

---

# Labor Supply Across Countries and Over Time

EC502 Macroeconomics  
Topic 7

Masao Fukui

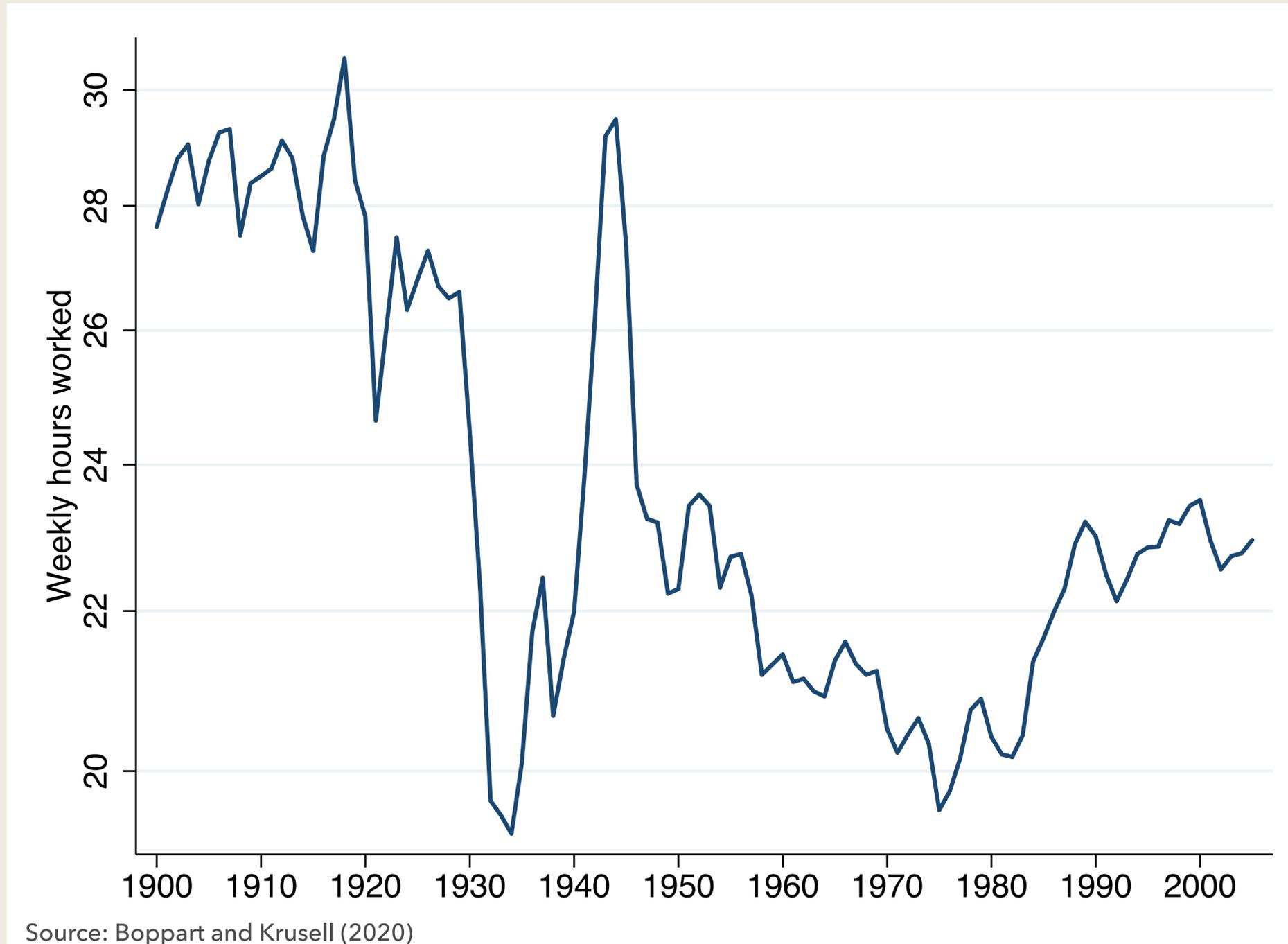
2026 Spring

---

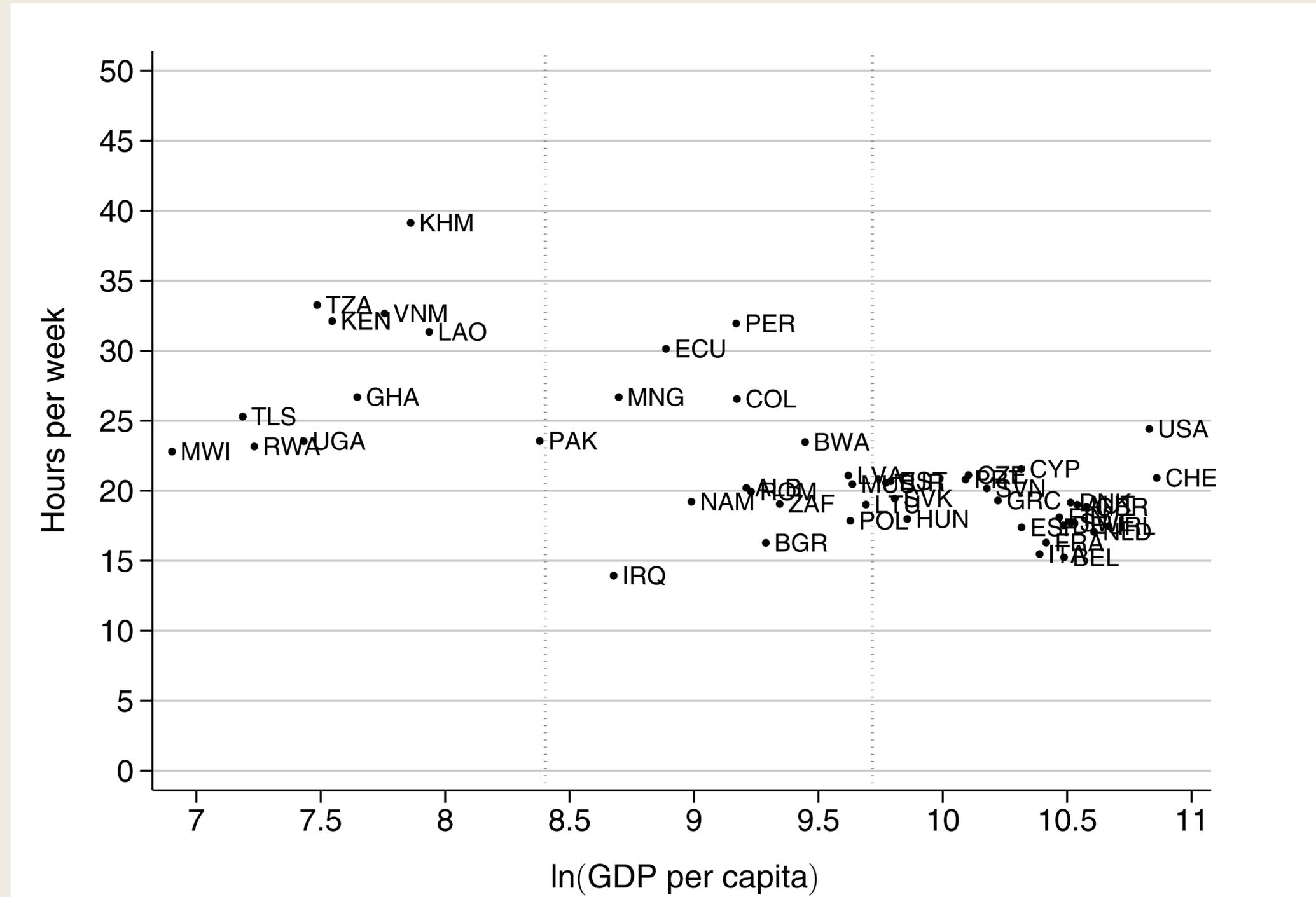
# Hours Worked

- We took the hours worked per person as exogenous so far
- We assumed that everyone supplies the same amount of labor
  - over time
  - across countries
- Is this true?

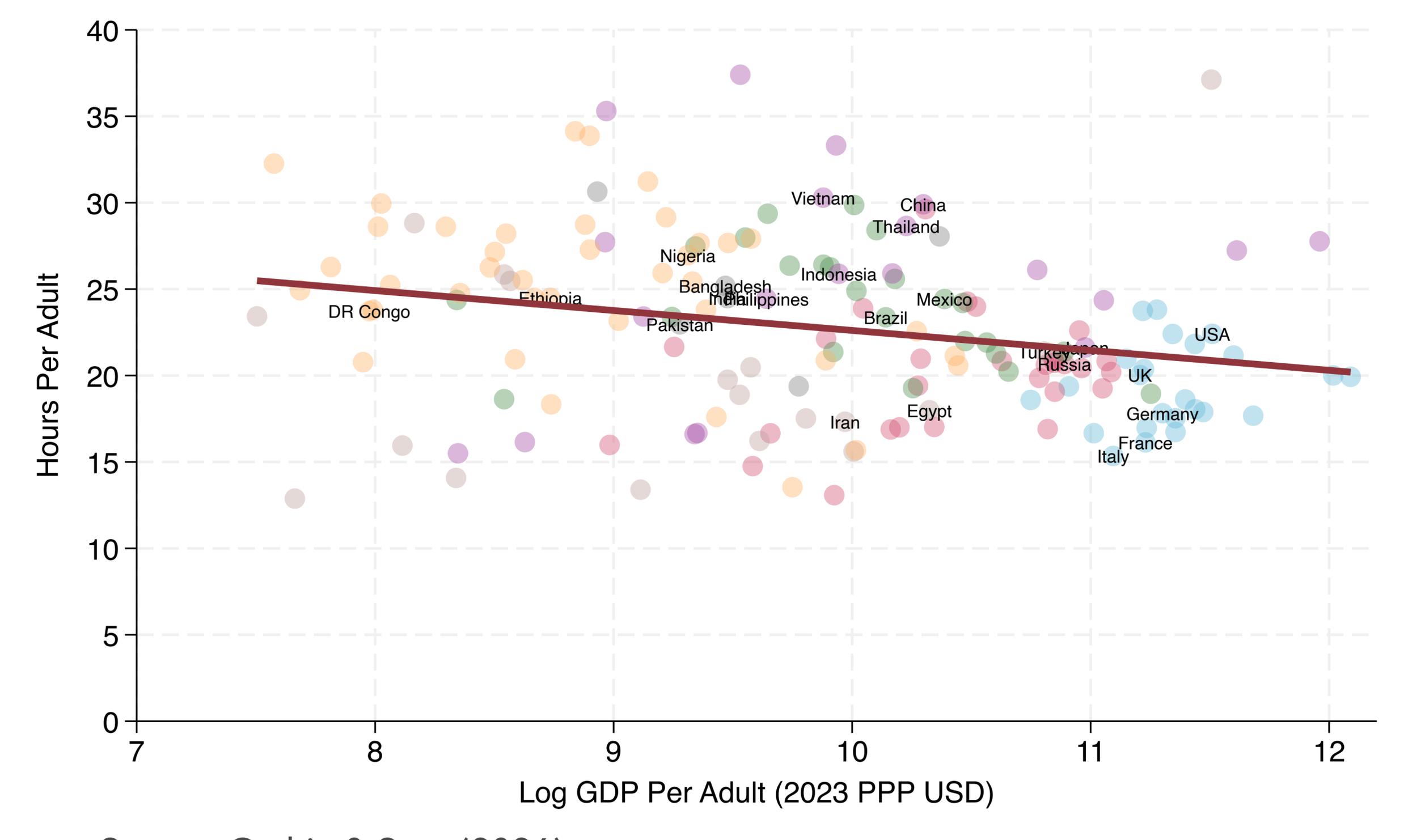
# The U.S. Time-Series



# Cross-Section in 2005



# Now More Comprehensive Data is Available



Source: Gethin & Saez (2026)

---

# Question

- Over the time-series, as a country grows, people work less
- In the cross-section, richer countries tend to work less
  - Though the relationship is weaker with more comprehensive data
- What determines the hours worked in the time-series and in the cross-section?

---

# **A Simple Model of Labor Supply**

---

# A Model of Labor Supply

- What is the benefit of working more? – earn a higher income
- What is the cost of working more? – pain to work longer hours
- We introduce a minimal model that captures these trade-offs

---

# Preferences

- Households have the following utility functions:

$$u(c) - v(l)$$

- We  $u$  is concave and  $v$  is convex:

- $u'(c) > 0$ : households are happier if consumption is higher
- $u''(c) < 0$ : additional consumption is less pleasant if already consuming a lot
- $v'(l) > 0$ : households are less happy if they work more
- $v''(l) > 0$ : additional hours of work are more painful if already working a lot

- The households face the following budget constraint

$$c = wl$$

---

# Optimality Condition

- The households decide  $(c, l)$  subject to the budget constraint:

$$\max_{c,l} u(c) - v(l)$$

$$\text{s.t. } c = wl$$

- First-order condition:

$$u'(c)w = v'(l)$$

- LHS: marginal benefit of work
- RHS: marginal cost of work

---

# Functional Form Assumptions

- For simplicity, we assume

$$u(c) = \frac{c^{1-\sigma} - 1}{1-\sigma}, \quad v(l) = \bar{v} \frac{l^{1+\nu}}{1+\nu}$$

with  $\sigma > 0$  and  $\nu > 0$

- One can check:

- $u'(c) = c^{-\sigma} > 0$ ,  $u''(c) = -\sigma c^{-\sigma-1} < 0$
- $v'(l) = \bar{v} l^{\nu} > 0$ ,  $v''(l) = \bar{v} \nu l^{\nu-1} > 0$

- For  $\sigma = 1$ ,

$$u(c) = \log c \quad \text{when } \sigma = 1$$

- Obtained as a limit of  $\sigma \rightarrow 1$  (apply L'hospital's rule)

