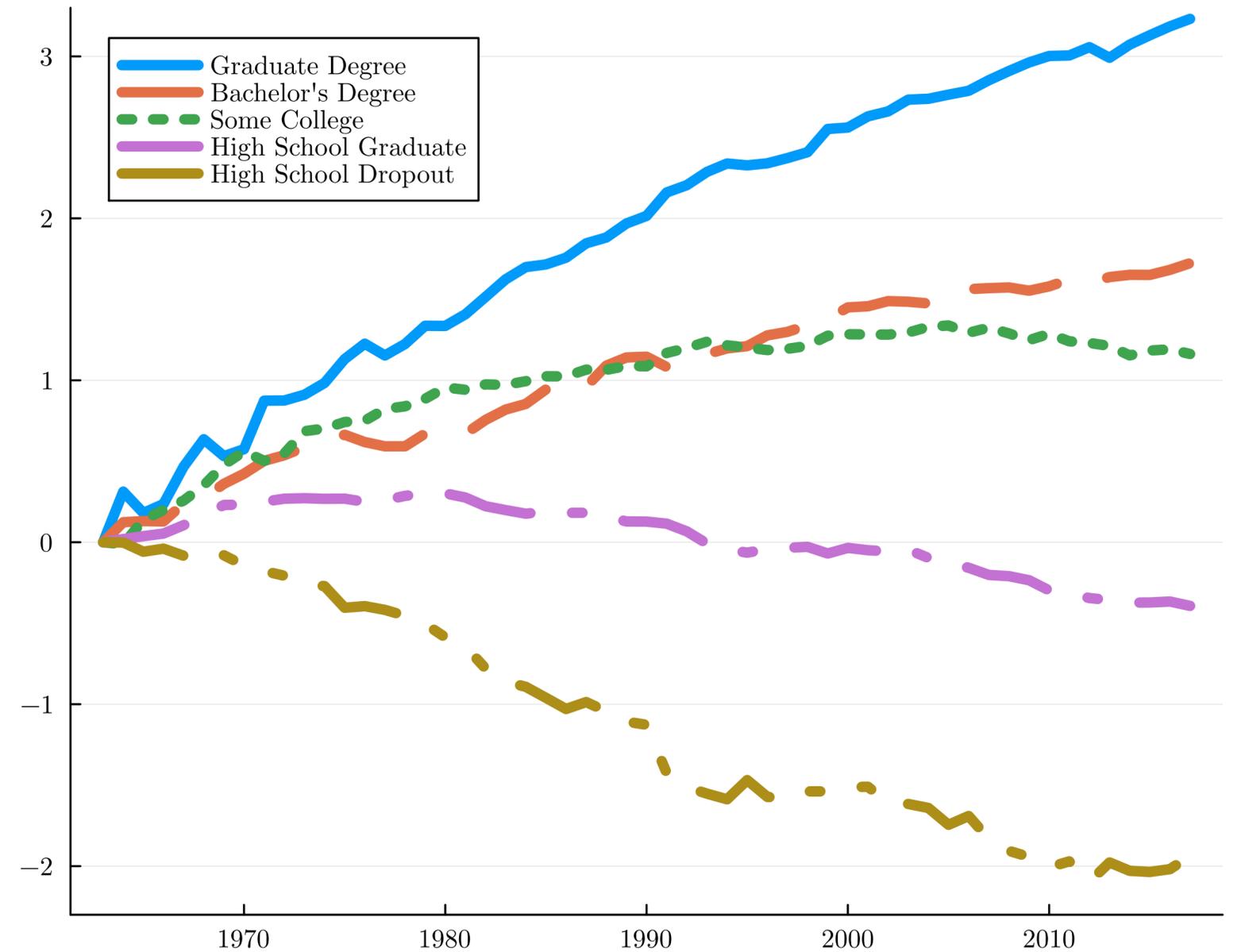
- Suppose we know  $\sigma$  (around  $\sigma \in [2,5]$ ) and fix  $\alpha$
- We observe  $(L_H, L_L)$  and  $(w_H, w_L)$  in the data
- We can reverse-engineer  $(A_H, A_L)$  in the data
  - Just as in how we constructed aggregate TFP (Solow residual)
  - Now each for different groups of people!
- Implement with more than two skill groups:
  - post-college, college, some college, high-school, high-school dropout

# Inferred $A$ with $\sigma = 2$

Inferred  $A$  for Men (in log)

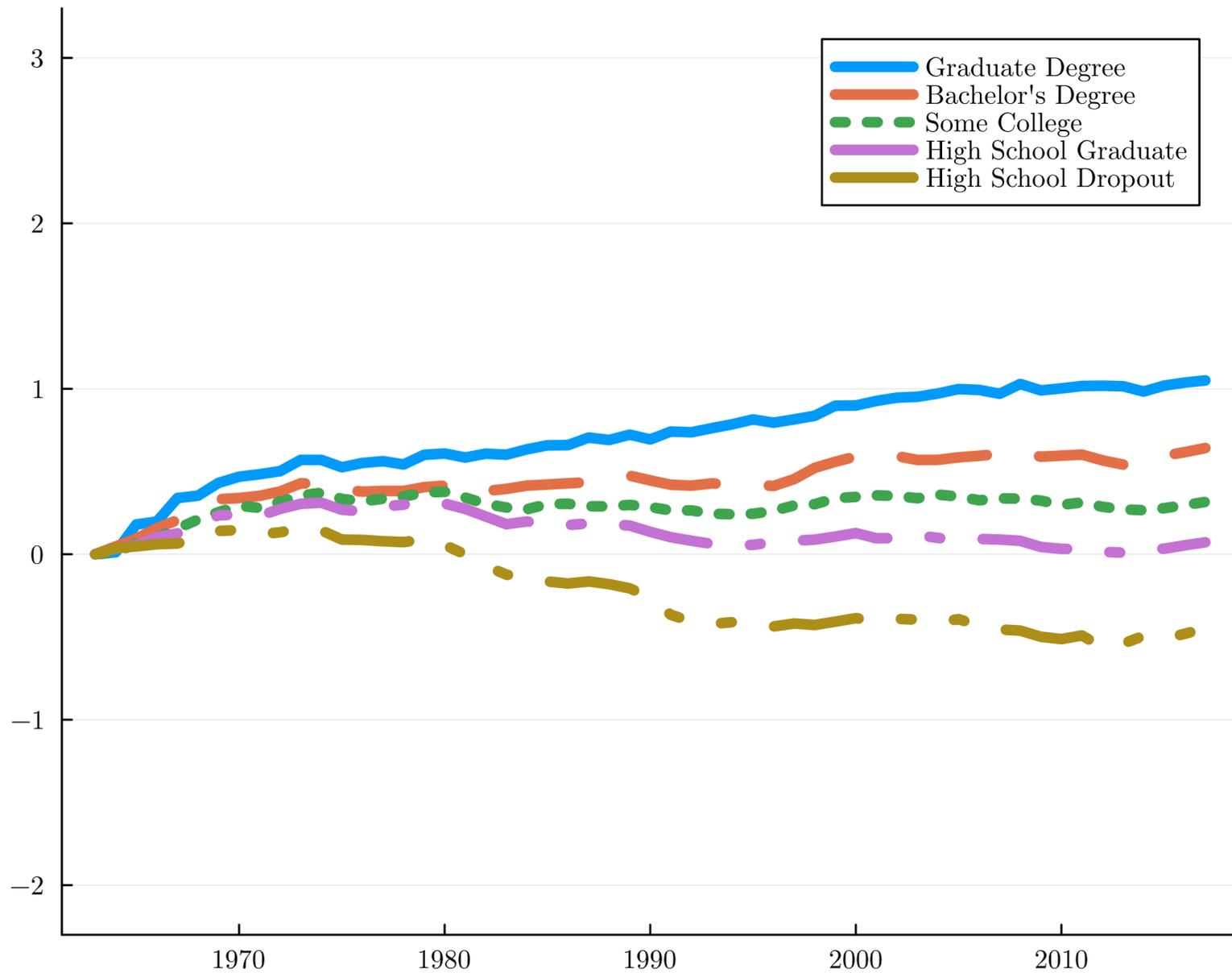


Inferred  $A$  for Women (in log)