---

# Optimal Labor Supply Solutions

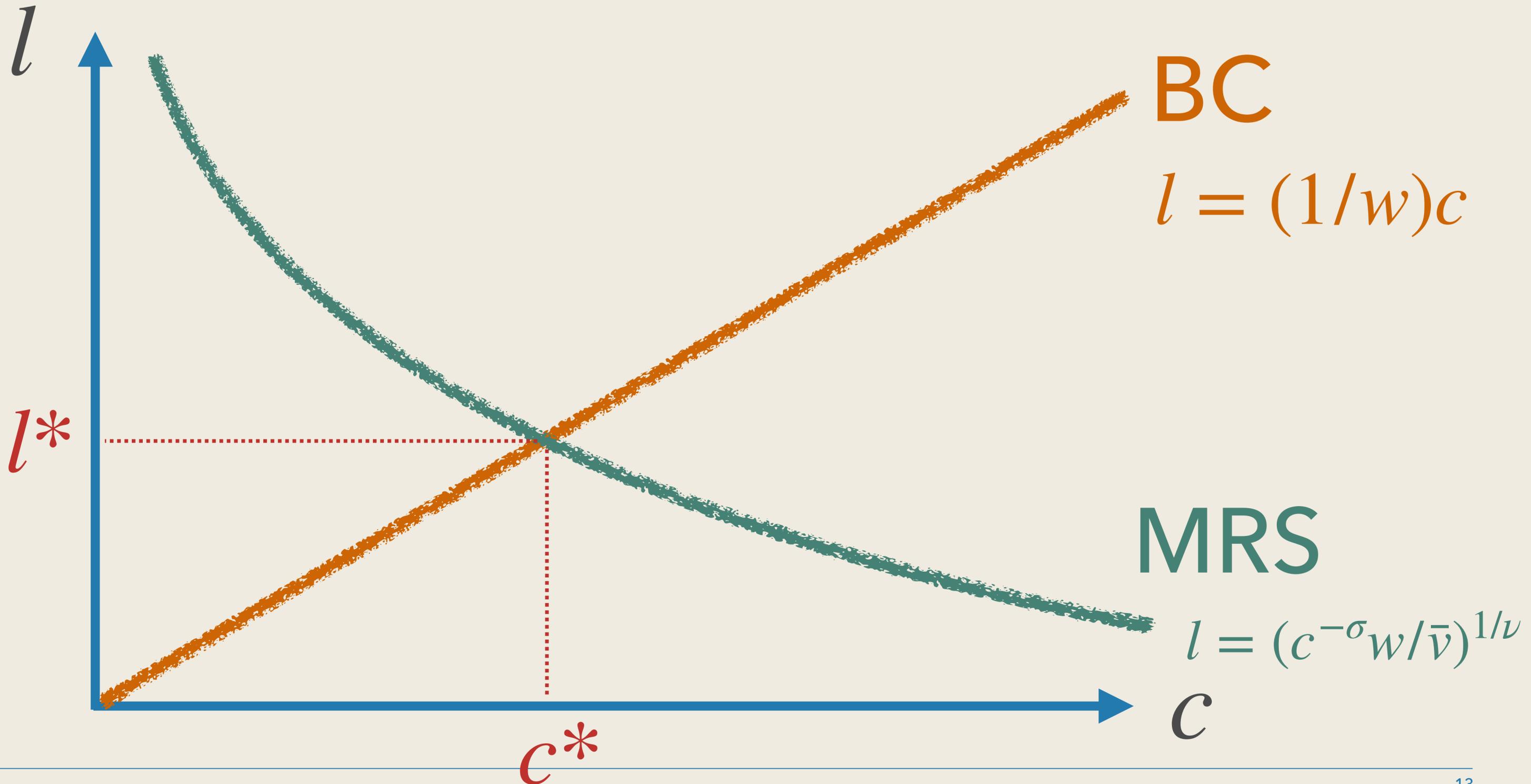
- Consumption and hours worked,  $\{c, l\}$ , jointly solve

$$c^{-\sigma} w = \bar{v} l^{\nu} \quad \text{(MRS)}$$

$$c = wl \quad \text{(BC)}$$

1. **(MRS)** defines a decreasing relationship between  $c$  and  $l$
2. **(BC)** defines an increasing relationship between  $c$  and  $l$

# Graphical Representation



---

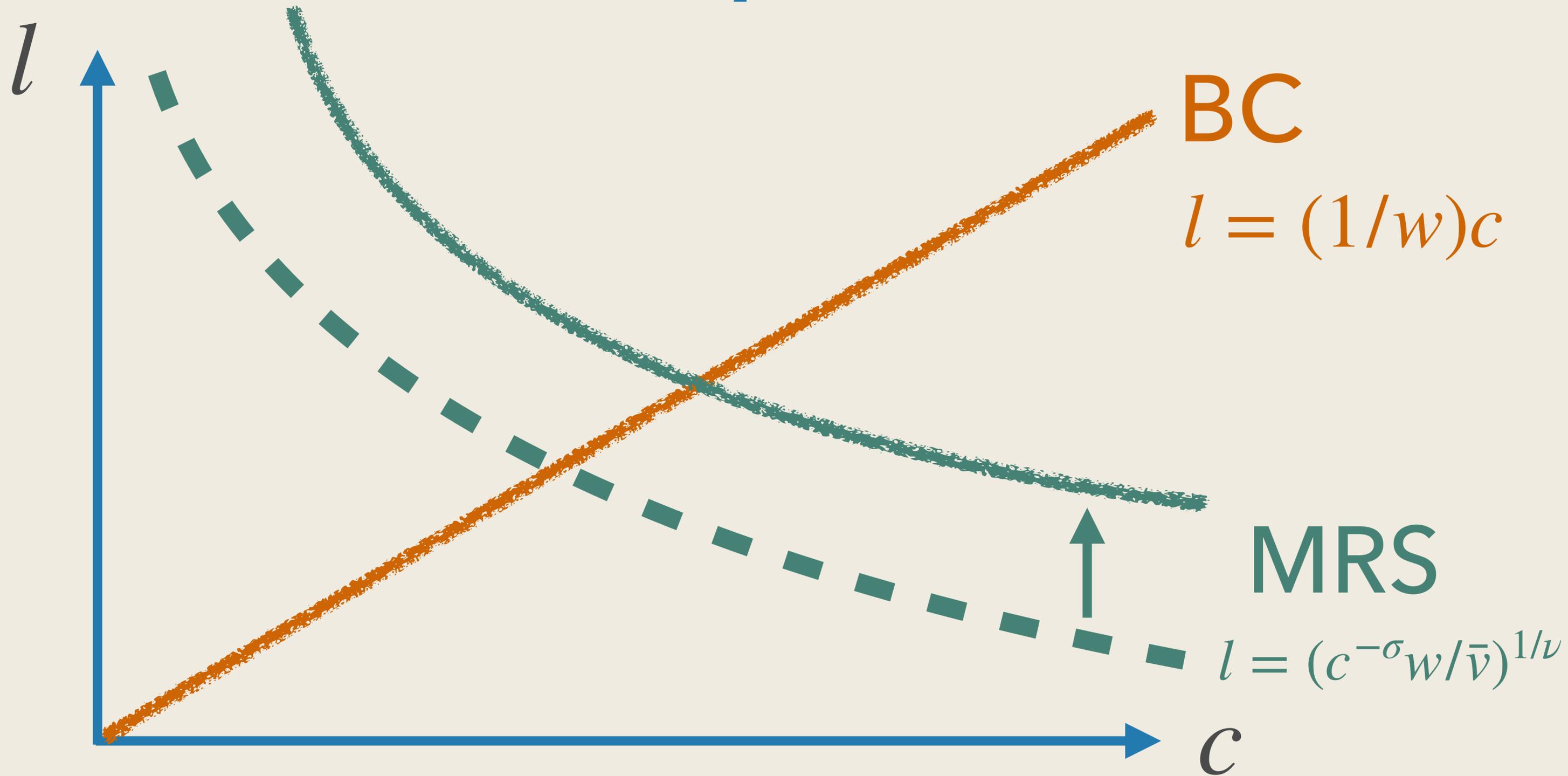
# Question

$$c^{-\sigma} w = \bar{v} l^\nu \quad (\text{MRS})$$

$$c = w l \quad (\text{BC})$$

- As a country gets richer, what happens to the labor supply?
- We will consider an increase in wage,  $w$
- Note that wage,  $w$ , appears in two places (**orange** and **green**)

# First Effect: Shift Up in MRS Curve

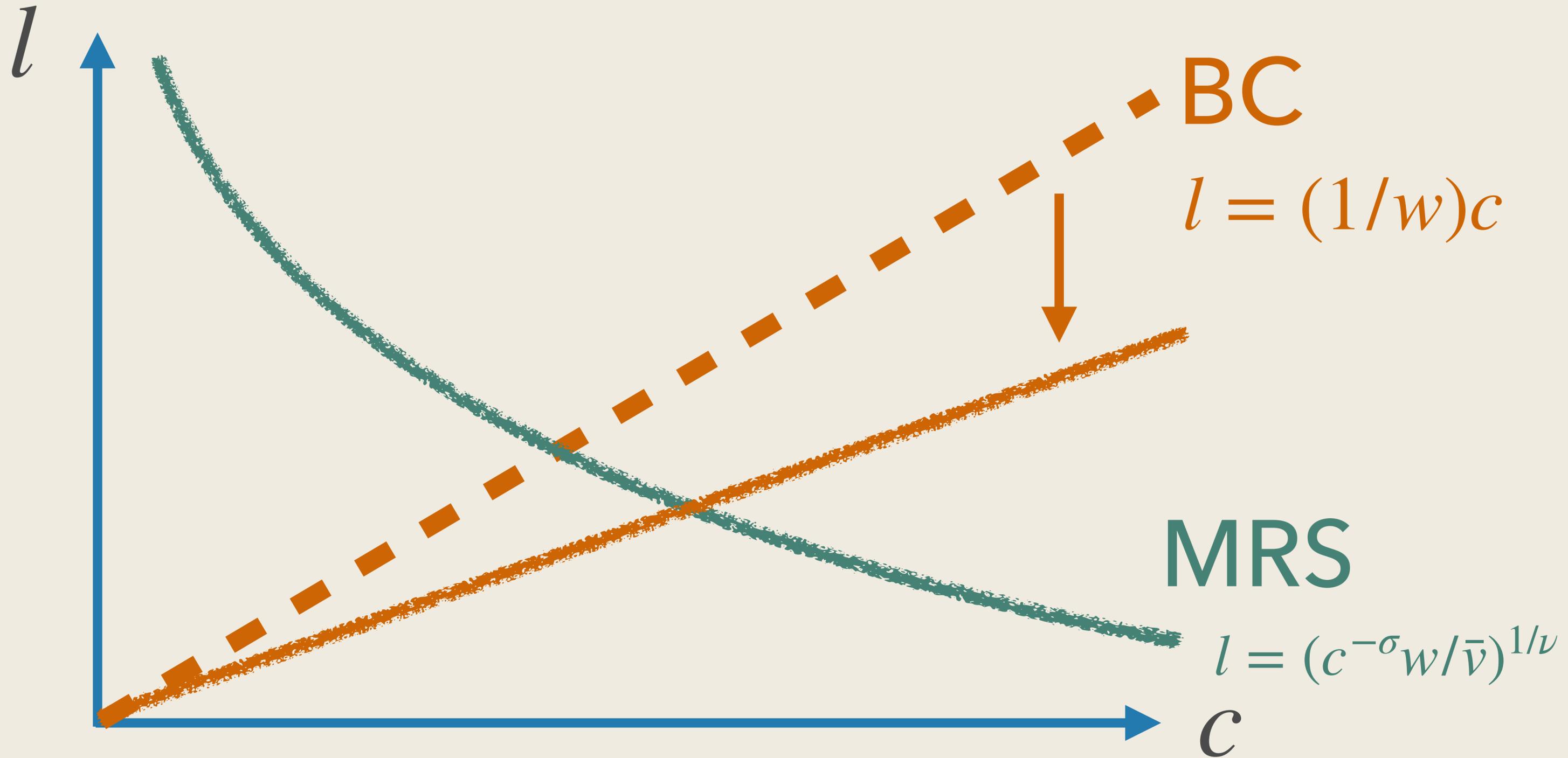


---

# Substitution Effect

- MRS curve shifts up when  $w$  goes up
- If wages are higher, the marginal benefit of working is higher for any given  $c$
- Holding the BC curve fixed, this means the labor supply,  $l$ , goes **up!**
- We call this a **substitution effect**

# Second Effect: Shift Down in BC Curve

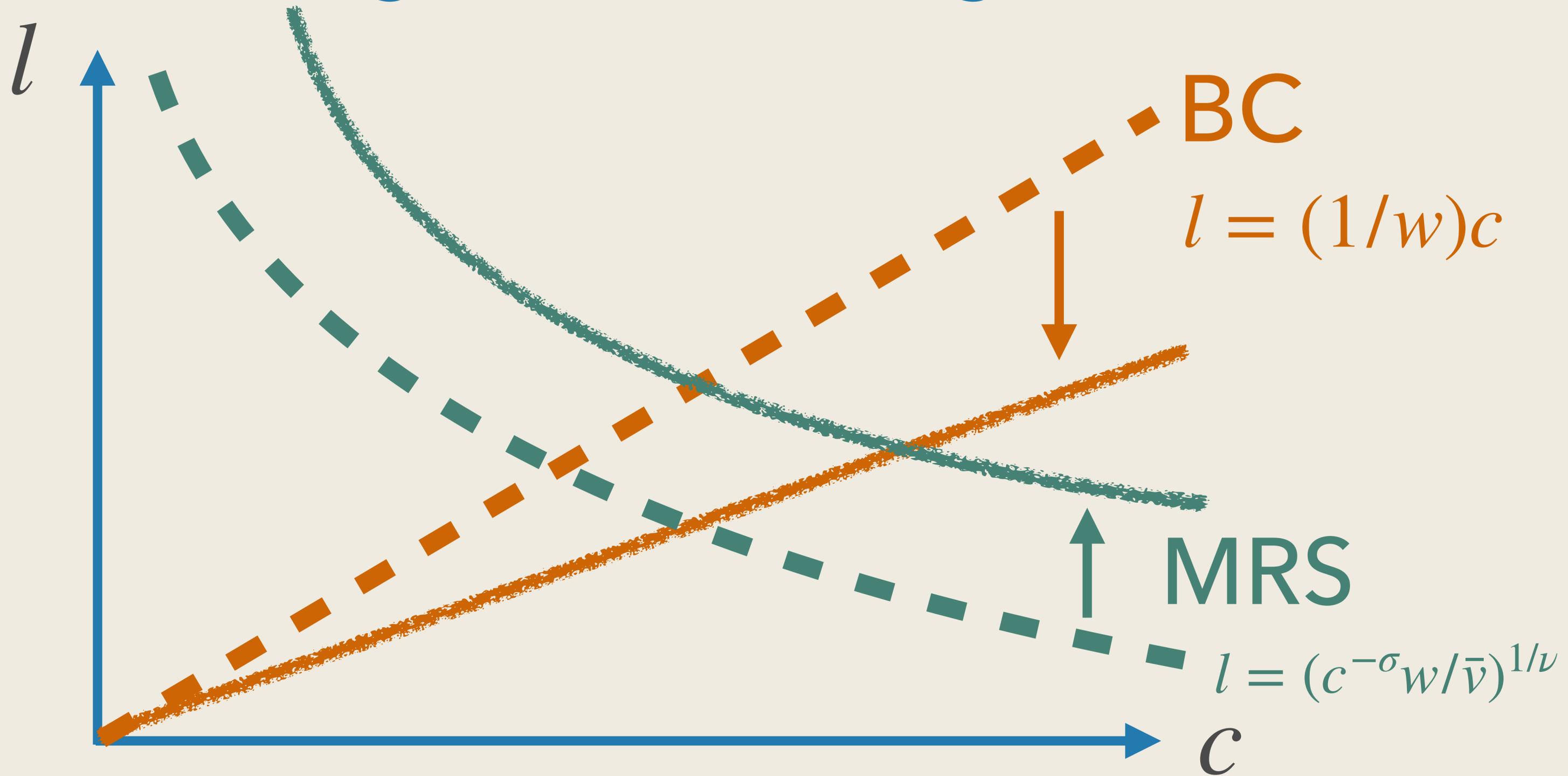


---

# Income Effect

- The BC curve shifts down when  $w$  goes up
  - If wages are higher, the budget constraint implies  $c$  is higher for any given  $l$
- Holding the MRS curve fixed, this means the labor supply,  $l$ , goes **down!**
- If I get richer, I don't need to work hard to achieve a given level of  $c$
- We call this the **income effect**

# Putting Two Effects Together



---

# Higher or Lower Labor Supply?

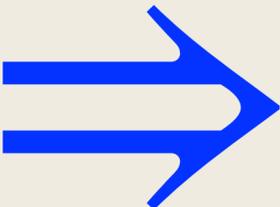
- So, does the labor supply go up or down when  $w$  goes up?
- Not clear
- In fact, it can go either way

---

## Solving for $l$

$$c^{-\sigma} w = \bar{v} l^\nu \quad (\text{MRS})$$

$$c = w l \quad (\text{BC})$$

  $l = \frac{\bar{v}^{-1}}{\nu + \sigma} w^{\frac{1}{\sigma + \nu}} w^{\frac{-\sigma}{\sigma + \nu}}$

---

# $\sigma$ Determines the Relative Importance

$$l = \bar{v} \frac{-1}{\nu + \sigma} \mathcal{W} \frac{1}{\sigma + \nu} \mathcal{W} \frac{-\sigma}{\sigma + \nu}$$
$$= \bar{v} \frac{-1}{\nu + \sigma} \mathcal{W} \frac{1 - \sigma}{\sigma + \nu}$$

1.  $\sigma < 1$ :  $l$  is increasing in  $w$ . Substitution effect dominates income effect
2.  $\sigma > 1$ :  $l$  is decreasing in  $w$ . Income effect dominates substitution effect
3.  $\sigma = 1$ :  $l$  is invariant to  $w$ . Income effect and substitution effect cancel

---

# Endogeneizing $w$

- Now we endogenize wages,  $w$
- Suppose the firm operates the following production function

$$y = Al$$

- Firms solve

$$\max_l Al - wl$$

- In equilibrium,

$$w = A$$

- Plugging it back,

$$l = \bar{v}^{\frac{1}{\nu+\sigma}} A^{\frac{1-\sigma}{\sigma+\nu}}$$

---

# Can We Qualitatively Explain Two Facts?

- Taking log,

$$\log l = \frac{1 - \sigma}{\sigma + \nu} \log A + \text{const}.$$

- Suppose that  $\sigma > 1$

1. Rich (high  $A$ ) countries work less than poor countries
2. As countries grow (higher  $A$ ), they work less

- If income effect dominates substitution effect, we can explain aggregate data

# Can We Quantitatively Explain Two Facts?

## ■ Over time-series

$$g_l = \frac{1 - \sigma}{\sigma + \nu} g_A + \epsilon_t$$

- Calculations from the US data suggest  $g_l \approx -0.4\%$  and  $g_A \approx 2\%$
- This suggests  $\frac{1 - \sigma}{\sigma + \nu} \approx -0.2$

## ■ In the cross-section,

$$\log l_i = \frac{1 - \sigma}{\sigma + \nu} \log A_i + \epsilon_i$$

- Regression estimates by Bick, Fuchs-Schündeln, Lgagos (2015),  $\frac{1 - \sigma}{\sigma + \nu} \approx -0.15$
- Using Gethin & Saez (2026) data,  $\frac{1 - \sigma}{\sigma + \nu} \approx -0.08$

---

**Income Effect from Labor Supply:  
Direct Evidence**  
– **Golosov, Graber, Mogstad & Novgorodsky (2023)**

---

# Direct Evidence?

- Hours worked tend to, if anything, decline as an economy gets richer
- The model suggests that a strong income effect,  $\sigma \geq 1$ , is the key reason
- Do we have direct evidence of the income effect?
- What is the ideal experiment?
- What is the concern with using the aggregate data?

---

# Isolating Income Effect

- Maybe wage is not the only thing that changes over time and across countries
- The ideal experiment that isolates the income effect:
  - Give money to people and see how they change the labor supply
- If income effect is big, we will see a big reduction in labor supply
- If income effect is small, we will not see a major change in labor supply

---

# Conceptual Framework

- Add non-labor income  $T$  to the previous model,

$$\max_{c,l} u(c) - v(l)$$

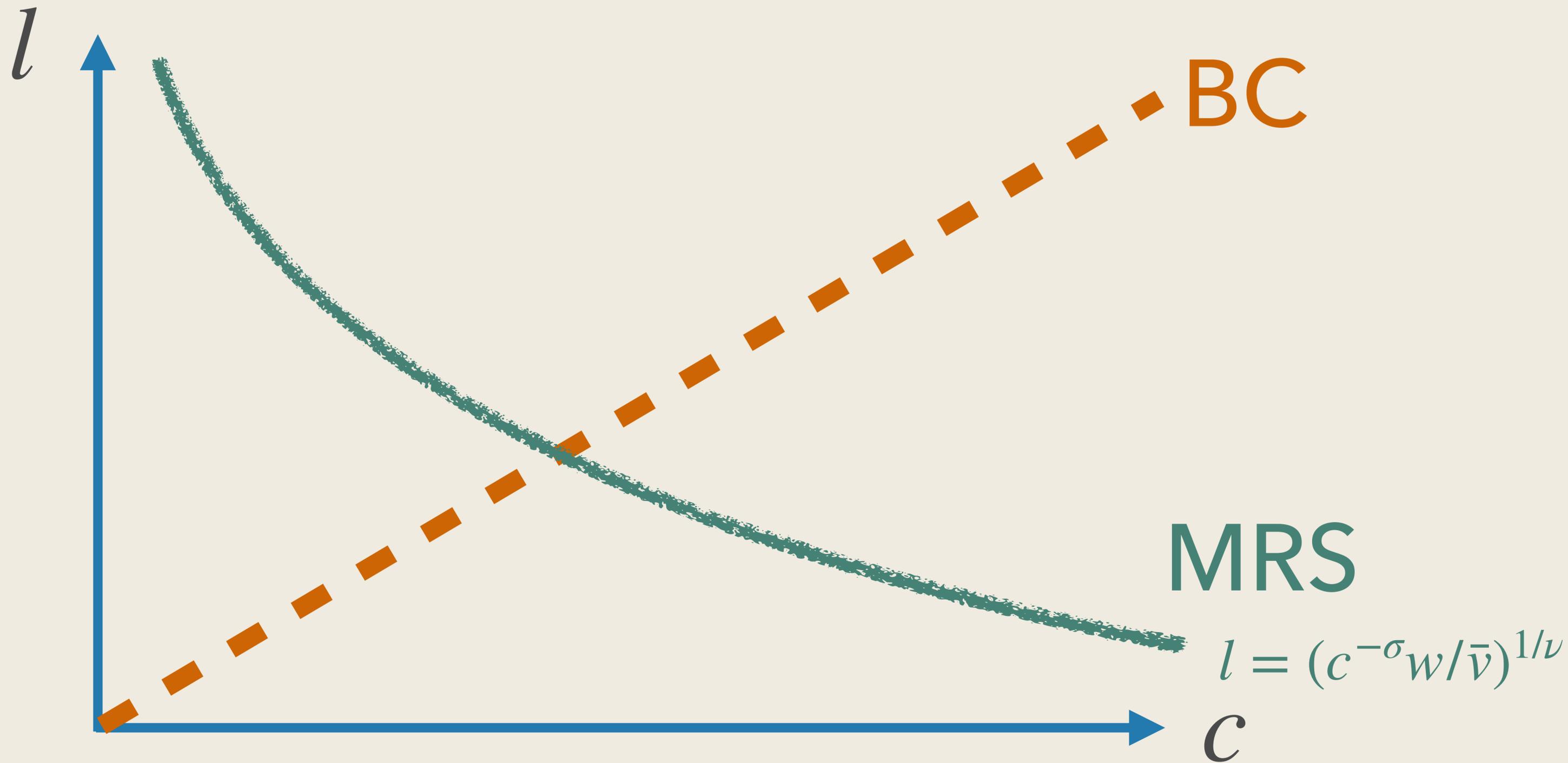
$$\text{s.t. } c = wl + T$$

- Assuming  $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$  and  $v(l) = \bar{v} \frac{l^{1+\nu}}{1+\nu}$ ,  $\{c, l\}$ , jointly solve

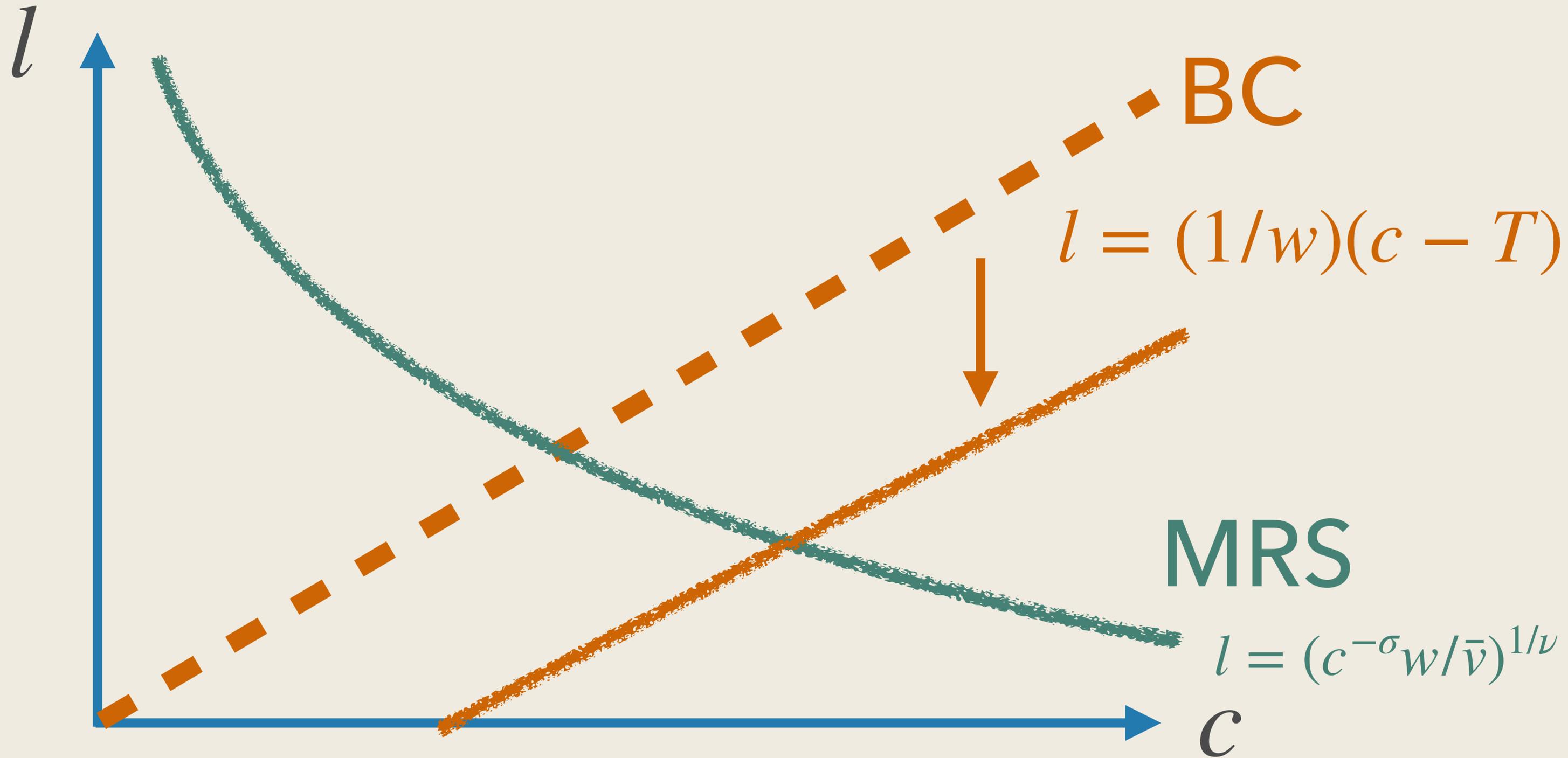
$$c^{-\sigma} w = \bar{v} l^{\nu} \quad \text{(MRS)}$$

$$c = wl + T \quad \text{(BC)}$$

# Impact of Lottery Winning $T \uparrow$



# Impact of Lottery Winning $T \uparrow$



---

# Marginal Propensity to Earn

- Empirically, it is convenient to look at MPE out of  $T \equiv \frac{d(wl)}{dT}$ 
  - MPE = marginal propensity to earn
- One can show:

$$MPE = \frac{d(wl)}{dT} = \frac{-\sigma s_w}{[\sigma s_w + \nu]}$$

where  $s_w = \frac{wl}{wl + T}$  is the share of wage income in total income

- MPE speaks to the importance of  $\sigma$ :  
If  $\sigma = 0$ ,  $MPE = 0$ . If  $\sigma$  is very big,  $MPE$  is very negative.