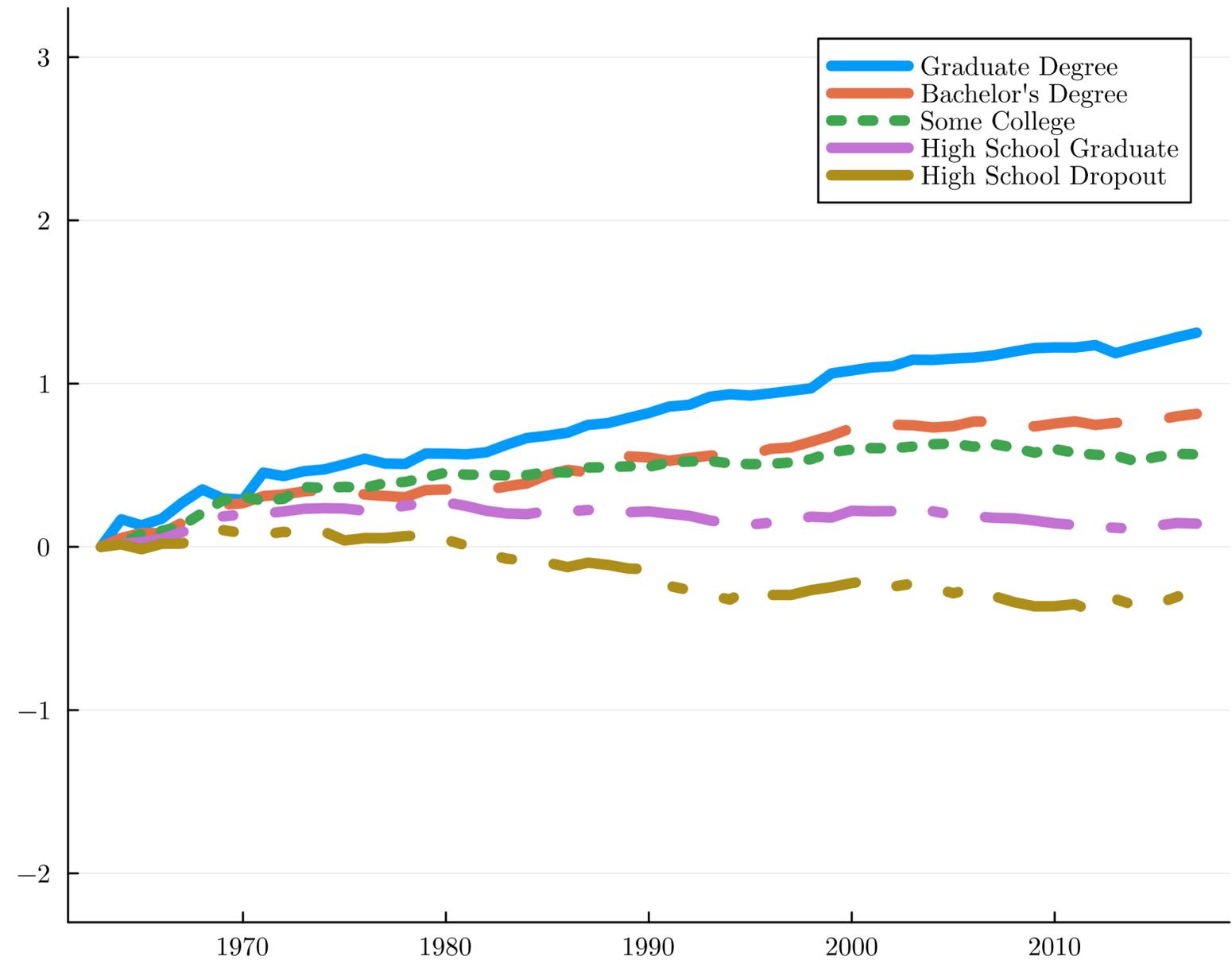


# Inferred $A$ with $\sigma = 5$

Inferred  $A$  for Men (in log)



Inferred  $A$  for Women (in log)



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# Takeaway

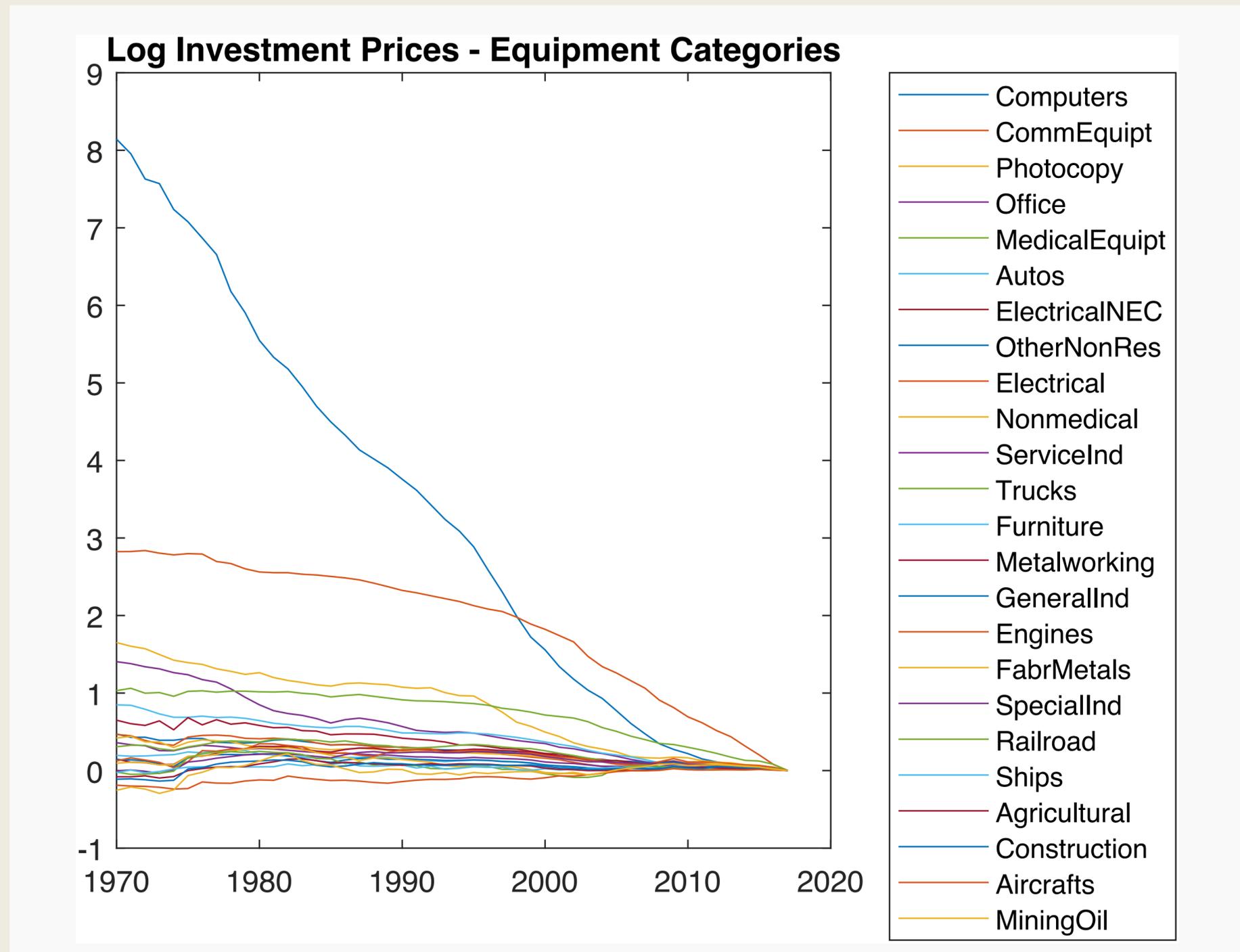
- Productivity of more educated groups sharply increasing over time
  - 50-300% **increase** during 1962-2017
- Productivity of less educated groups sharply declining over time
  - 50-250% **decrease** during 1962-2017
- We infer a substantial degree of “skill-biased technological change”
- What exactly are these technological changes?

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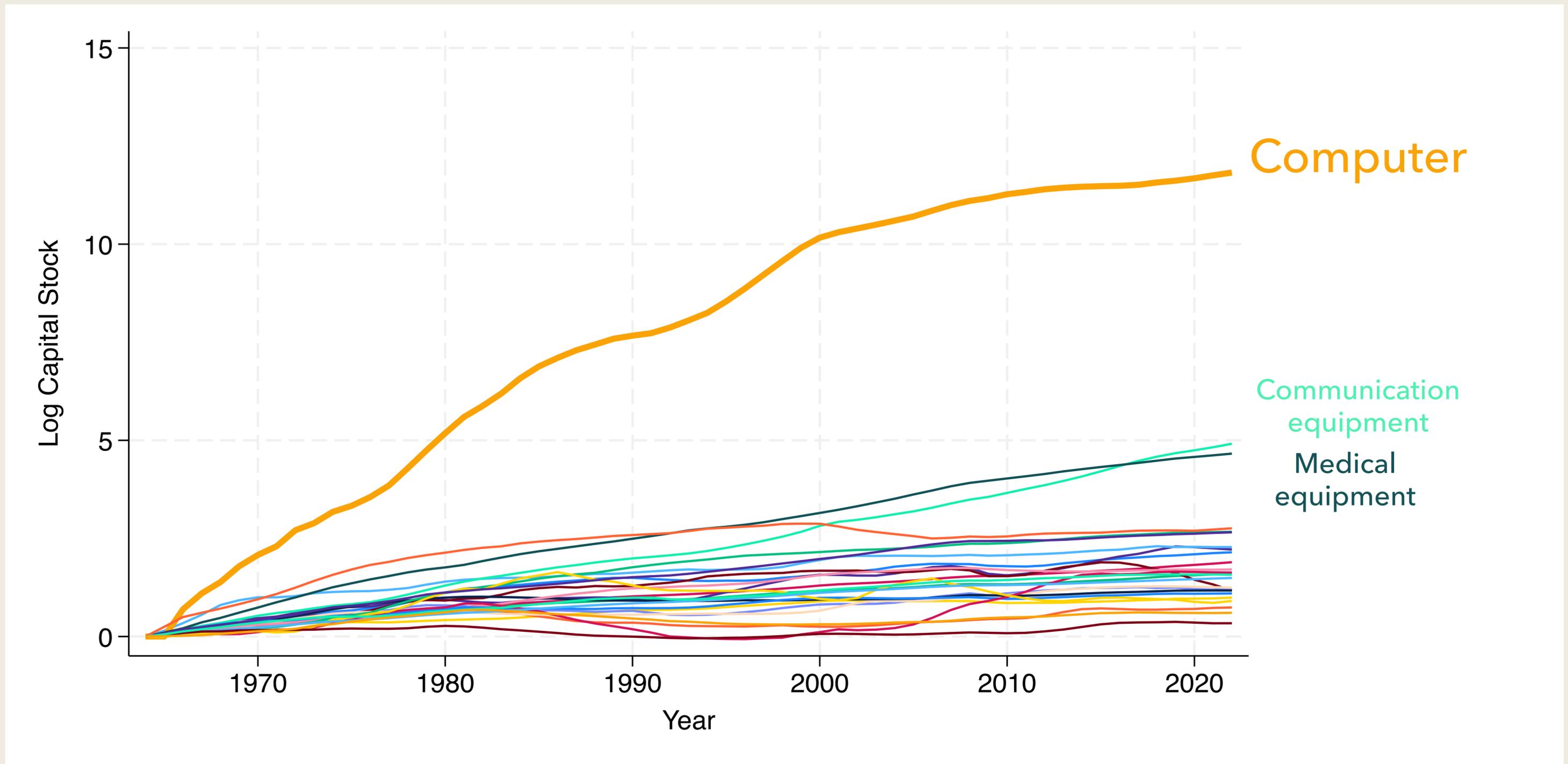
# **Empirical Evidence of the Skill-Biased Technological Change**