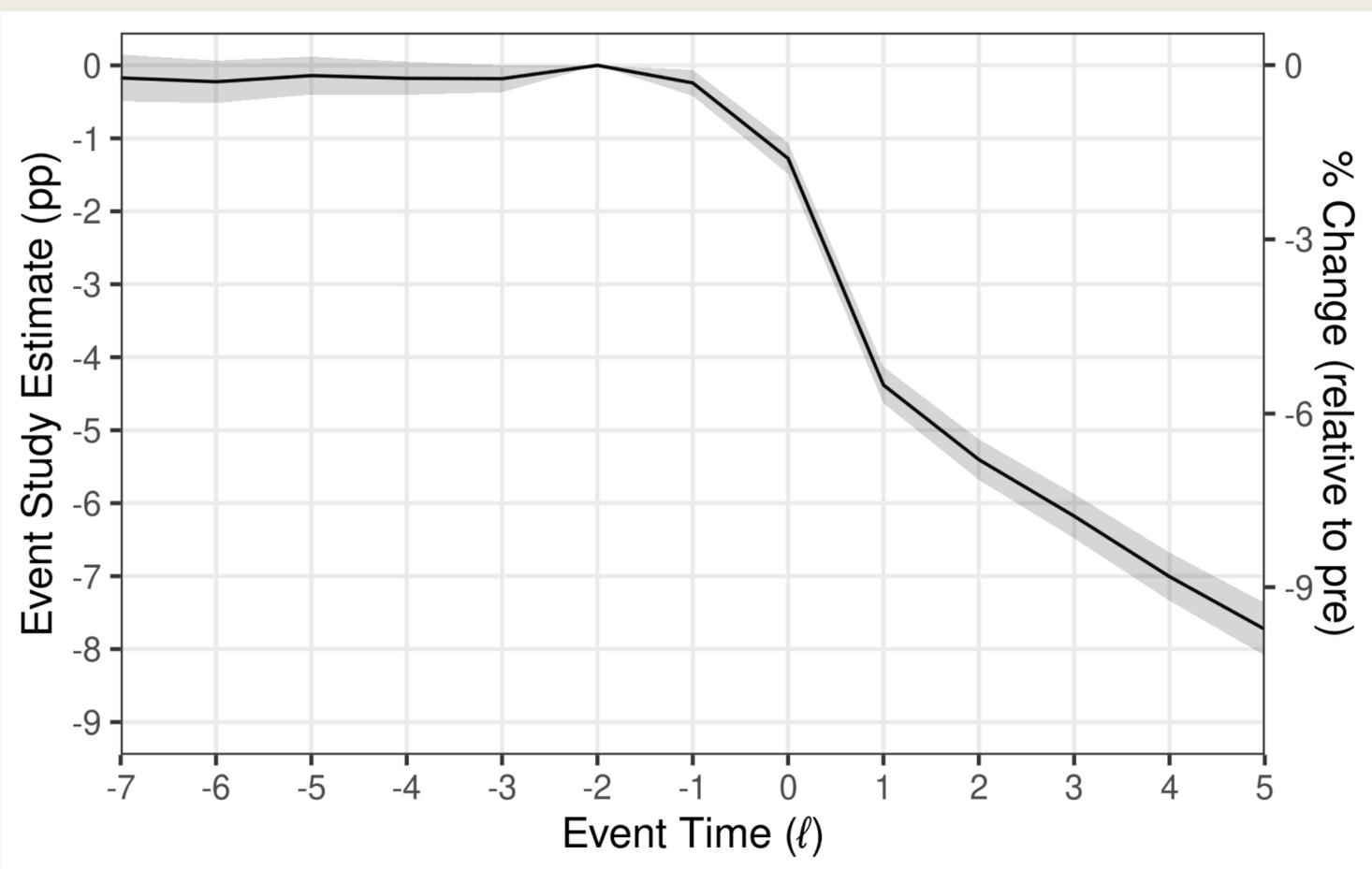
---

# Labor Supply Response of Lottery Winners

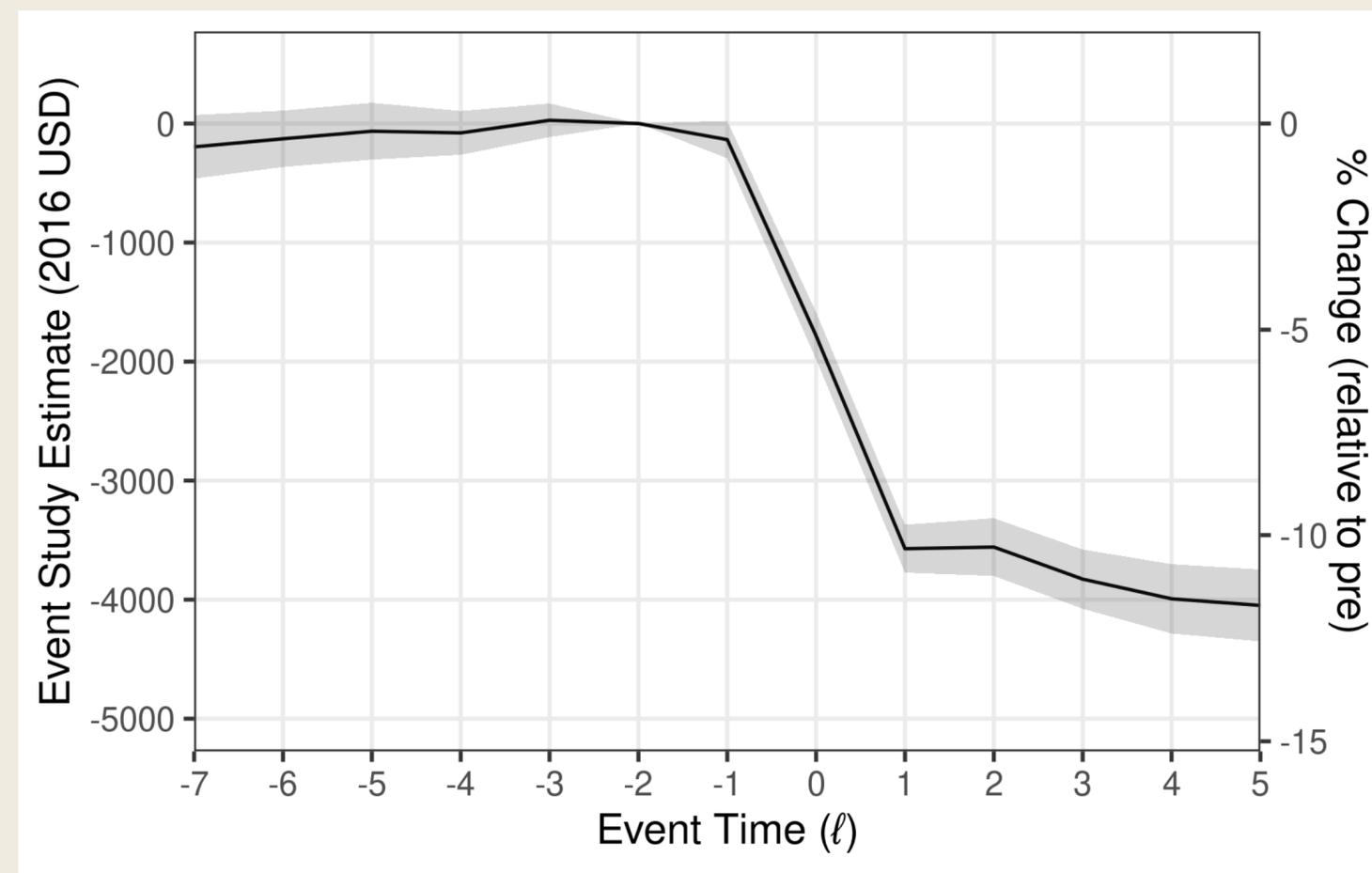
- Golosov, Graber, Mogstad & Novgorodsky (2023):  
Study the labor supply responses of US lottery winners
- US tax data for 1999-2016
  - Lottery winnings are taxable income
- Median size of post-tax winning: \$43,600
- 90,731 lottery winners in the sample
- Compare the response to lottery winnings relative to later winners

# Labor Supply Response to Lottery Winning

## Employment



## Wage Earnings



Source: Golosov, Graber, Mogstad & Novgorodsky (2023)

# MPE Estimates

Table 4.1: IV estimates of the effect of exogenous change in unearned income

Outcome	Sample				
	Full Sample	Quartile 1 Pre-Win Income	Quartile 2 Pre-Win Income	Quartile 3 Pre-Win Income	Quartile 4 Pre-Win Income
	(1)	(2)	(3)	(4)	(5)
Per-Adult Total Labor Earnings	-0.5227 (0.0146)	-0.3080 (0.0240)	-0.5204 (0.0197)	-0.5893 (0.0221)	-0.6735 (0.0389)

Source: Golosov, Graber, Mogstad & Novgorodsky (2023)

- Therefore

$$\frac{d(wl)}{dT} = - \frac{\sigma s_w}{[\sigma s_w + \nu]} \approx -0.52$$

- Assuming  $s_w \approx 2/3$  (labor share) and  $\nu \in [0.025, 0.5]$  (micro estimates) implies

$$\sigma \in [0.04, 0.8]$$

- Can be large, but not as large as  $\sigma > 1$

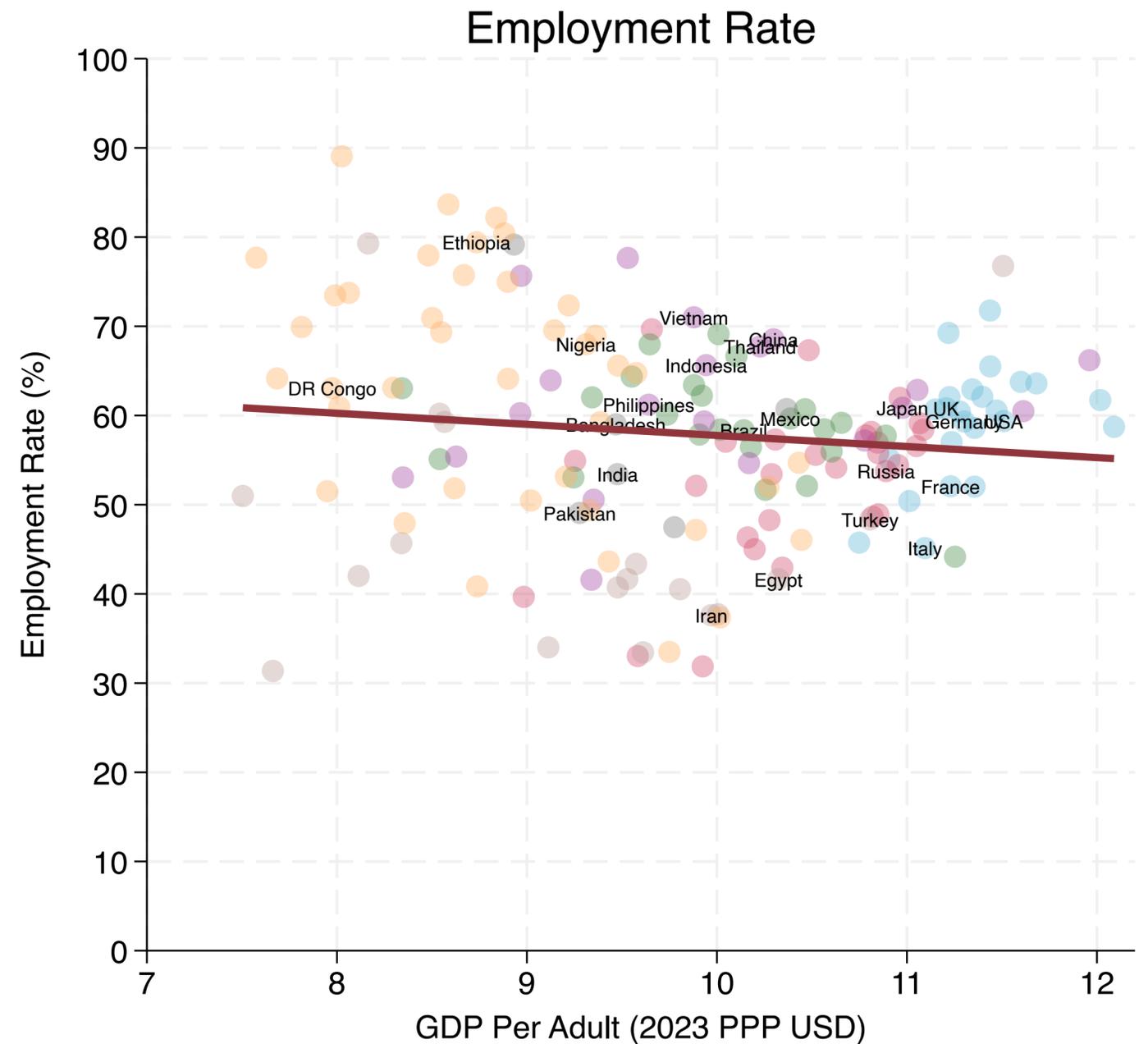
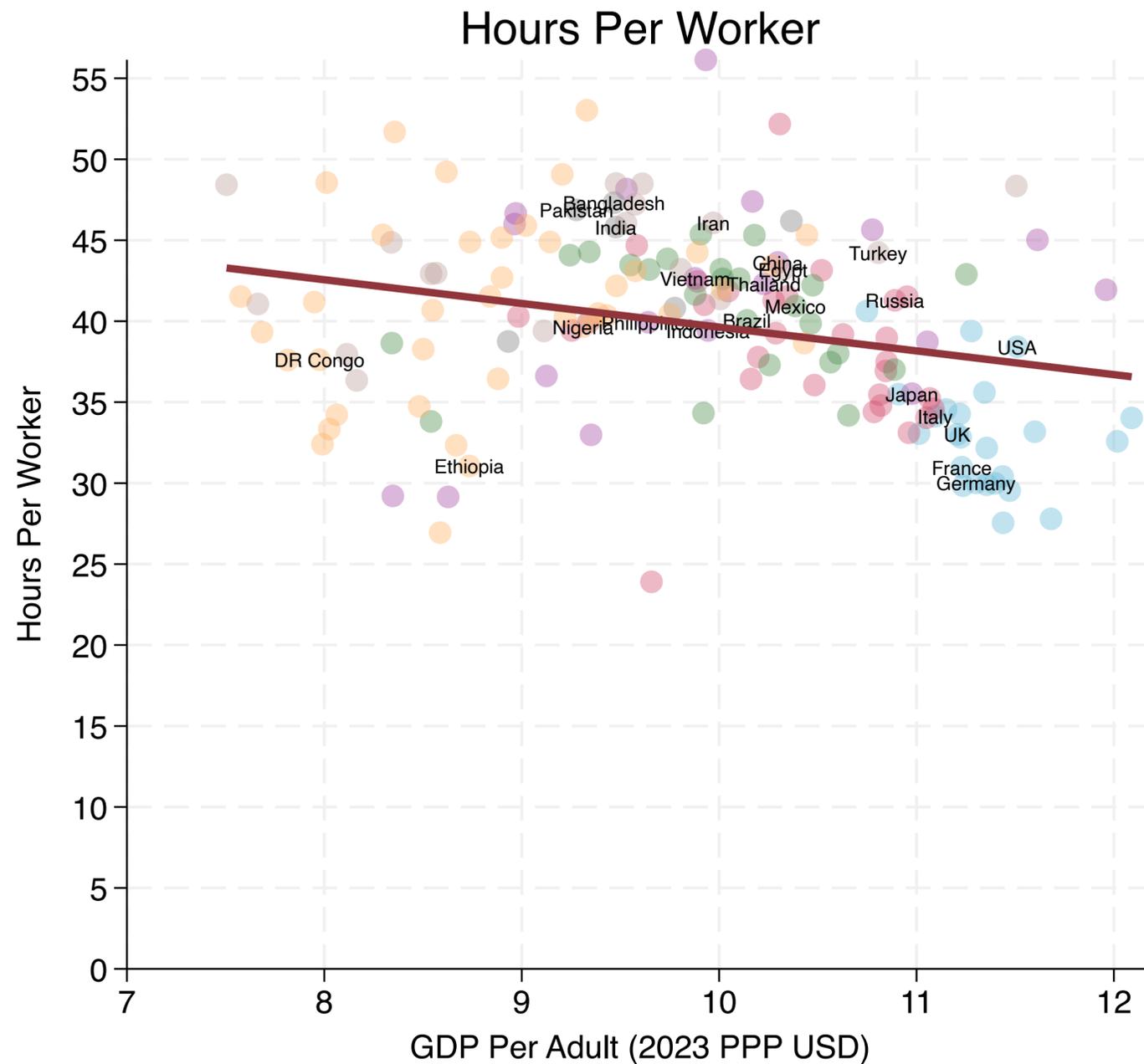
Chetty, Guren, Manoli, & Weber (2013),  
Martínez, Saez, & Siegenthaler (2021)