**– Akerman, Gaarder & Mogstad (2015)**

# Declining ICT Equipment Prices



# Surge in ICT Capital Stock



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# Question

- How do the recent advancements in IC technology affect inequality?
- Setup: Norway 2001-2007
- Institutional background: National Broadband Policy
  - Goal: nationwide broadband access at uniform pricing
  - Means: infrastructure investments, local gov't mandates
- 428 municipalities differed in the timing of the rollout of broadband internet
  - compare municipality with early rollout to the late rollout
- Skill groups: (i) skill (college); (ii) medium (high-school); (iii) low (less than high-school)

# Broadband Internet Availability in Norway

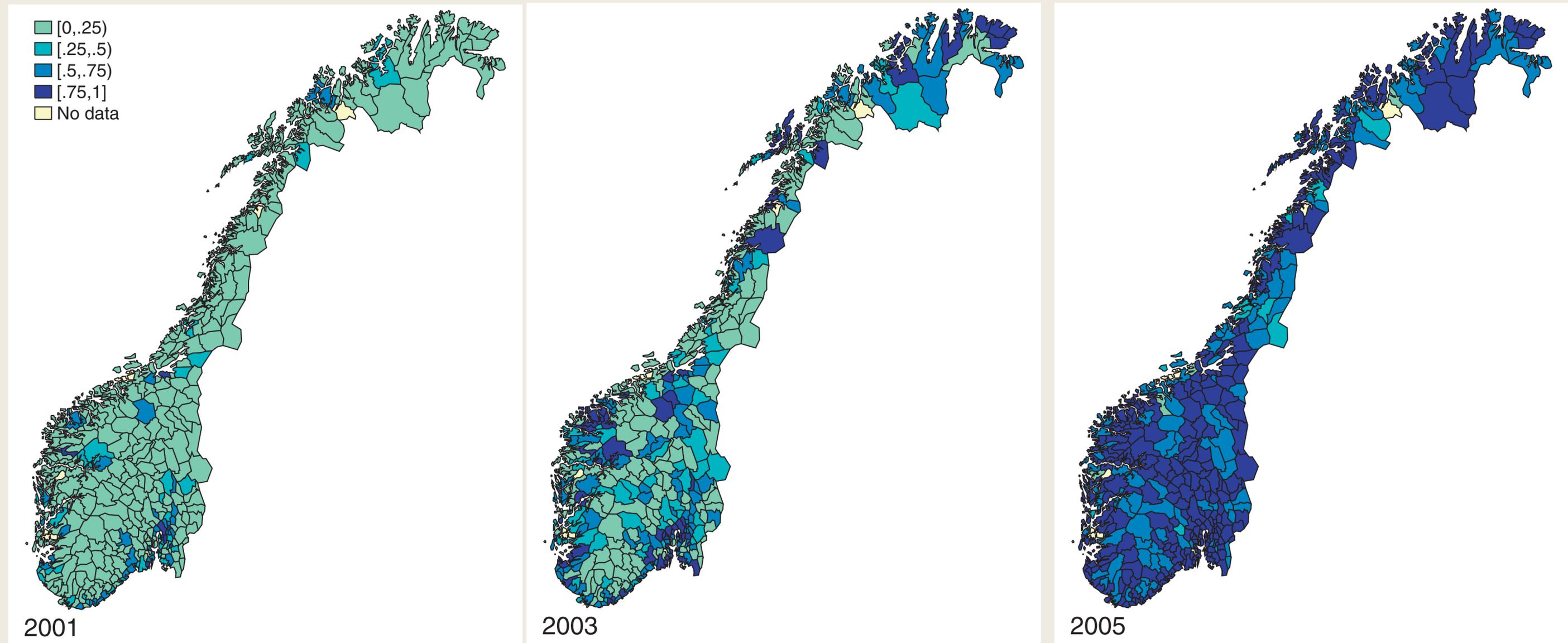


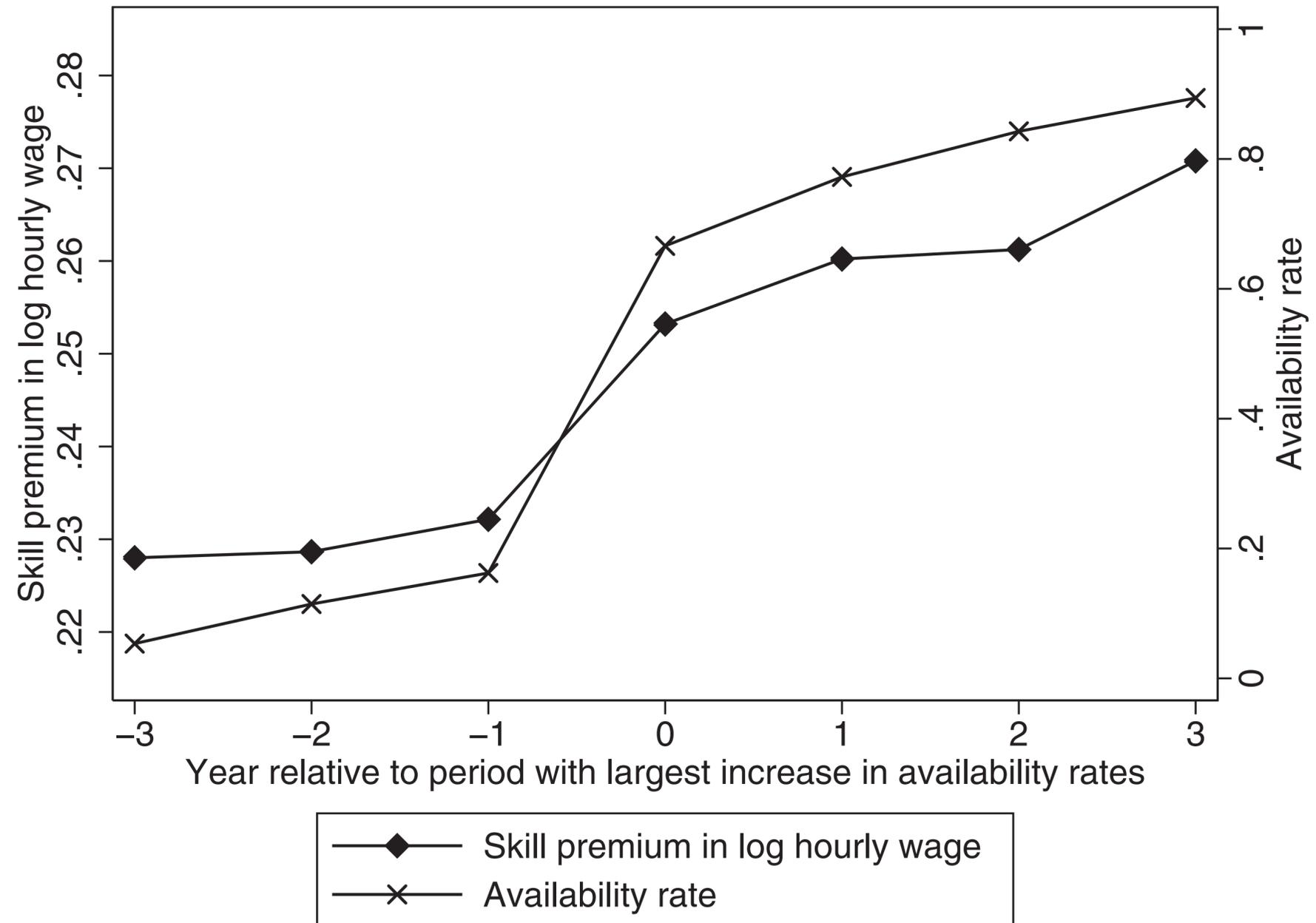
FIGURE I

Geographical Distribution of Broadband Availability Rates

The graphs show the geographical distribution of broadband availability rates of households in 2001, 2003, and 2005.

# Impact of the Broadband Internet on Skill Premium

(c) Return to Skill: Hourly wage



# Impact on Wages and Employment

Dependent variable	(1)	(2)	(3)	(4)
	Log hourly wage		Employment	
	2 skills	3 skills	2 skills	3 skills
Availability × Unskilled	-0.00622 (0.00455)		0.000794 (0.00252)	
Low skilled		-0.0108*** (0.00325)		-0.00392 (0.00244)
Medium skilled		-0.00793 (0.00600)		0.00388 (0.00281)
Skilled	0.0178** (0.00720)	0.0202*** (0.00692)	0.0208** (0.00920)	0.0225** (0.00892)
Worker-year observations	8,759,388	8,759,388	20,327,515	20,327,515
		<i>p</i> -values		
Test for no skill bias	.000	.000	.012	.001

- Availability of internet...