---

# **Closer Look at the Data**

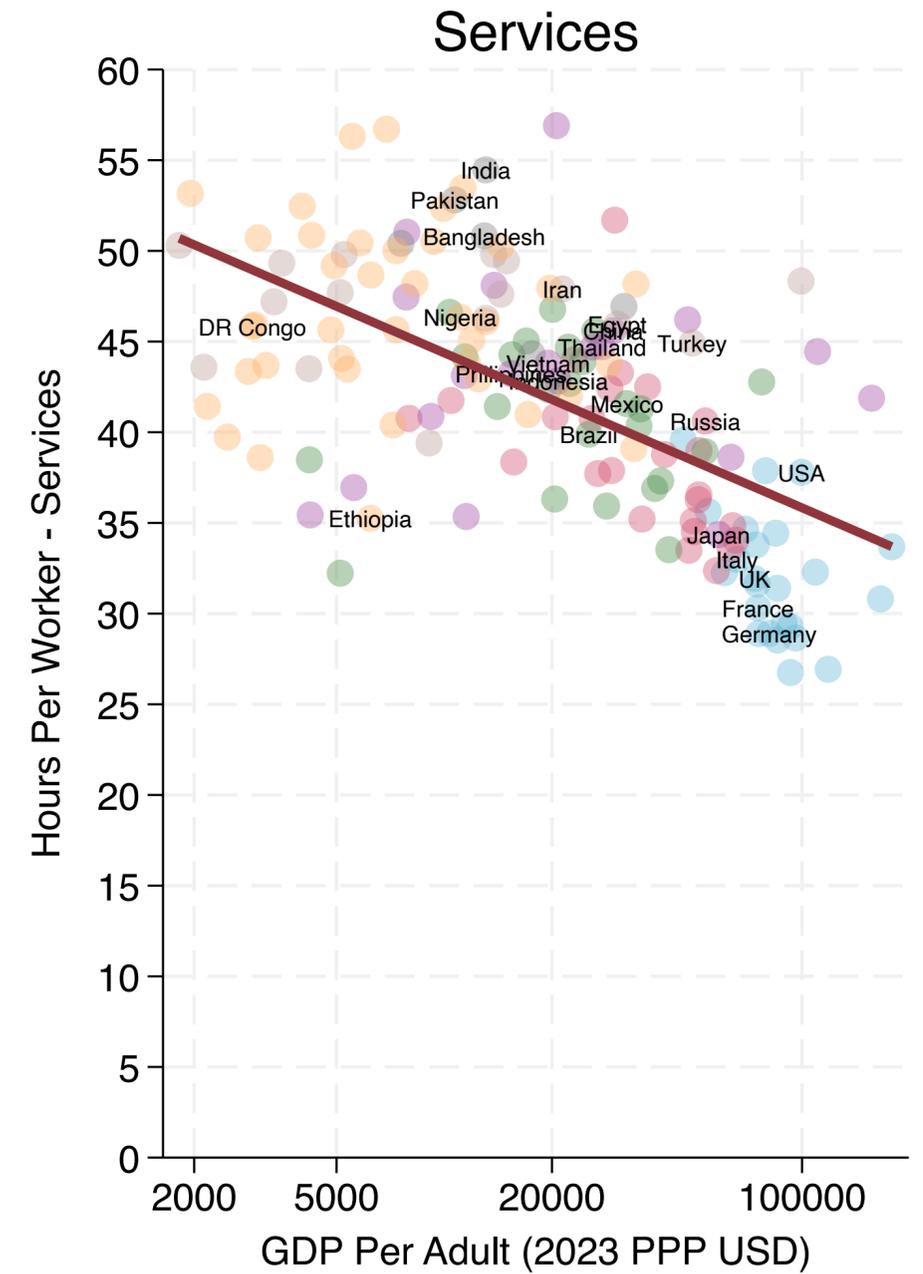
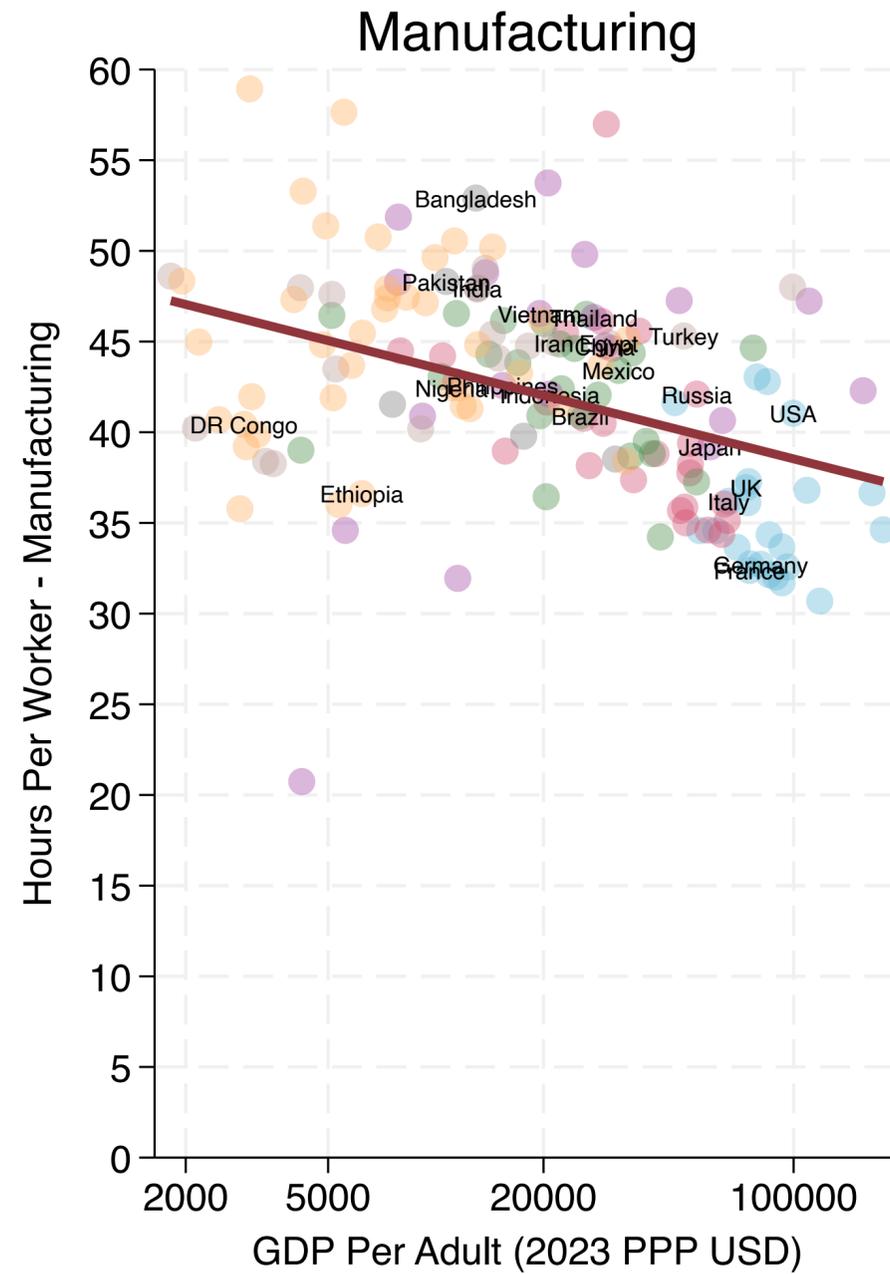
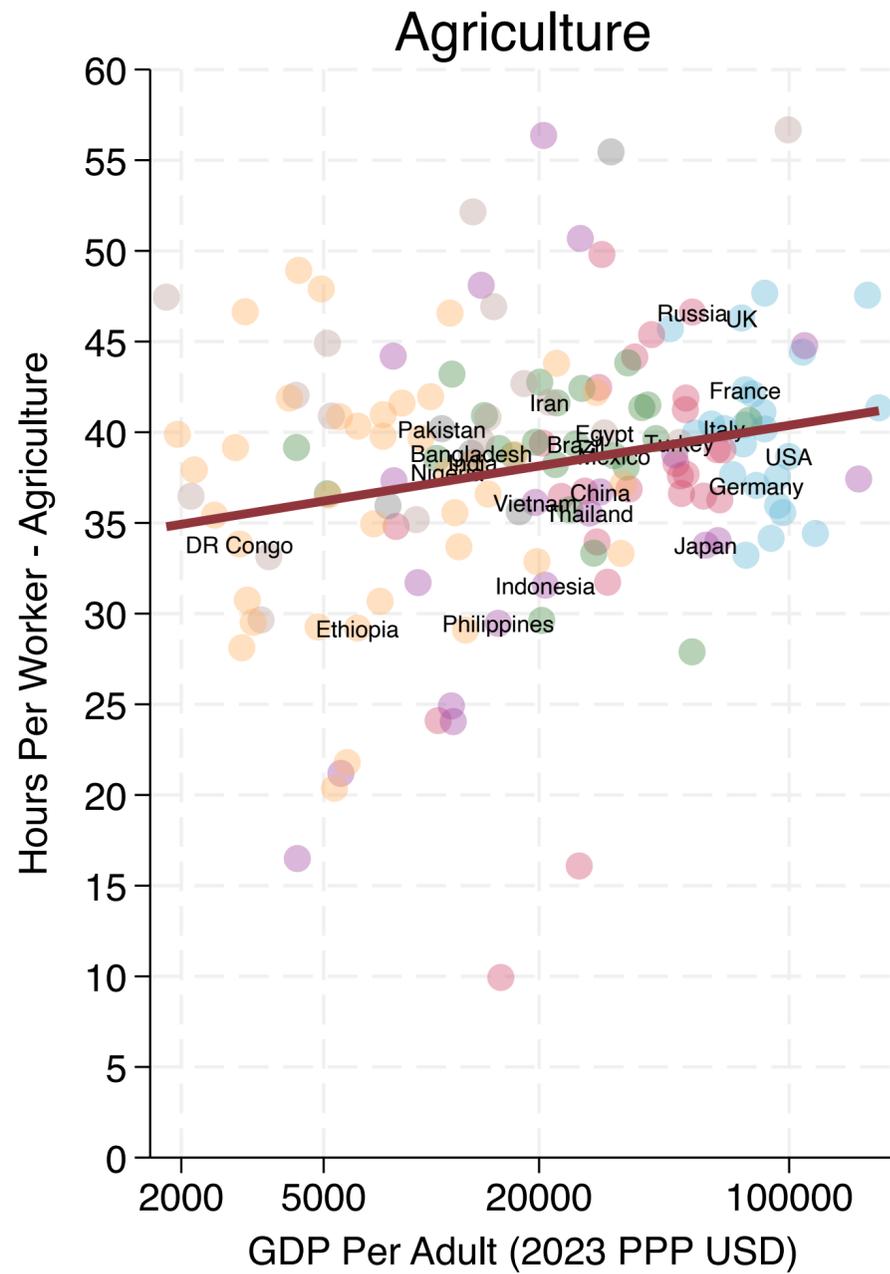
## **– Gethin & Saez (2026)**

# Hours per Worker vs. Employment



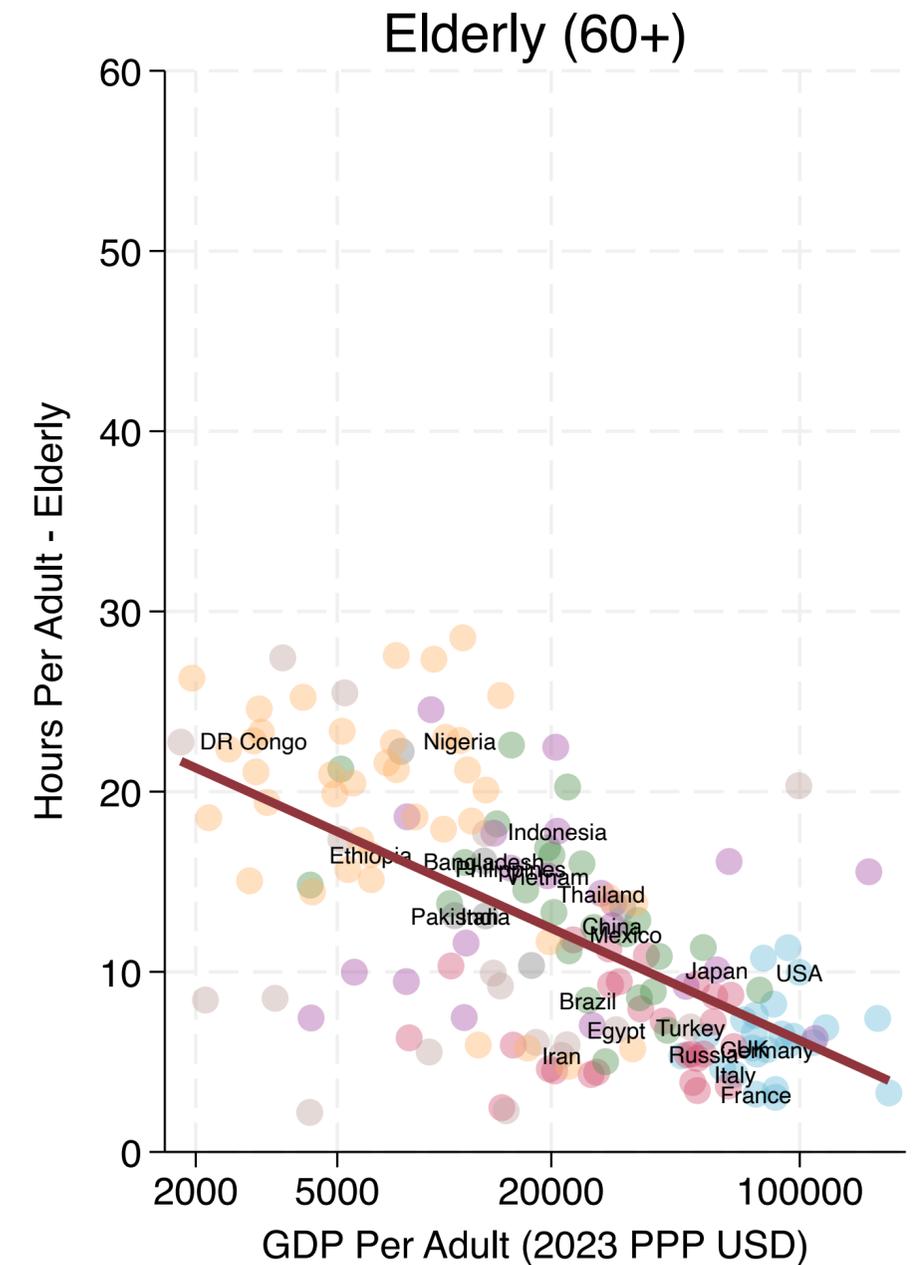
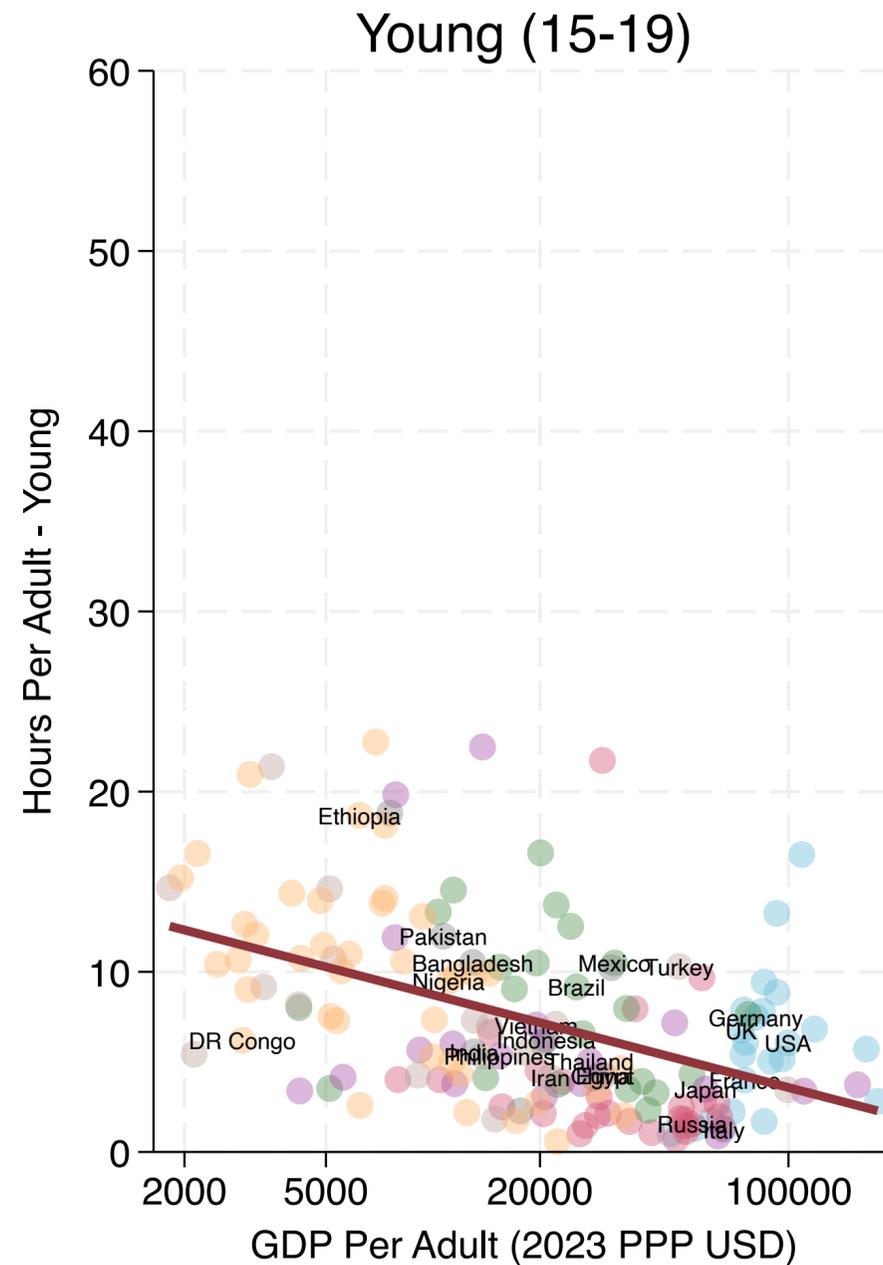
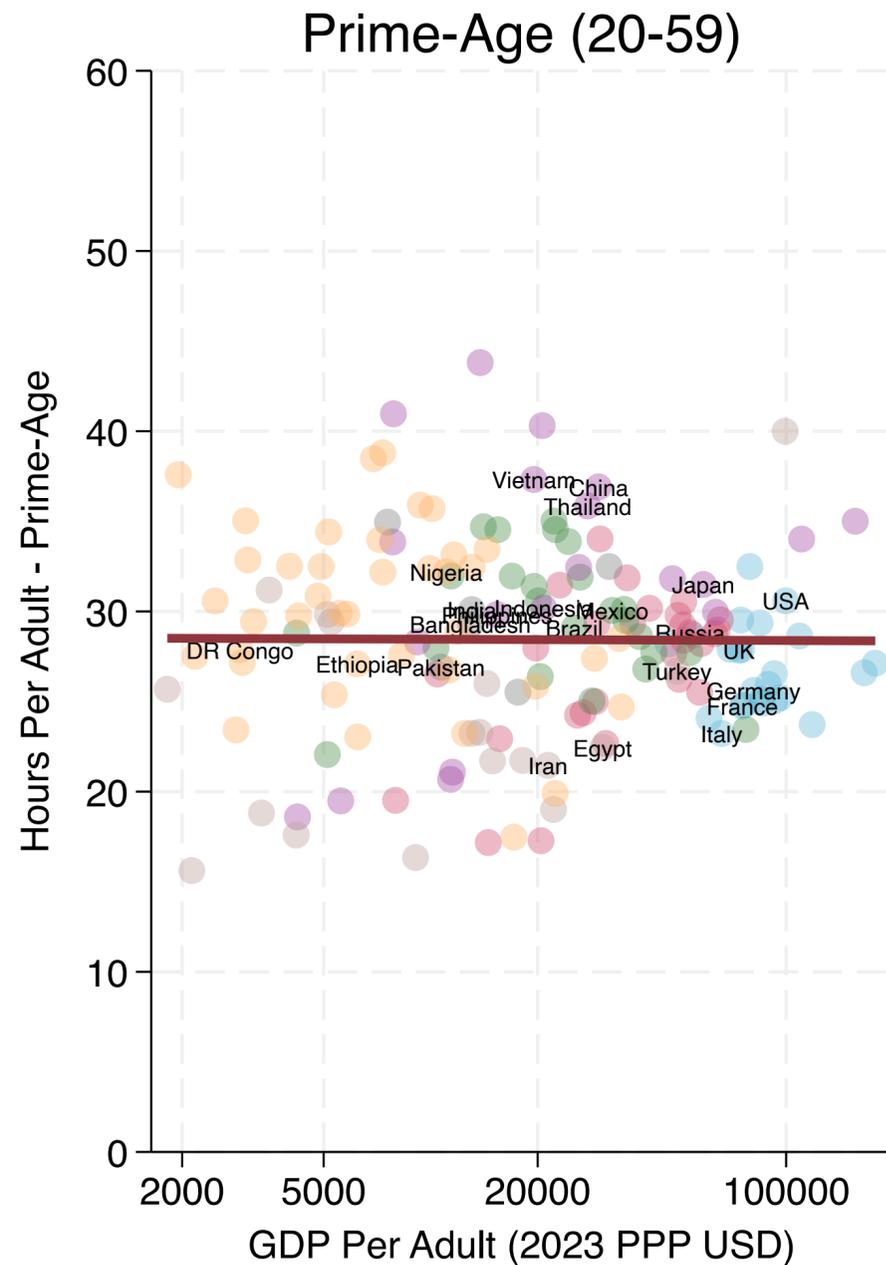
Data: Gethin and Saez (2026)

# By Sector



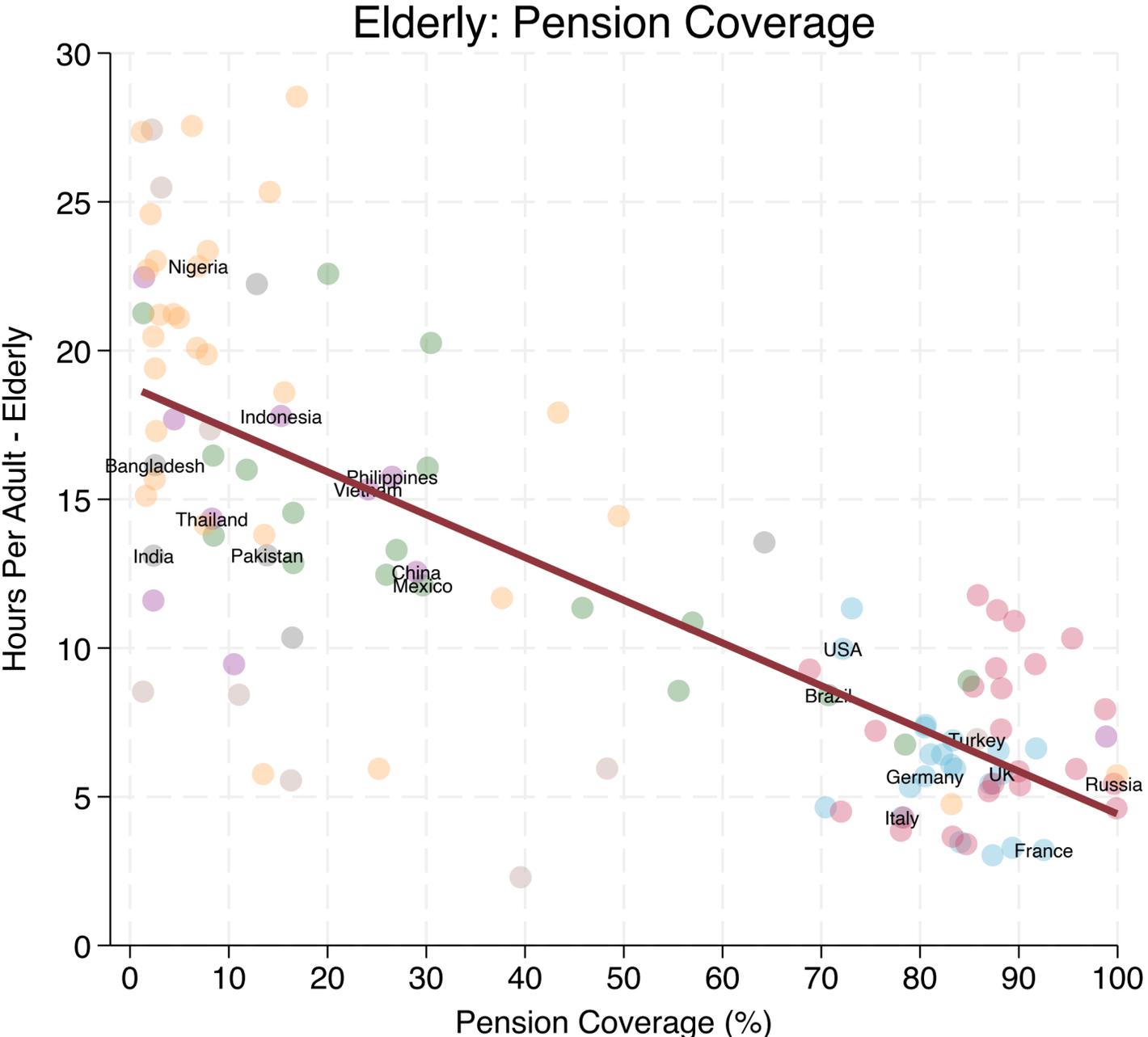
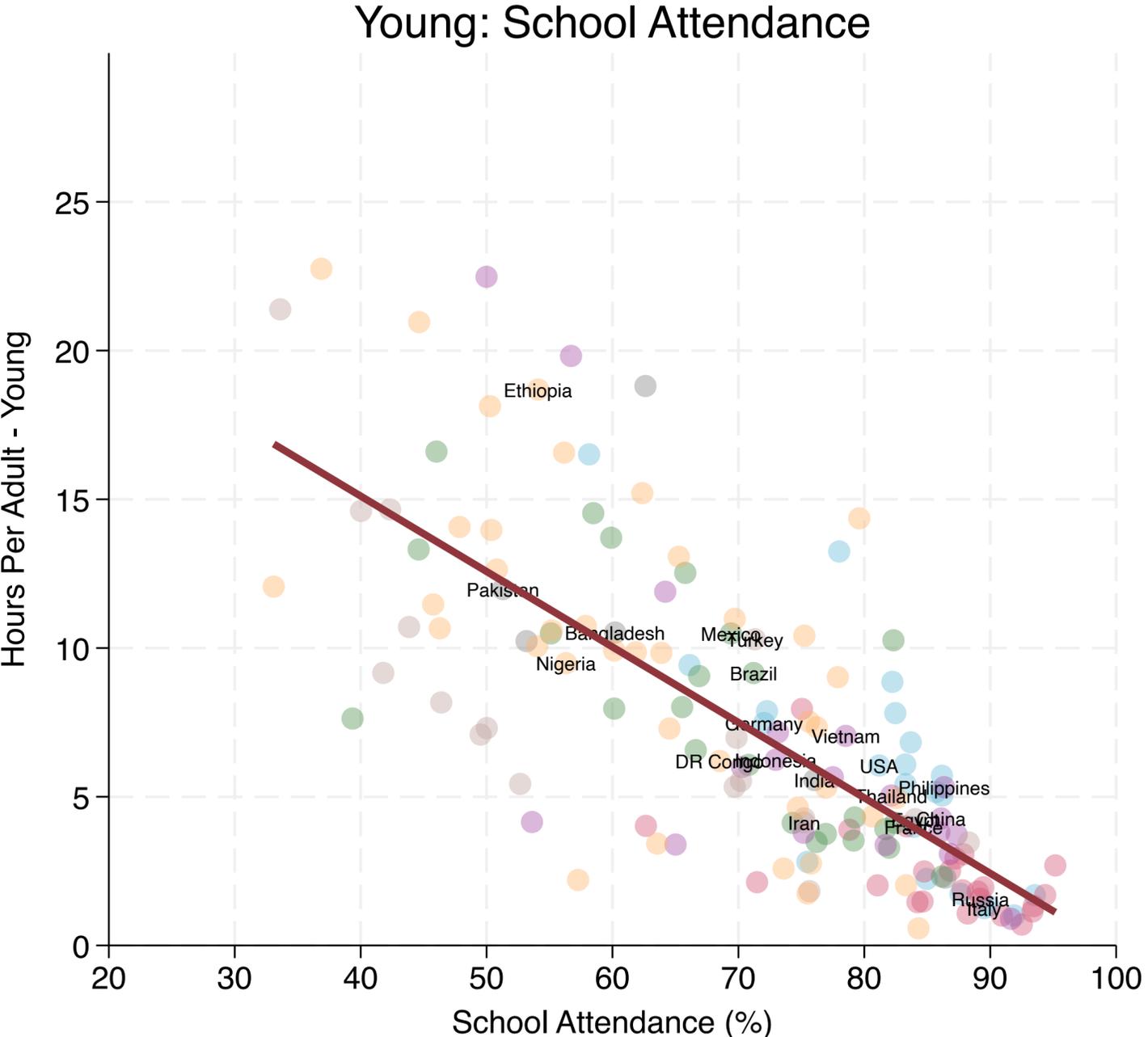
Data: Gethin and Saez (2026)