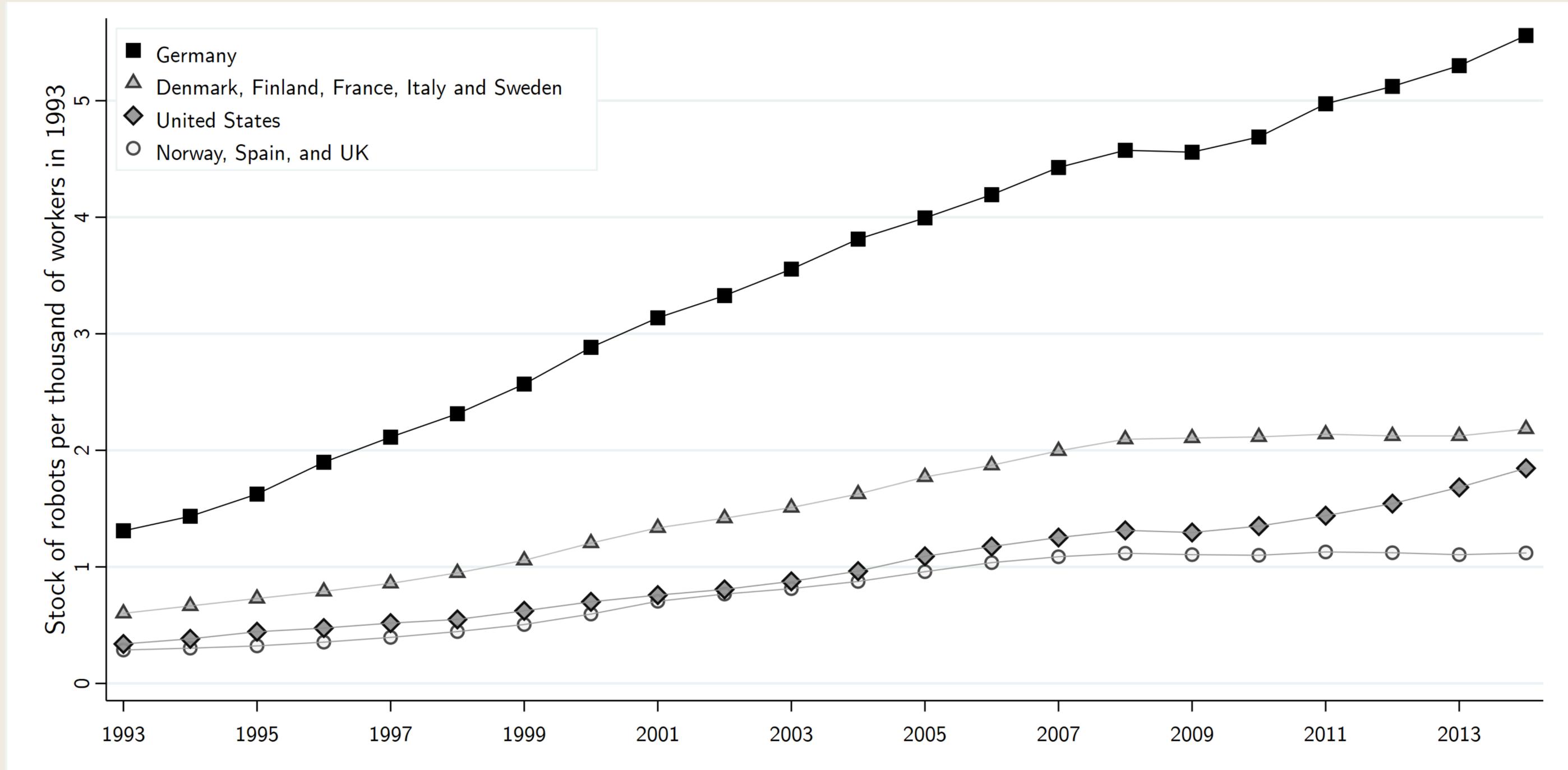
(i) raises skilled wage by 2%; (ii) reduces low skilled wage by 1%

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## **2. Automation and Wages**

**– Acemoglu and Restrepo (2019)**

# Industrial Robots per Thousand Workers



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# Robots and Jobs

*Labor will become less and less important...More and more workers will be replaced by machines. I do not see that new industries can employ everybody who wants a job.*

– Wassily Leontief

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# Can Robots Reduce Wages?

- Can robots make labor less and less important?
- Consider the production function of the form:

$$F(K, L) = AK^\alpha L^{1-\alpha}$$

- As before, wages are given by the marginal product of labor:

$$w = (1 - \alpha)AK^\alpha L^{-\alpha} = (1 - \alpha)\frac{Y}{L}$$

- More robots (higher  $K$ ) always increase wages!
- What did we miss? Is higher  $K$  the right way to think about the automation?

# Task-Based Model

- There are  $N$  tasks in the economy (cutting, assembling, designing...)

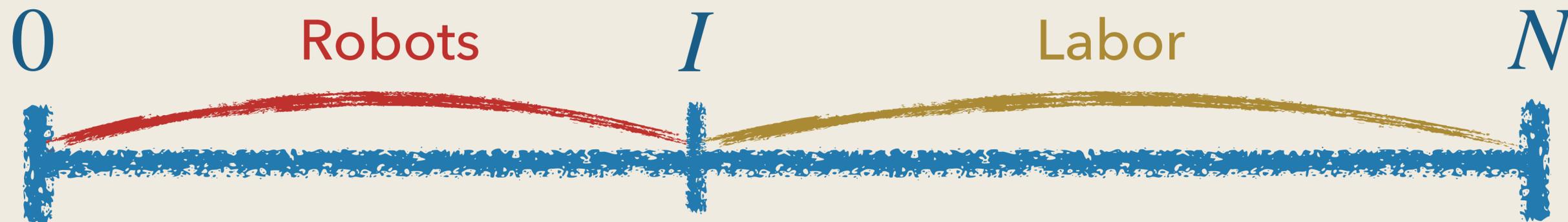
- Suppose that GDP is a combination of task-level output:

$$Y = (X_1)^{1/N} \times (X_2)^{1/N} \times \dots \times (X_N)^{1/N}$$

- Each task is produced using either labor or robots:

$$X_i = \begin{cases} K_i & \text{if } i \leq I \\ L_i & \text{if } i > I \end{cases}$$

- **Automation**: an increase in  $I$



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# Back to Cobb-Douglas

- There are  $L$  workers and  $K$  robots in the economy
- Since all tasks are symmetric, each task employ equal number of workers/robots

$$K_i = \frac{K}{I} \quad \text{for } i \leq I$$

$$L_i = \frac{L}{N - I} \quad \text{for } i > I$$

- Substituting back,

$$Y = \frac{1}{N\alpha^\alpha(1 - \alpha)^{1-\alpha}} K^\alpha L^{1-\alpha}, \quad \alpha \equiv I/N$$

- Back to the Cobb-Douglas production, but  $\alpha$  is now the share of automated tasks!

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# Automation and Wages Revisited

- The wage is given by the marginal product of labor:

$$w = (1 - \alpha) \frac{1}{N\alpha^\alpha(1 - \alpha)^{1-\alpha}} K^\alpha L^{-\alpha}$$
$$= (1 - \alpha) \frac{Y}{L}$$

- An increase  $\alpha$  now appears in two places
  - Displacement effect: automation displaces tasks that used to be performed by workers
  - Productivity effect: automation increases the overall output

# Automation and Wages Revisited

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Displacement effect

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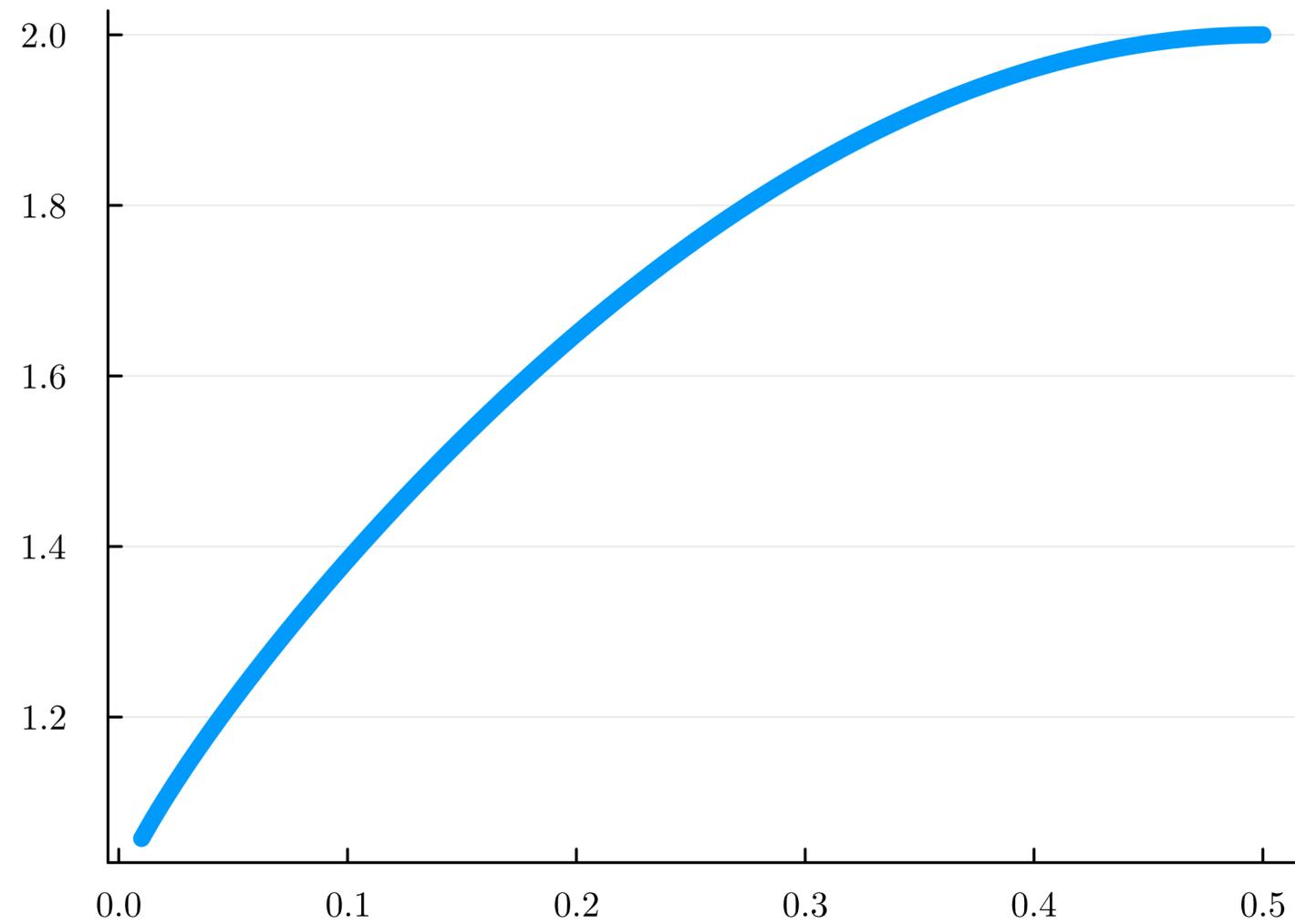
$$= (1 - \alpha) \frac{Y}{L} \text{ Productivity effect}$$

Displacement effect

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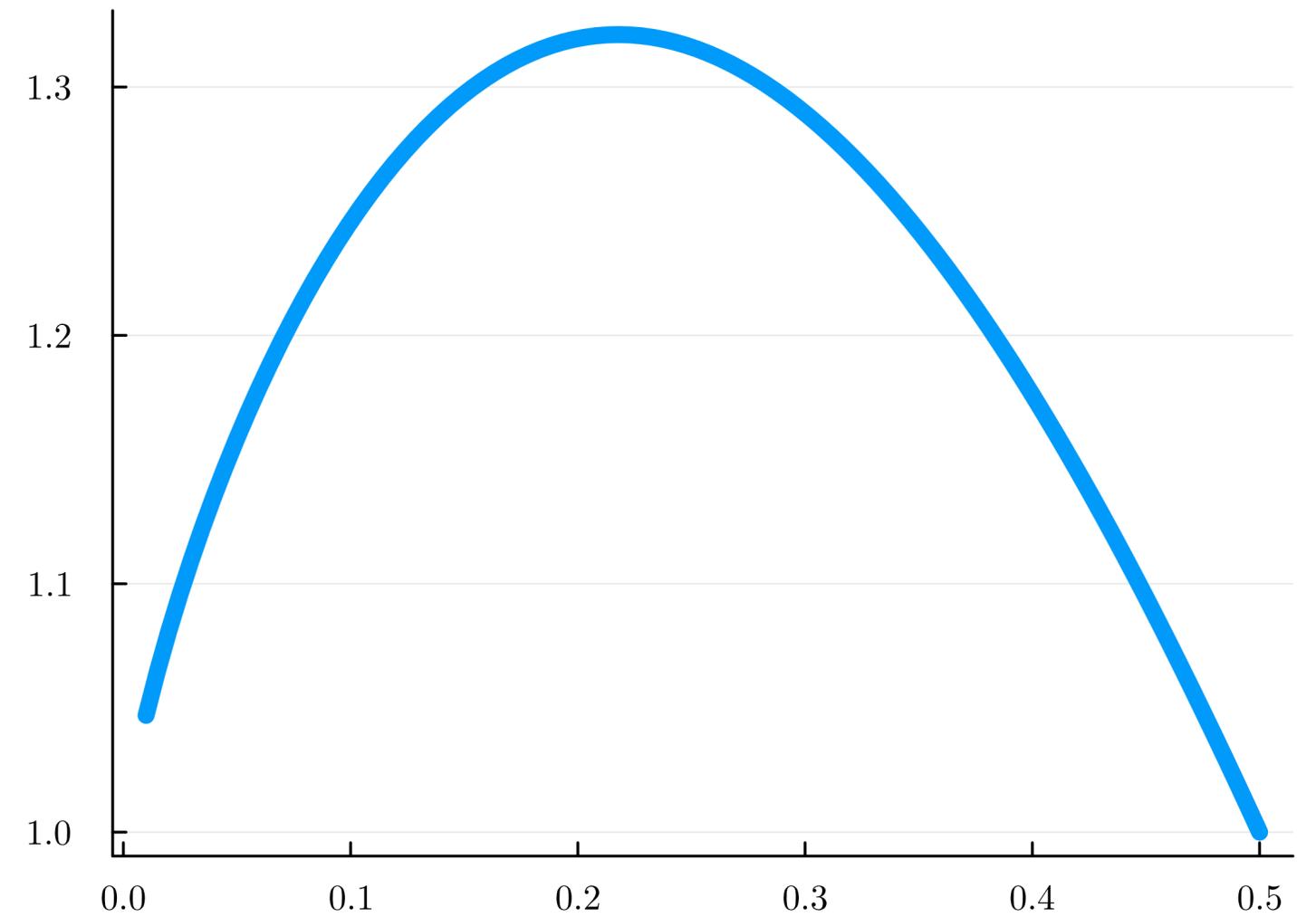
# Automation can Reduce Wage