# By Age Group



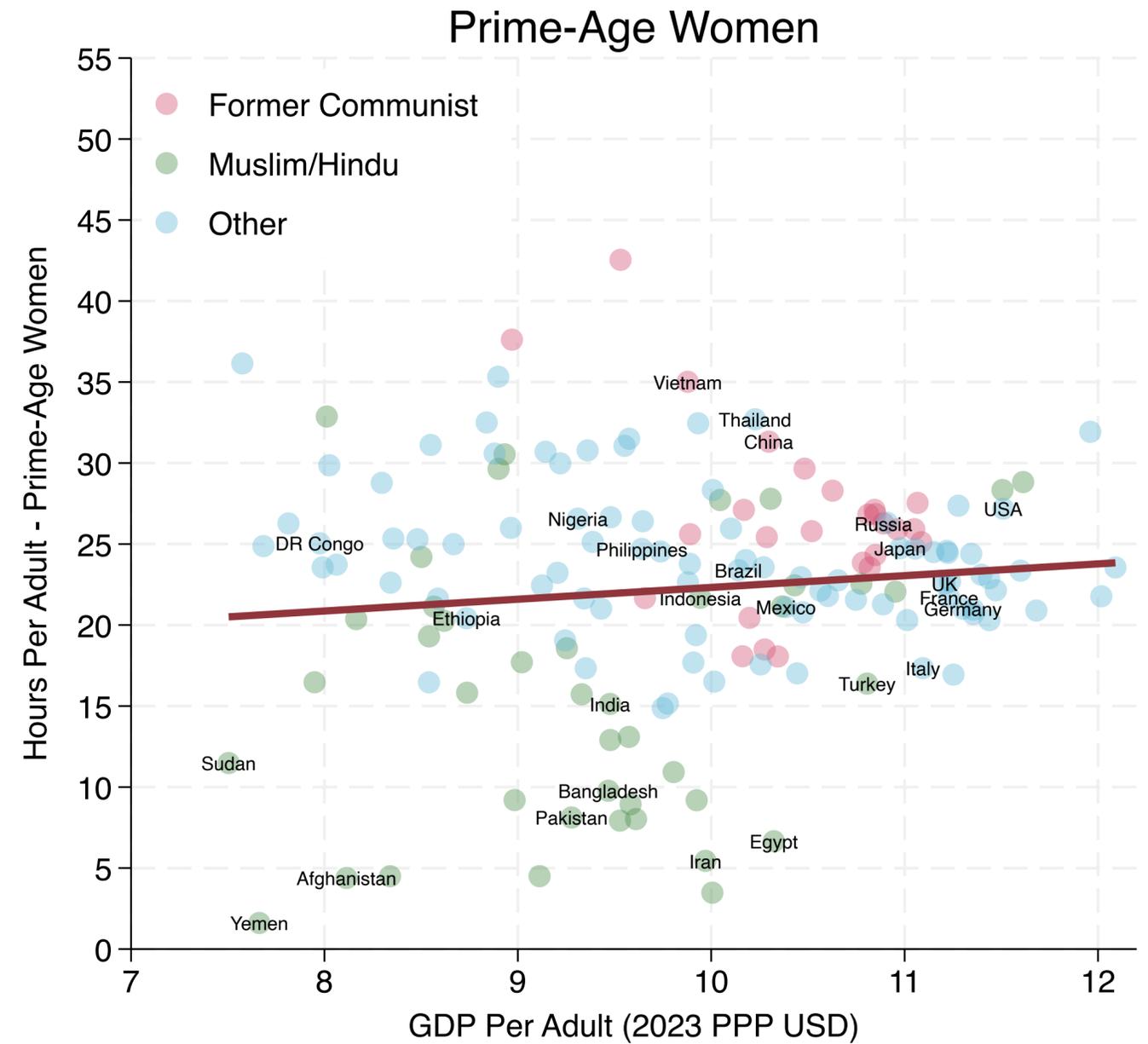
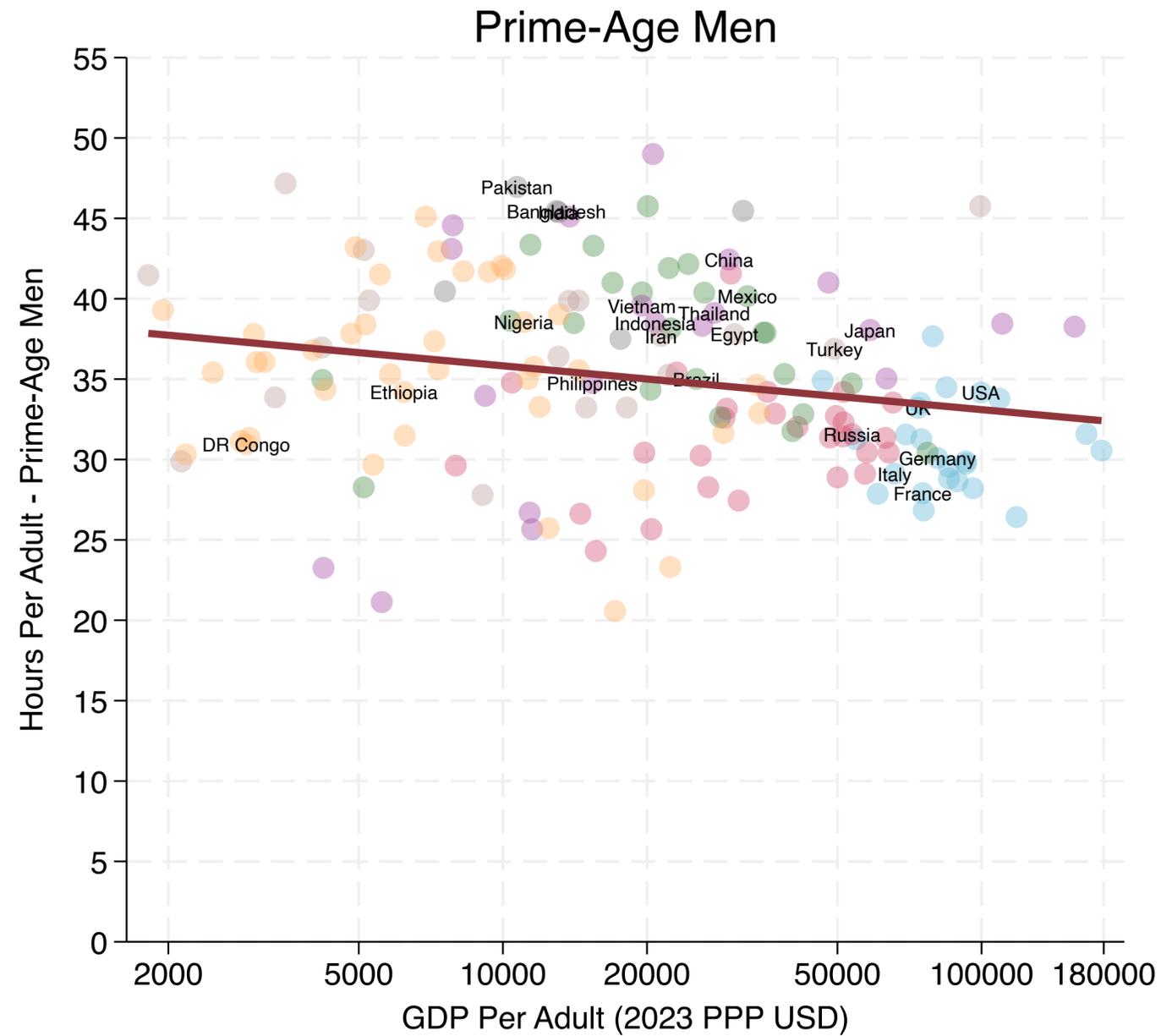
Data: Gethin and Saez (2026)

# The Importance of Schooling and Pension



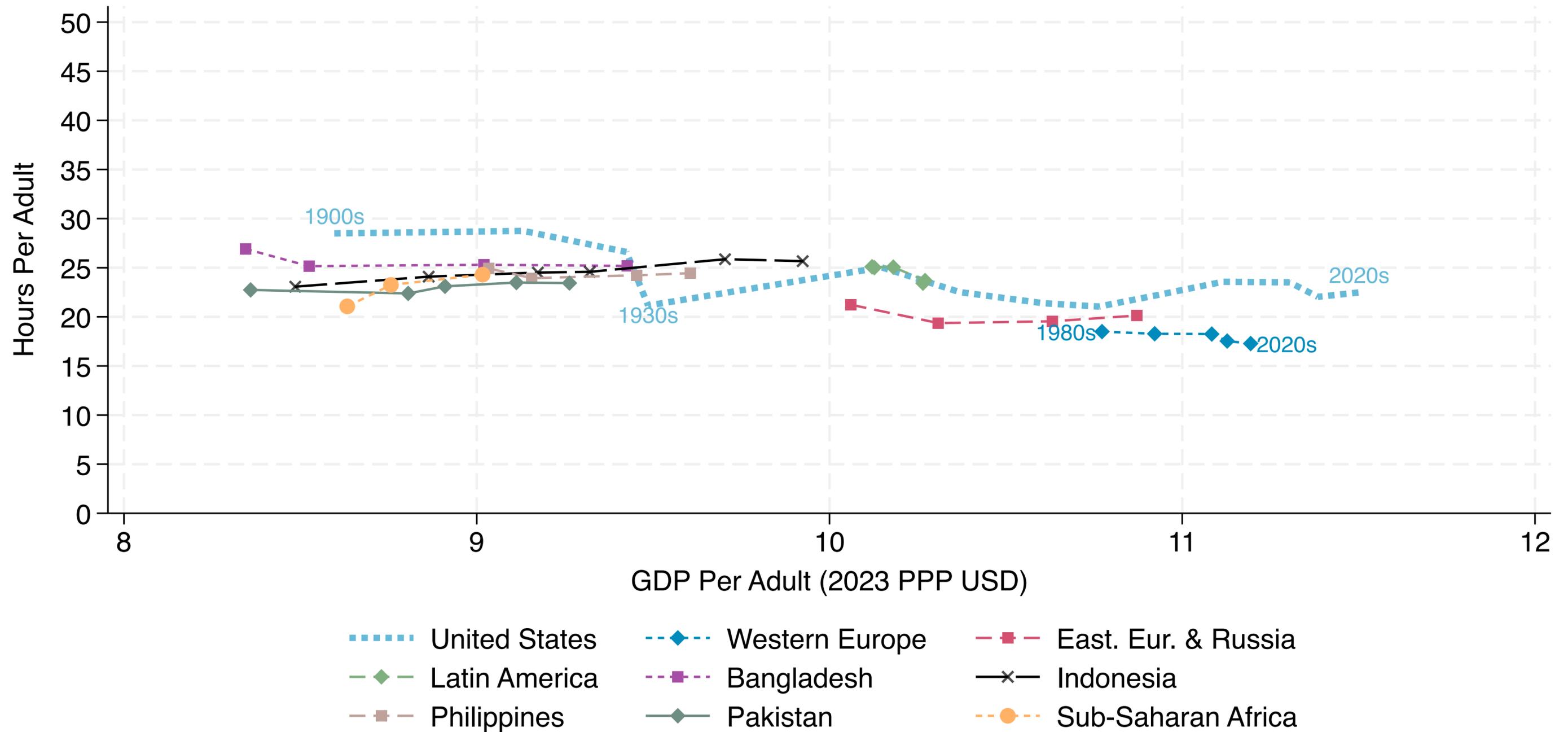
Data: Gethin and Saez (2026)

# By Gender

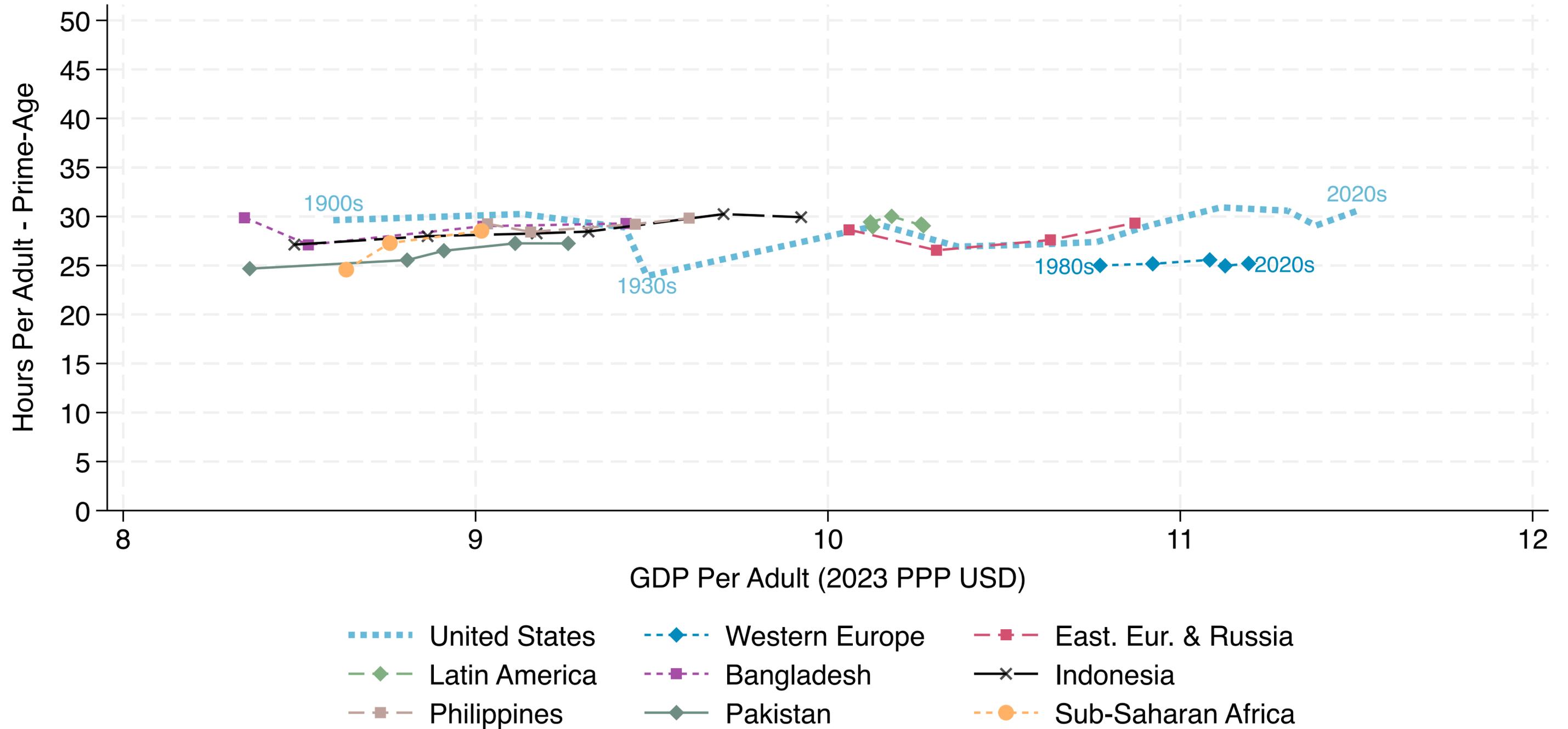


Data: Gethin and Saez (2026)