## GDP



Share of Automated Task,  $\alpha$

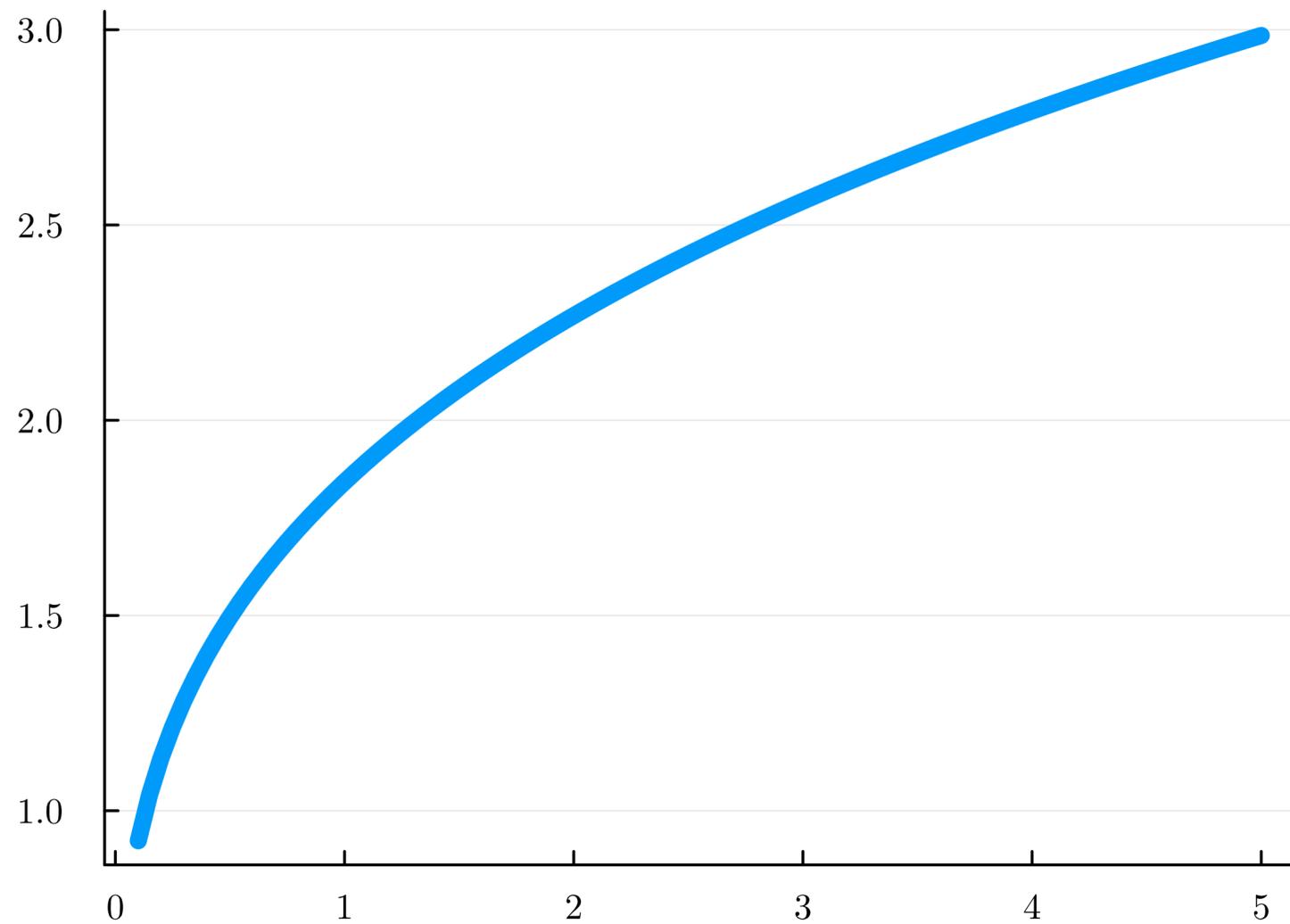
## Wage



Share of Automated Task,  $\alpha$

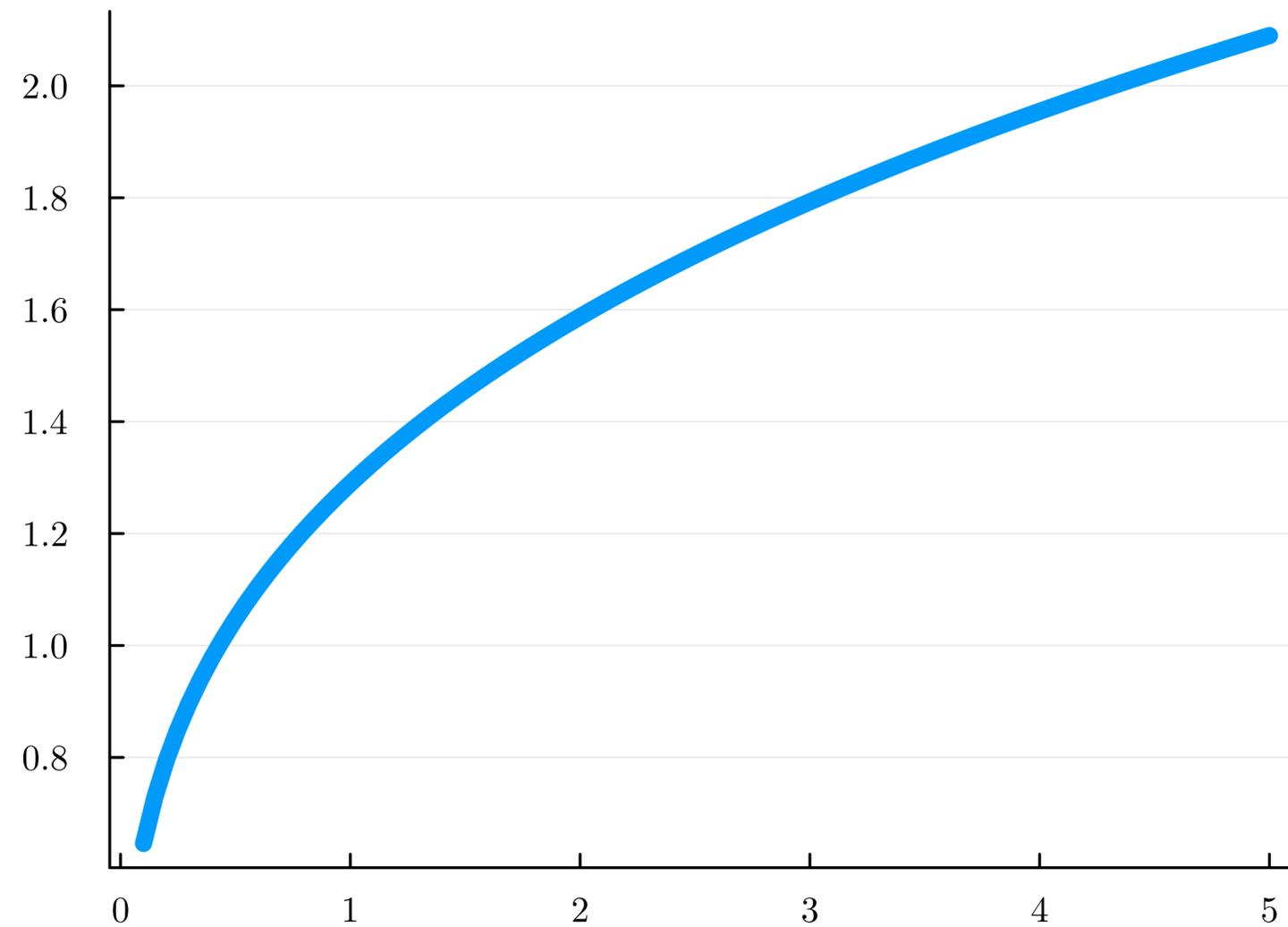
# Higher $K$ Always Increases Wages

## GDP



Capital,  $K$

## Wage



Capital,  $K$

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# **Do Robots Displace Workers?: Empirical Evidence**

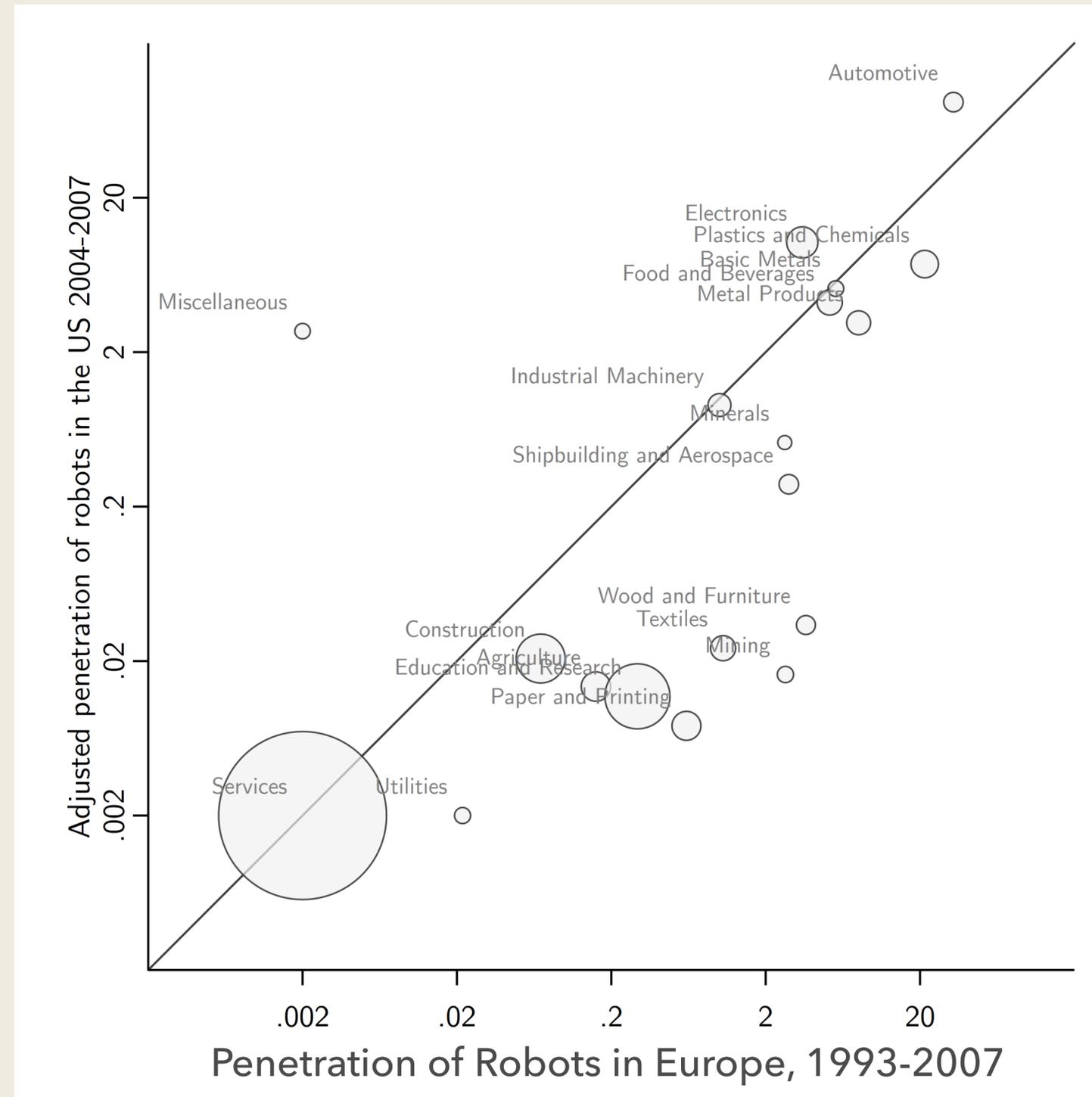
**– Acemoglu and Restrepo (2020)**

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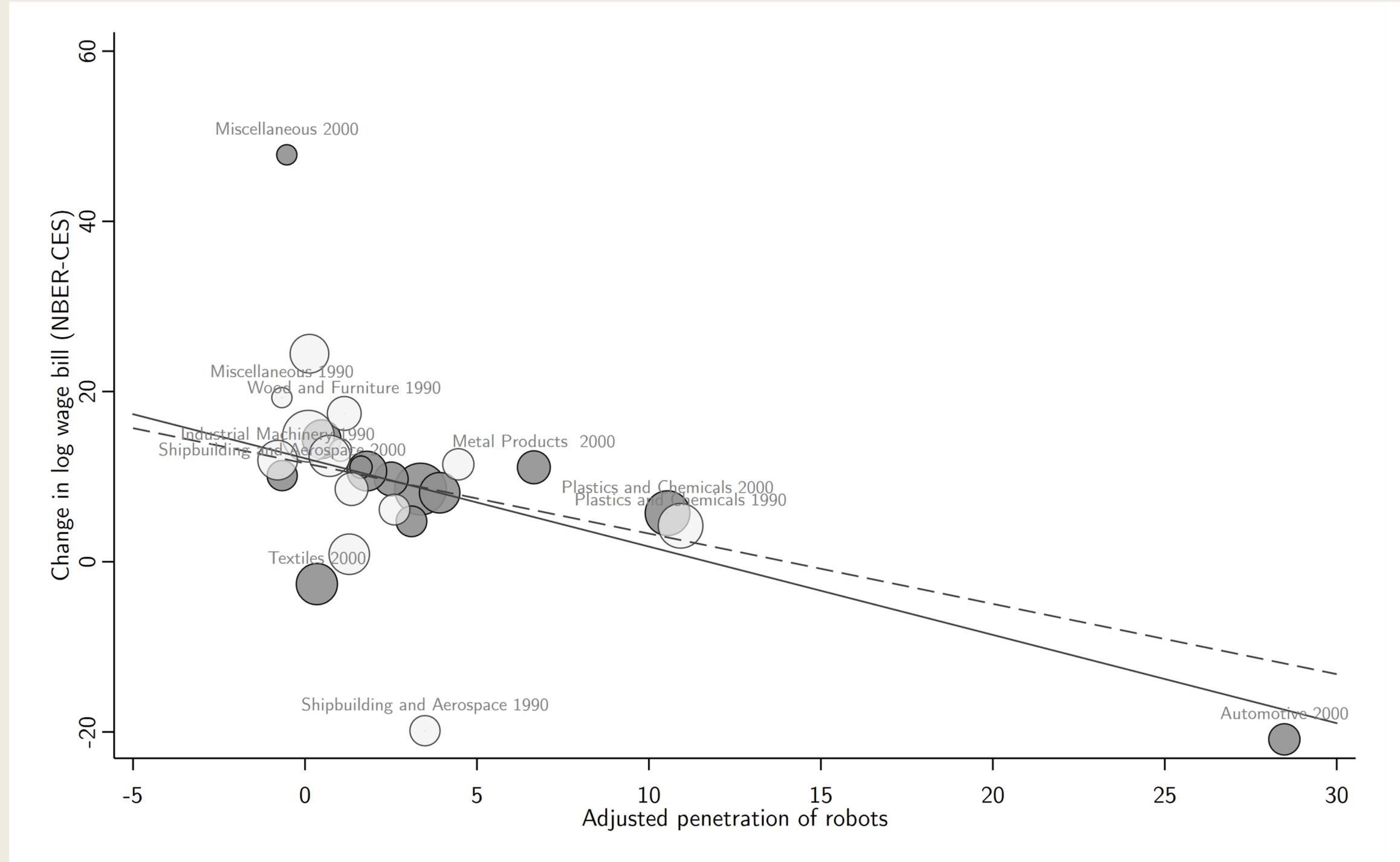
# Empirical Strategies

- Different industries experience different degrees of automation
- Regions differ in terms of industrial compositions  
⇒ difference in exposure to automation
- Two strategies:
  1. Compare more exposed industries with less exposed ones
  2. Compare more exposed regions with less exposed regions