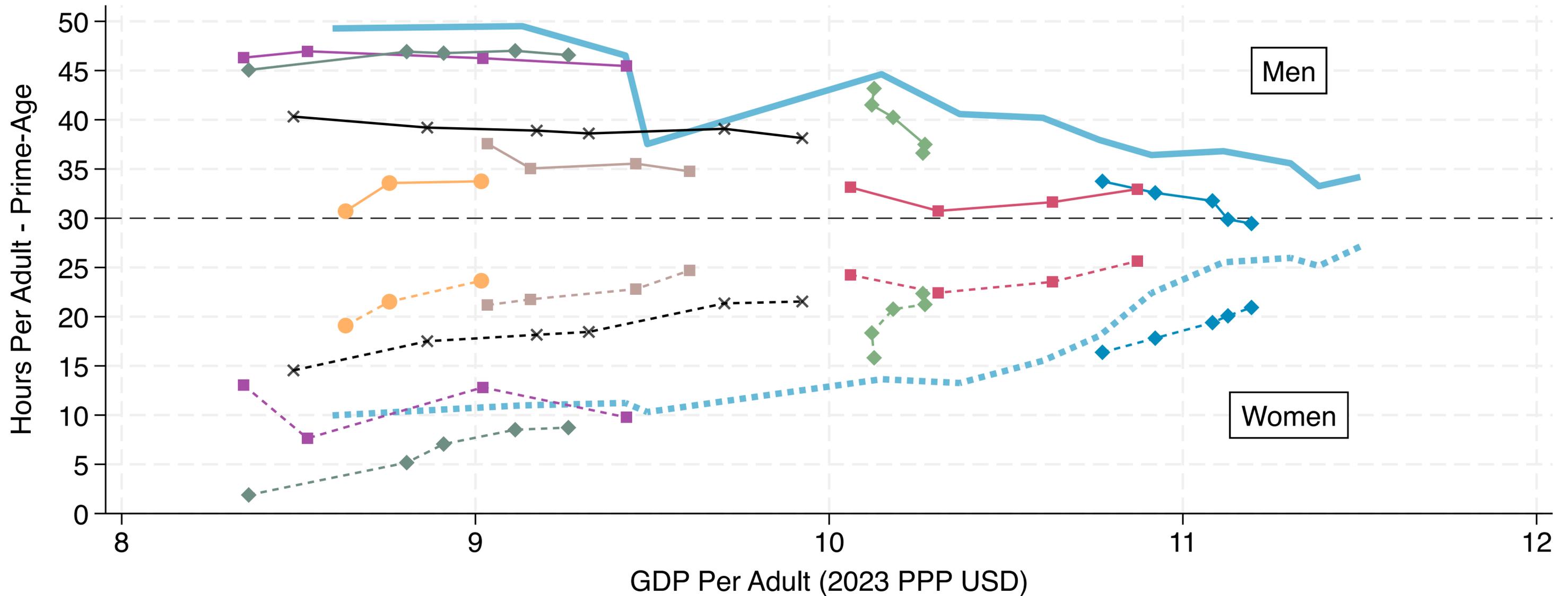
# Over Time



# Prime Age (20-59)

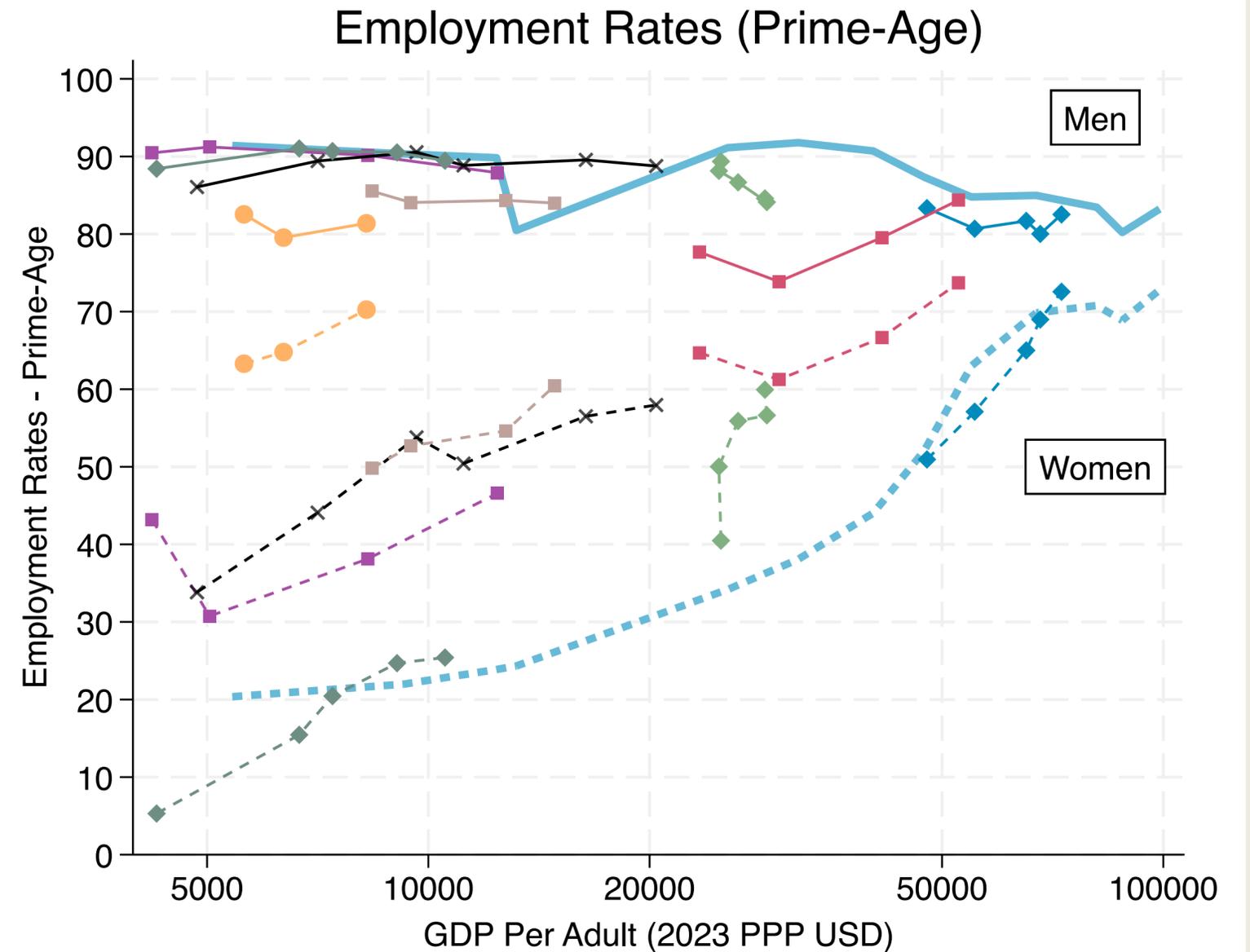
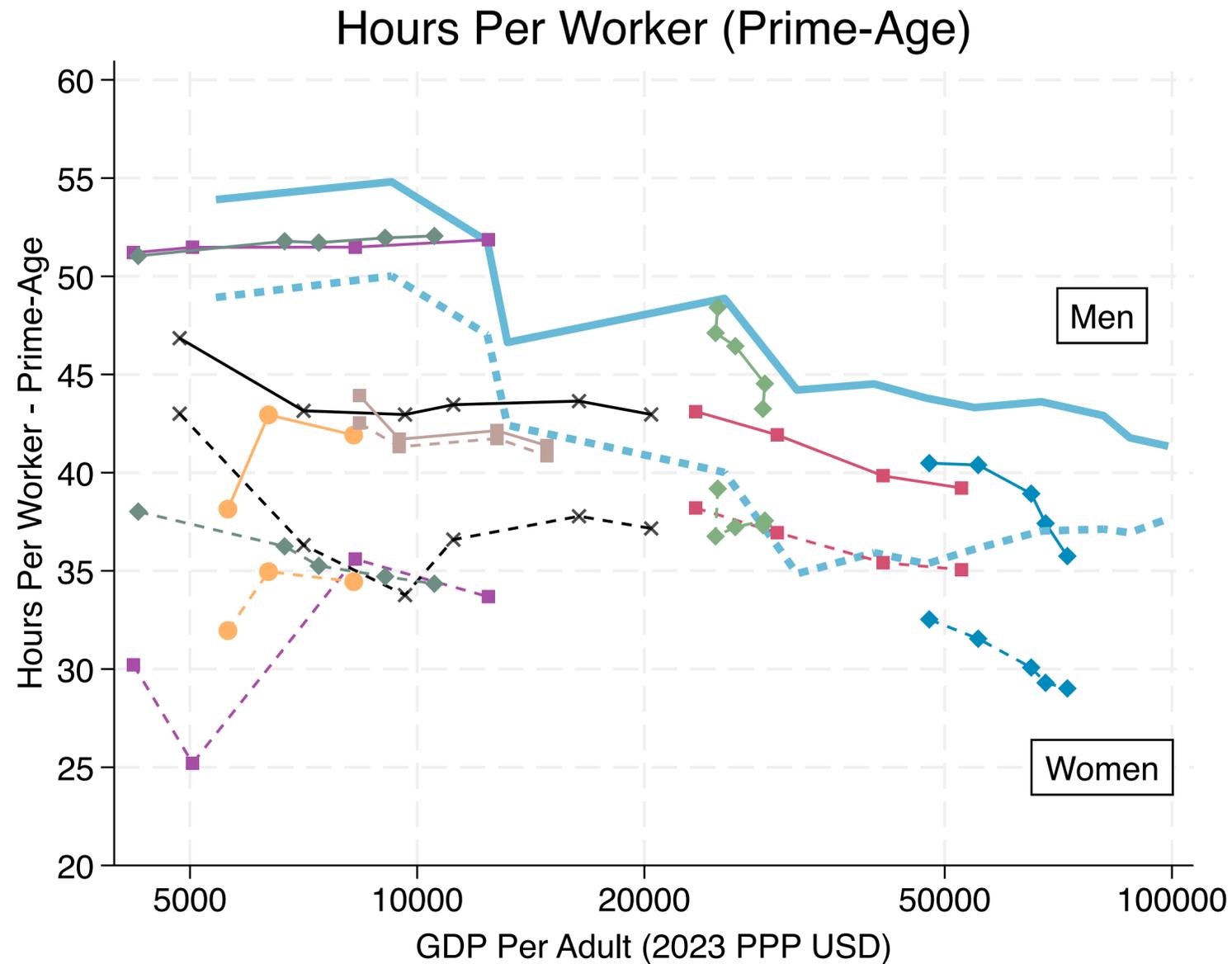


# Prime Age by Gender



- ◆— United States
- ◆- Western Europe
- East. Eur. & Russia
- ◆- Latin America
- Bangladesh
- x- Indonesia
- Philippines
- ◆- Pakistan
- Sub-Saharan Africa

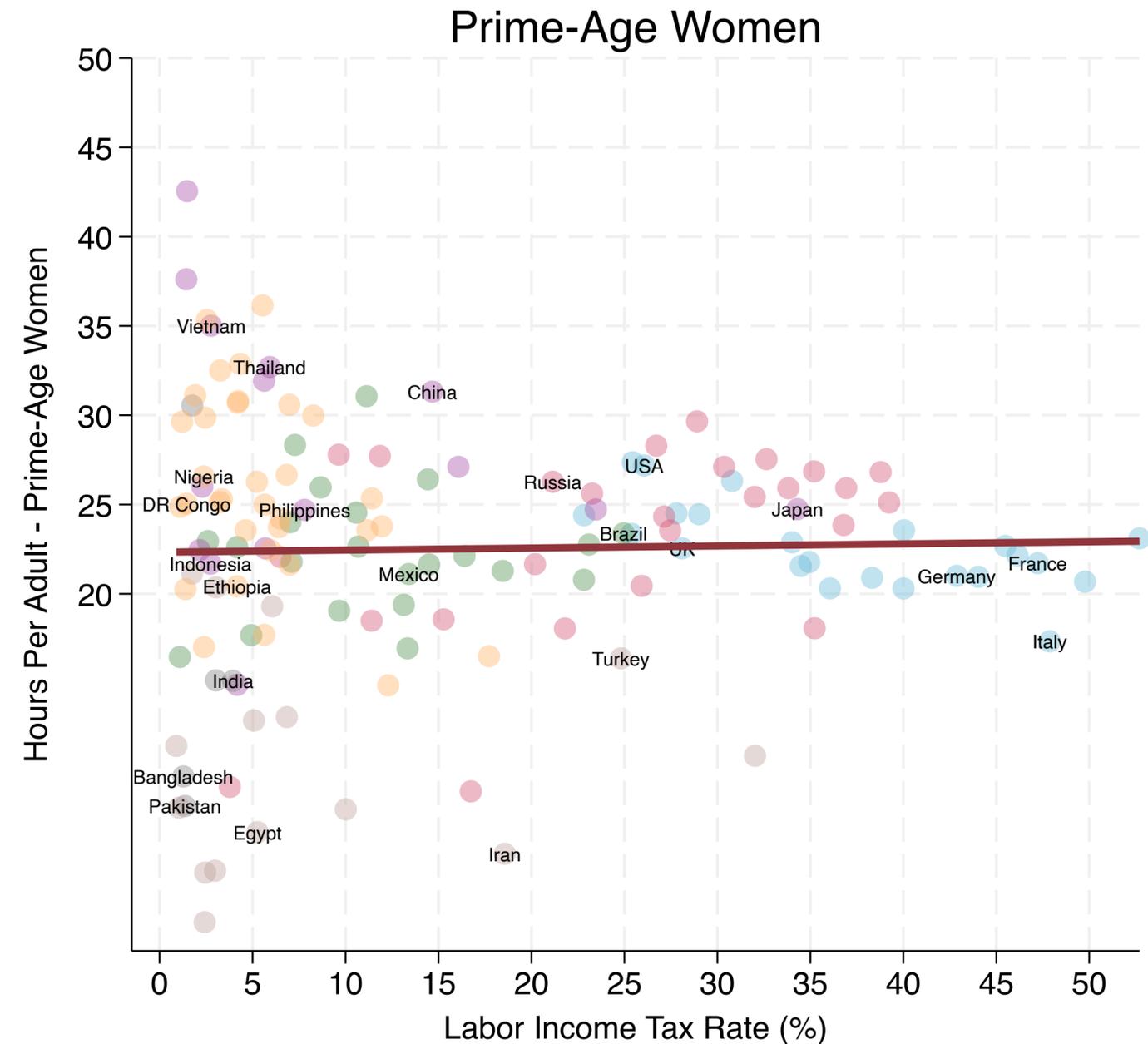
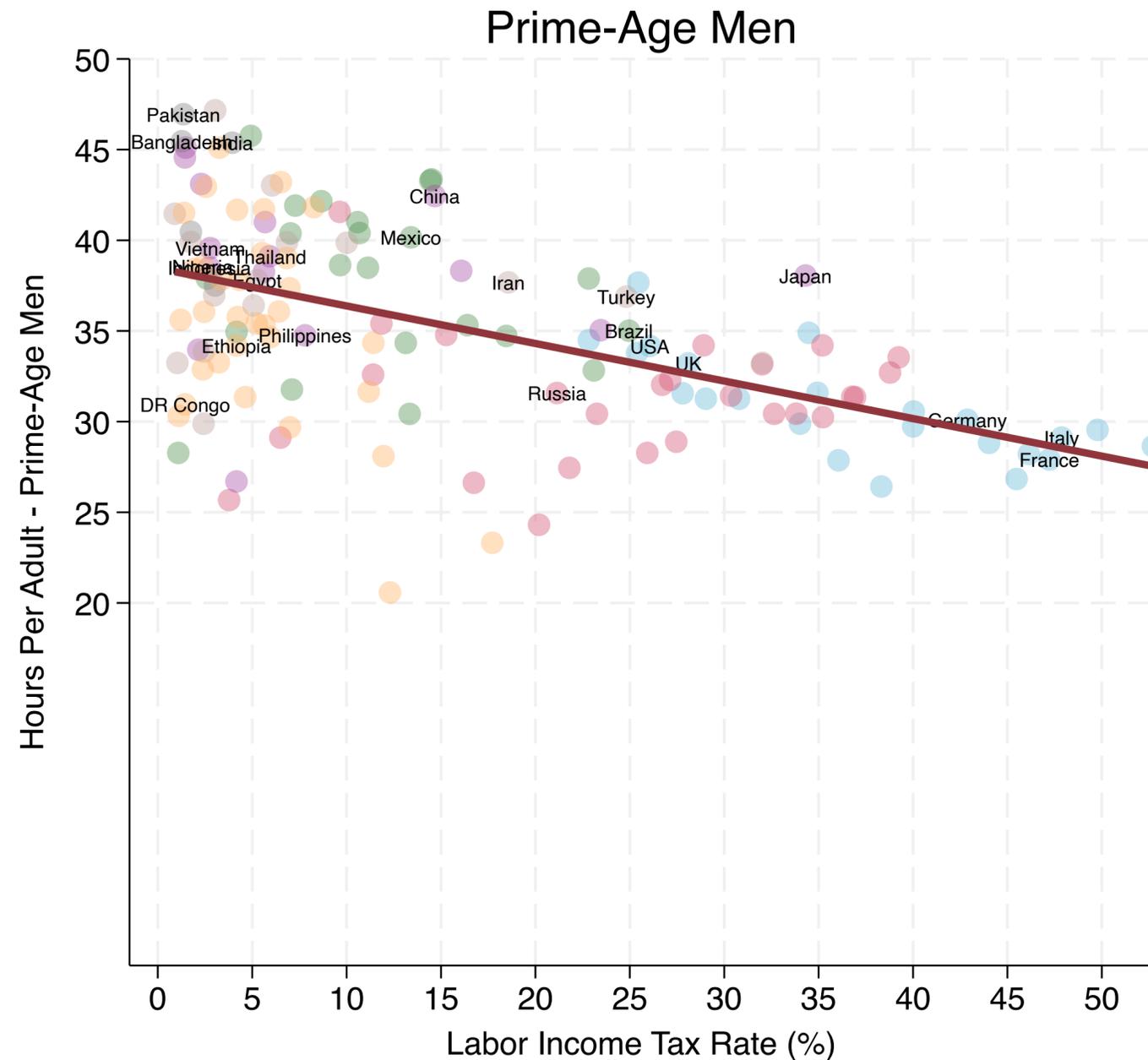
# Hours per Worker vs. Employment



- United States
- Latin America
- Philippines
- Western Europe
- Bangladesh
- Pakistan
- East. Eur. & Russia
- Indonesia
- Sub-Saharan Africa

- United States
- Latin America
- Philippines
- Western Europe
- Bangladesh
- Pakistan
- East. Eur. & Russia
- Indonesia
- Sub-Saharan Africa

# Role of Labor Income Tax



Data: Gethin and Saez (2026)