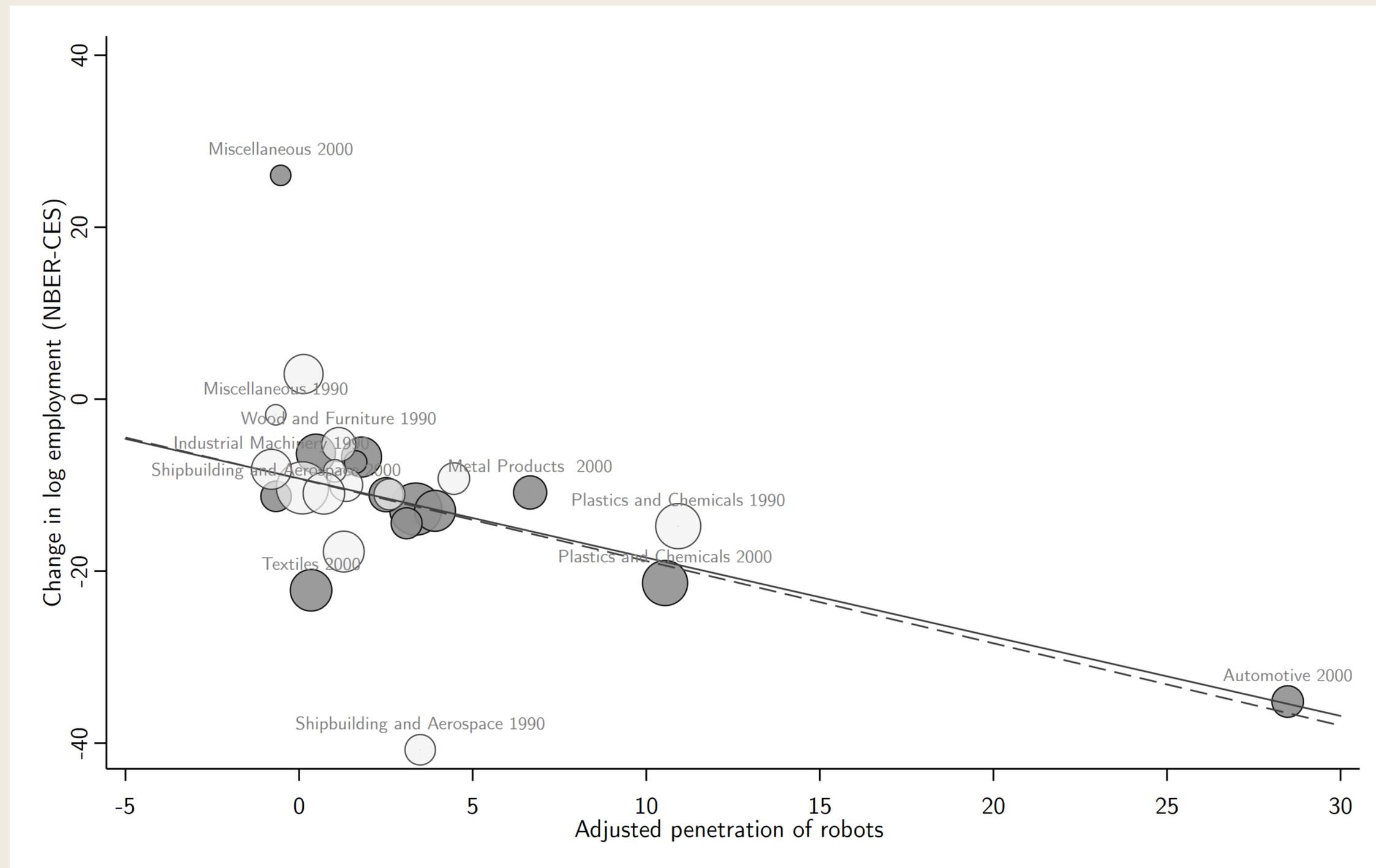
# Industry Variation



# Robot Penetration and Industry Wages



# Robot Penetration and Industry Employment

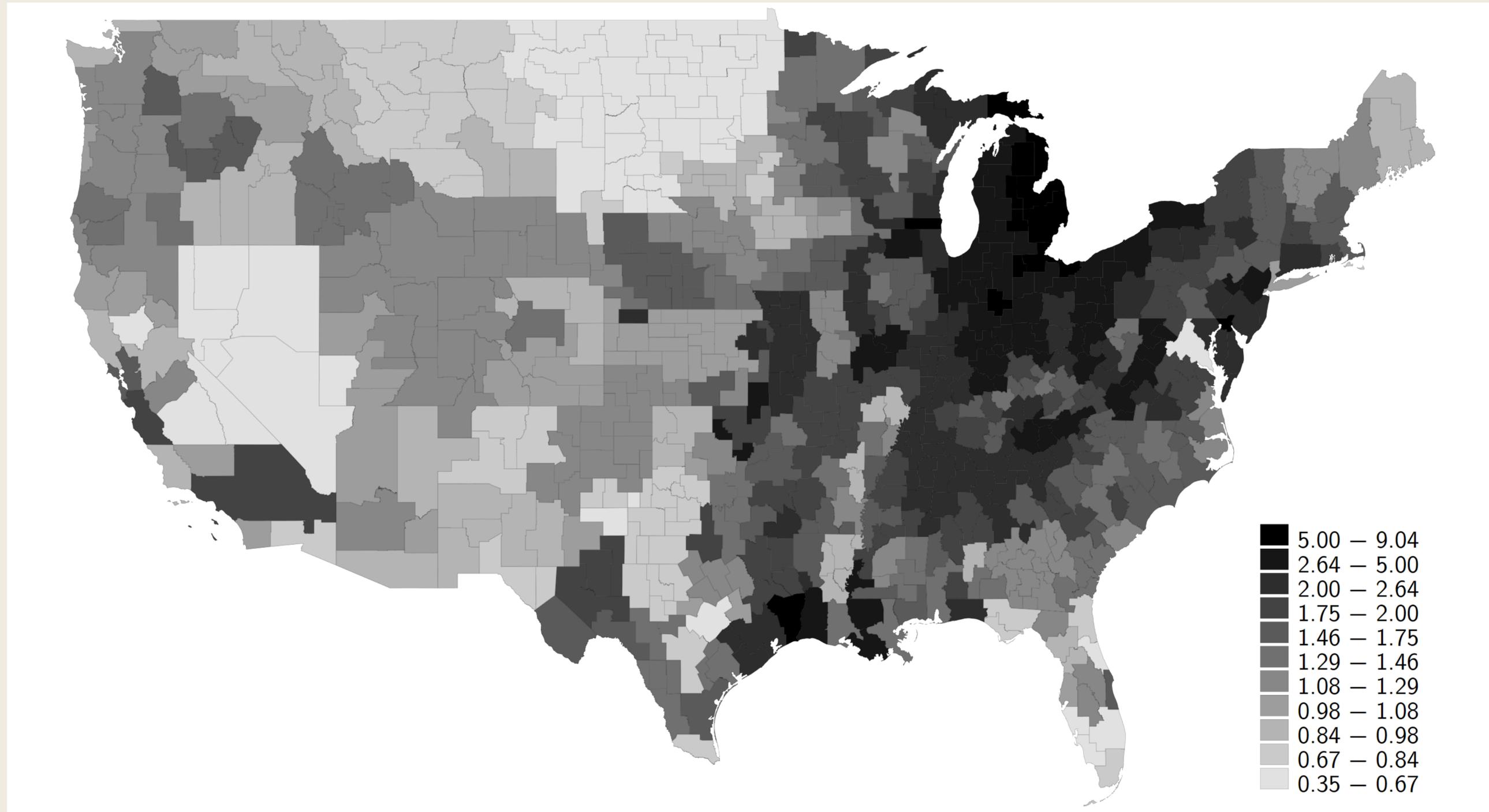


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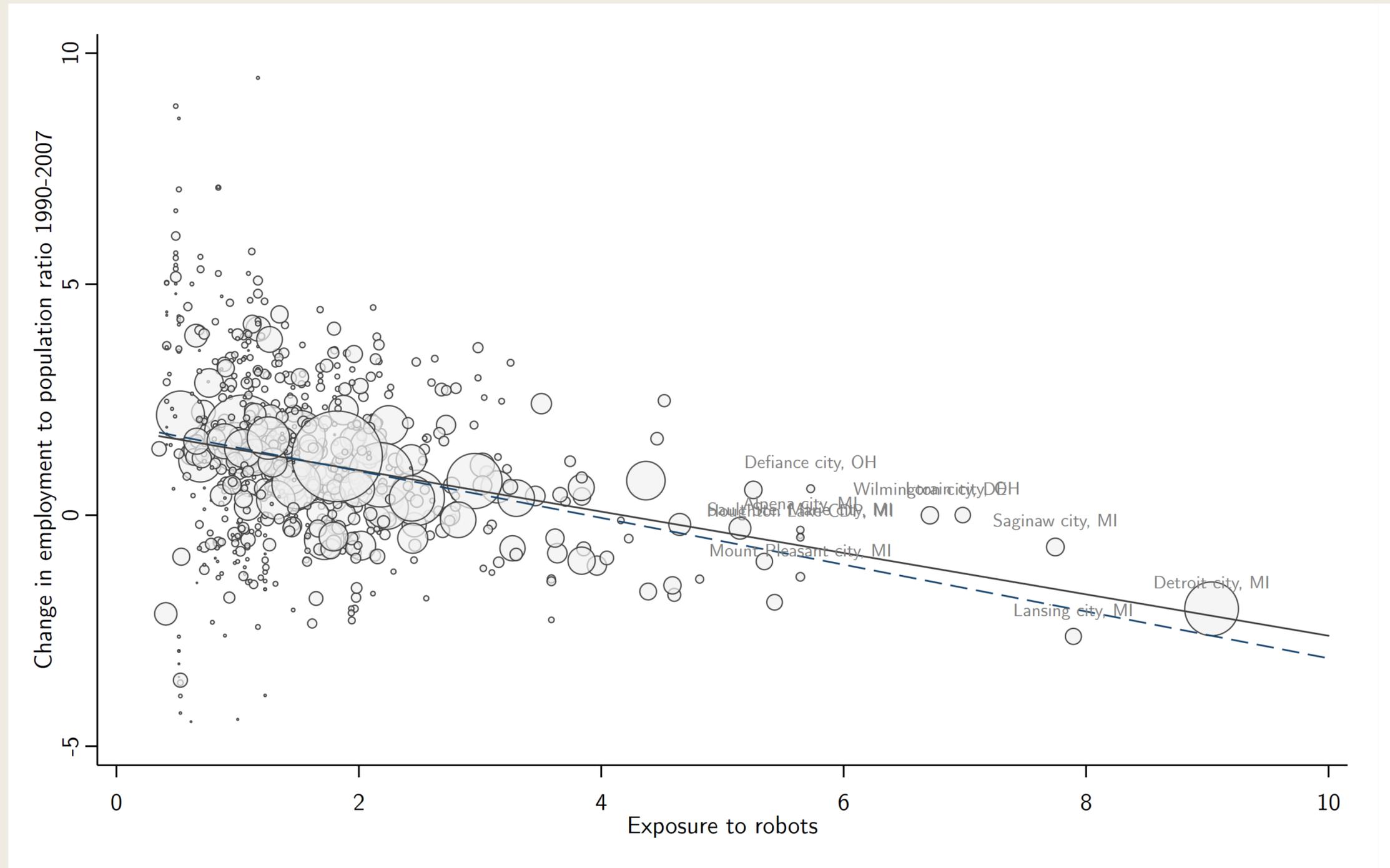
# Regional Exposure to Robots

- At the industry level, one more robot per thousand workers is associated with
  - a reduction in wages by 0.9%
  - a reduction in employment by 1.1%
- We now turn to regional analysis. Why regional?
  - It captures the local labor market *equilibrium* effect of automation
    - spillovers to people not working or leaving the directly affected industries
- US regions greatly differed in industry compositions
  - ⇒ they greatly differed also in exposures to robots

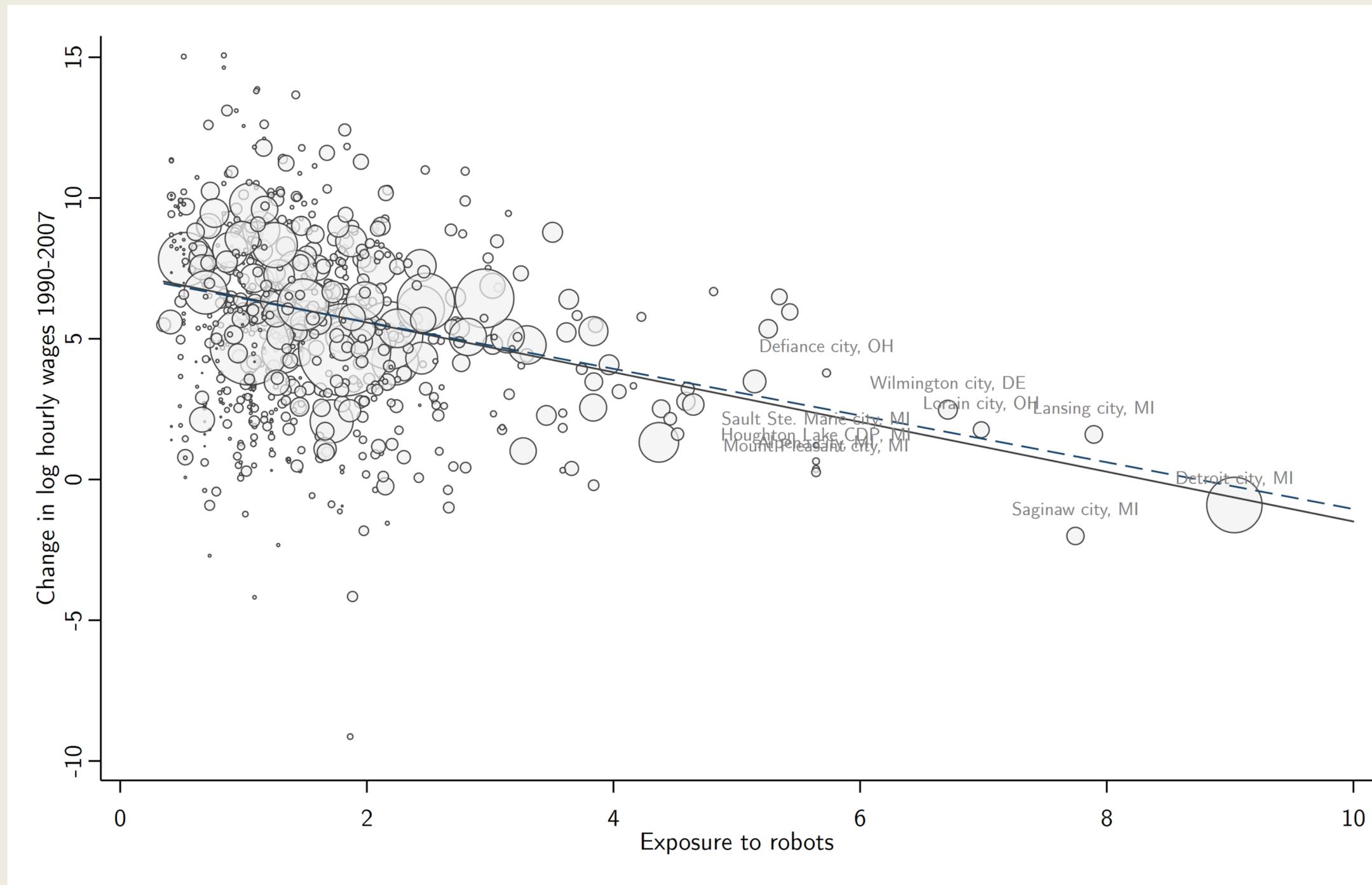
# Exposure to Robots



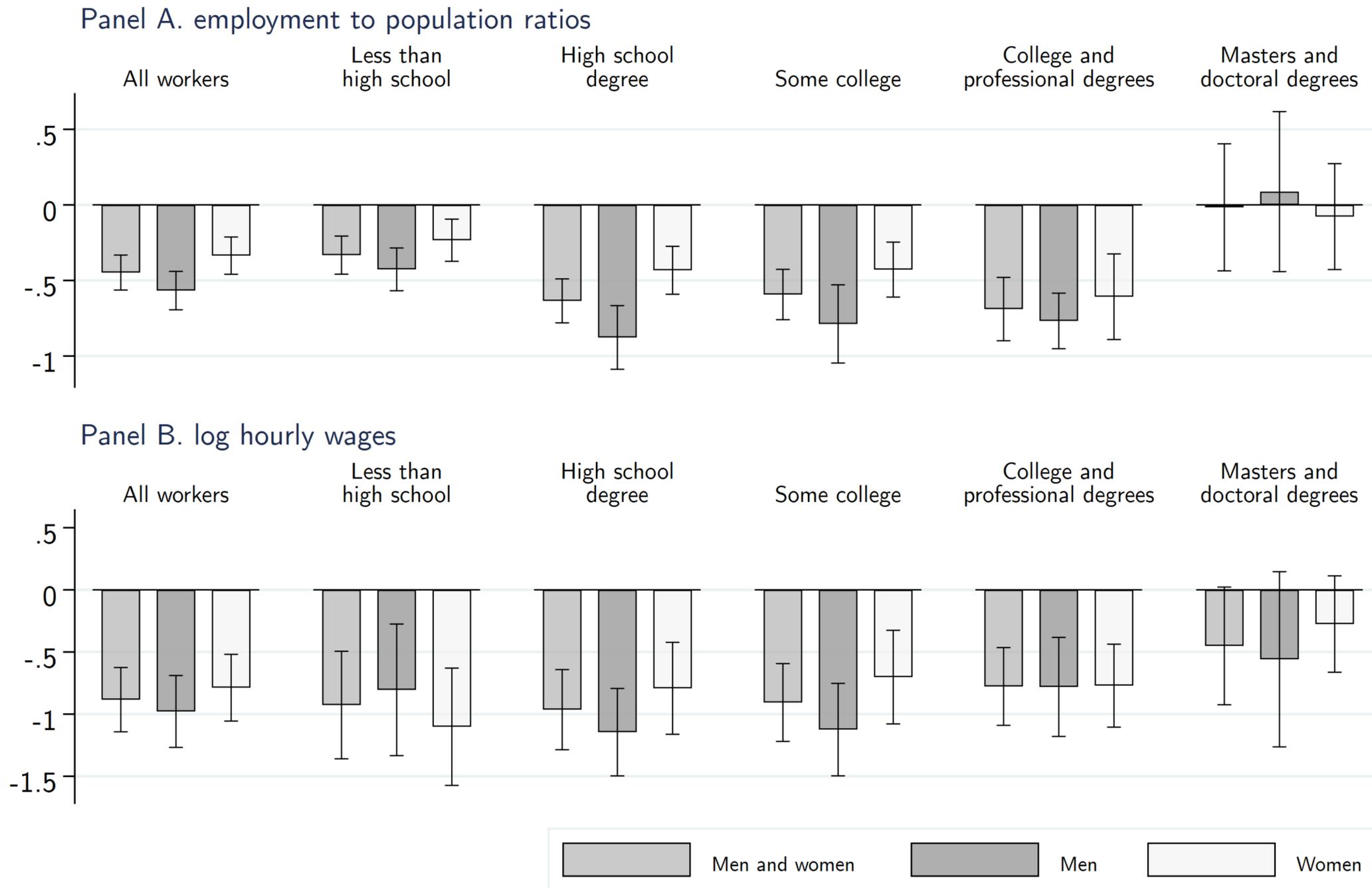
# Robots and Regional Employment



# Robots and Regional Wages



# Effect by Educational Groups



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# Quantitative Magnitude

- Robots per thousand workers increased by 1.5 in 1993-2014
- This implies
  - 0.3 p.p. decline in employment-to-population ratio
  - 0.42% decline in overall wages